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# GDR Neutrino Meeting

*Present and future challenges  
in neutrino oscillations*

Thomas Schwetz  
SISSA, Trieste

T.S. is supported by an Intra-European Marie Curie fellowship  
of the European Commission within the 6th framework program

# *Outline*

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- **Introduction**  
status of three-flavour neutrino oscillations

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- **Determination of neutrino oscillation parameters by future experiments**  
leading solar and atmospheric parameters  
determination of  $\theta_{13}$ , the CP-phase, and the mass hierarchy

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determination of  $\theta_{13}$ , the CP-phase, and the mass hierarchy
- **Summary**

# *Before starting...*

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I will not speak about determination of the  
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- tritium beta decay experiments
- neutrino-less double-beta decay experiments
- cosmological observations

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but I stress that  
**such experiments are an important part of the neutrino  
program, and provide complementary information to  
oscillation experiments**

# *Introduction*

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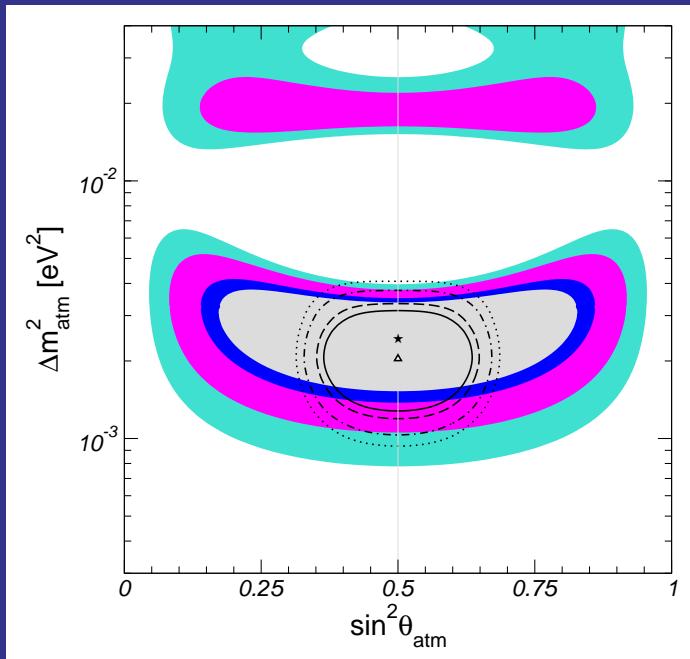
Evidences for neutrino oscillations:

# *Introduction*

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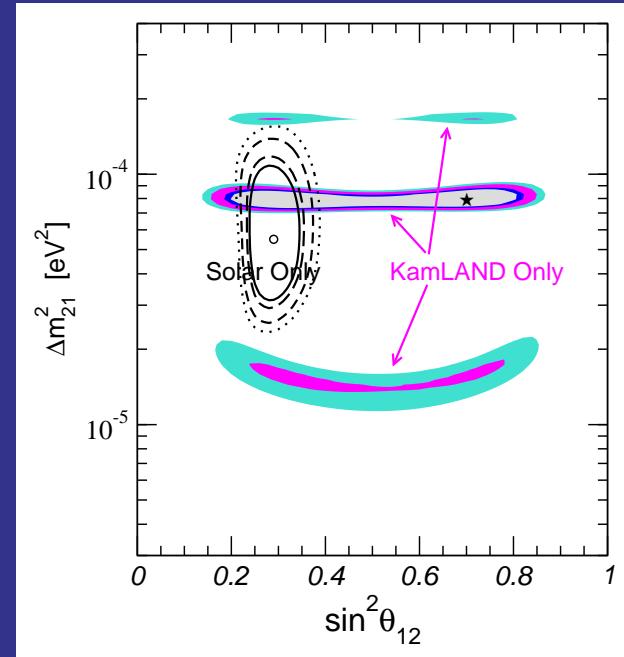
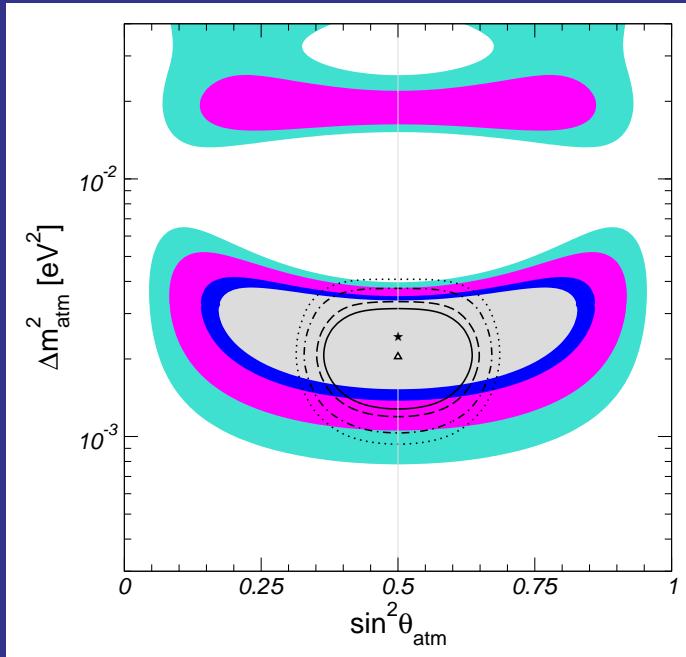
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# *Introduction*

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**natural explanation in three-flavour framework**

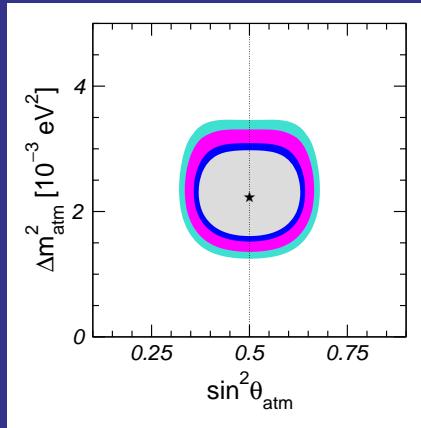
# *3-flavour oscillation parameters*

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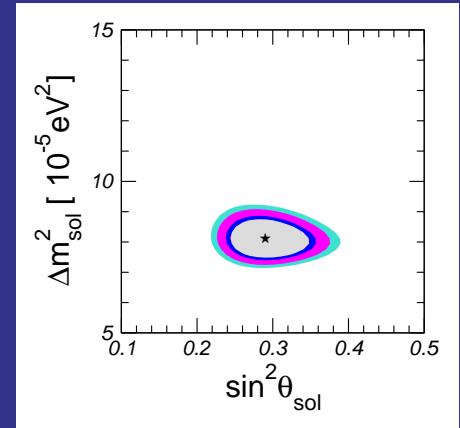
$$\Delta m_{31}^2 \qquad \qquad \qquad \Delta m_{21}^2$$
$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & e^{-i\delta} s_{13} \\ 0 & 1 & 0 \\ -e^{i\delta} s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

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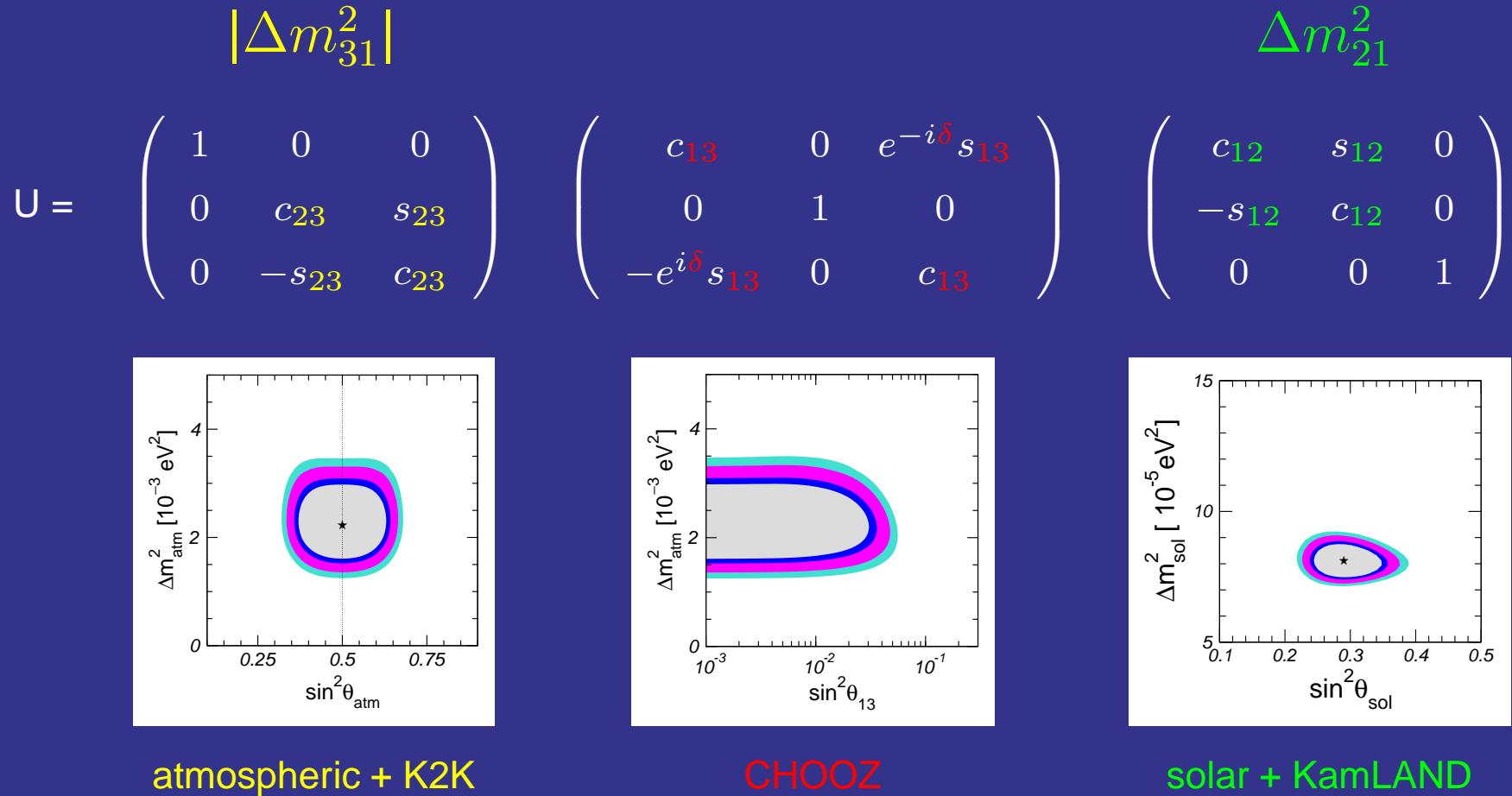
atmospheric + K2K



solar + KamLAND

Maltoni, Schwetz, Tortola, Valle, hep-ph/0405172; Fogli, Lisi, Marrone, Palazzo, hep-ph/0506083; Gonzalez-Garcia, Pena-Garay, PRD **68** (2003) 093003; Bahcall, Gonzalez-Garcia, Pena-Garay, JHEP **0408** (2004) 016; de Holanda, Smirnov, Astropart. Phys. **21** (2004) 287; Bandyopadhyay, Choubey, Goswami, Petcov, Roy, hep-ph/0406328; Strumia, Vissani, hep-ph/0503246.

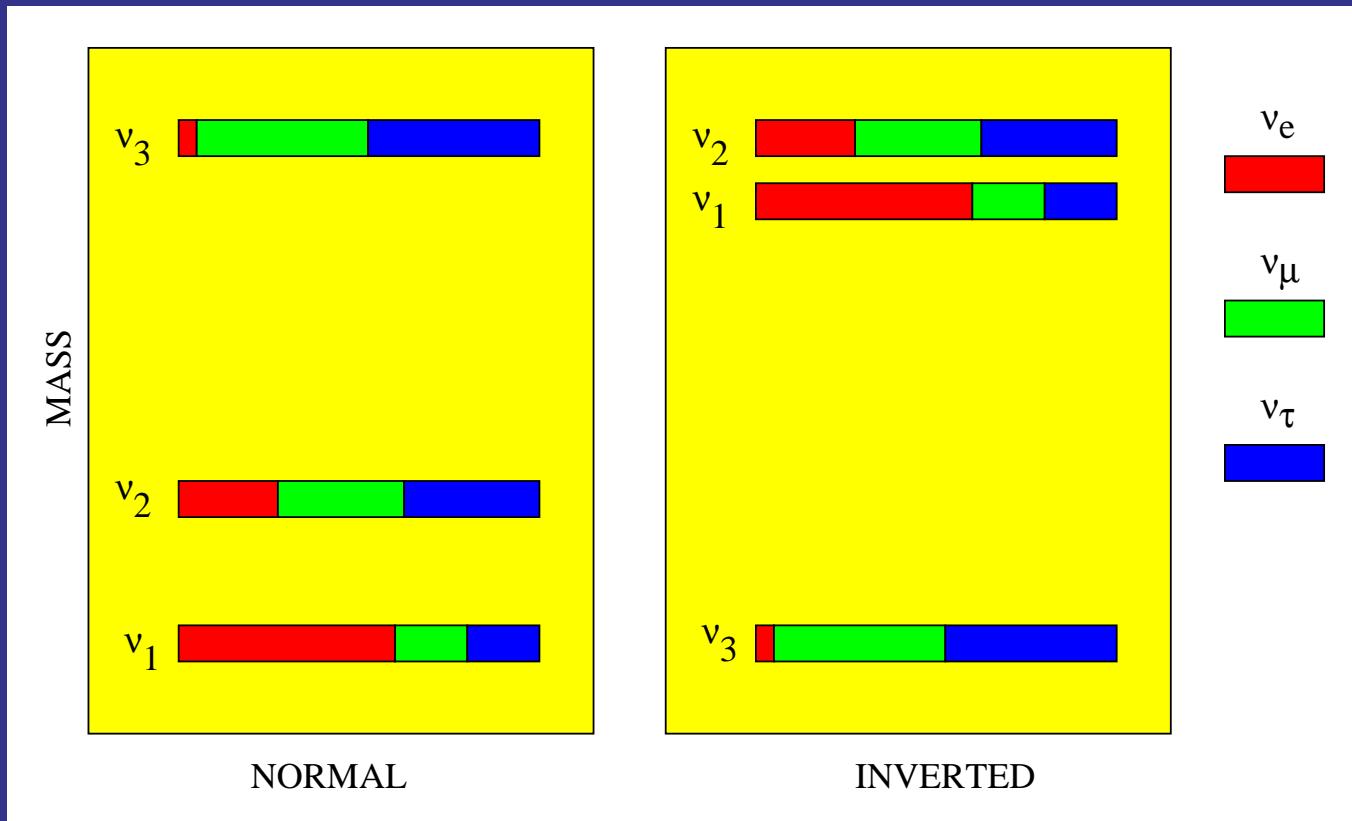
# 3-flavour oscillation parameters



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# 3-flavour oscillation parameters

Two possibilities for the neutrino mass spectrum:



$$\Delta m_{31}^2 > 0$$

$$\Delta m_{31}^2 < 0$$

# *3-flavour oscillation parameters*

## mass-squared differences:

parameter	bf $\pm 1\sigma$	$1\sigma$ acc.	$3\sigma$ range
$\Delta m_{21}^2$ [10 $^{-5}$ eV $^2$ ]	$7.9 \pm 0.3$	4%	7.1 – 8.9
$ \Delta m_{31}^2 $ [10 $^{-3}$ eV $^2$ ]	$2.2^{+0.37}_{-0.27}$	14%	1.4 – 3.3

## mixing angles:

parameter	bf $\pm 1\sigma$	$1\sigma$ acc.	$3\sigma$ range
$\sin^2 \theta_{12}$	$0.31^{+0.02}_{-0.03}$	9%	0.24 – 0.40
$\sin^2 \theta_{23}$	$0.50^{+0.06}_{-0.05}$	11%	0.34 – 0.68
$\sin^2 \theta_{13}$	—	—	$\leq 0.046$

updated from M. Maltoni, T. Schwetz, M.A. Tortola and J.W.F. Valle, hep-ph/0405172

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# The LSND puzzle

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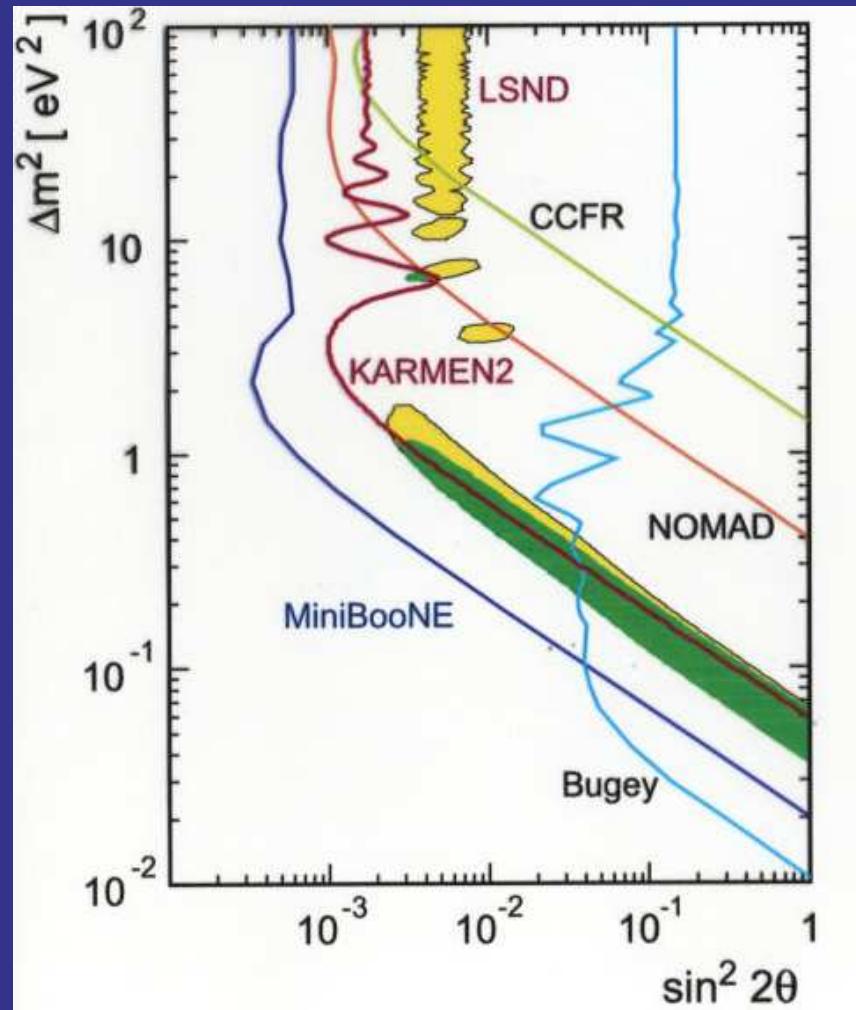
evidence for  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  oscillations

A. Aguilar *et al.*, PRD 64 (2001) 112007

$87.9 \pm 22.4 \pm 6.0$  excess events

$P = (0.264 \pm 0.067 \pm 0.045)\%$

$\sim 3.3\sigma$  away from zero



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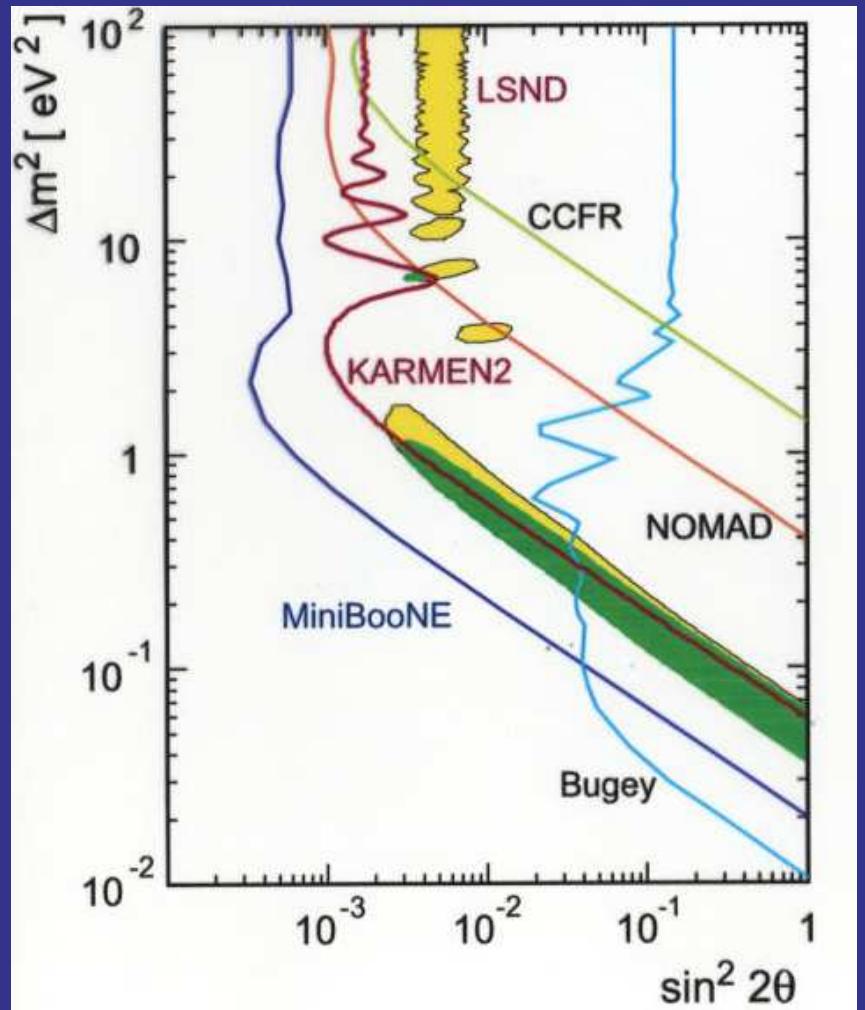
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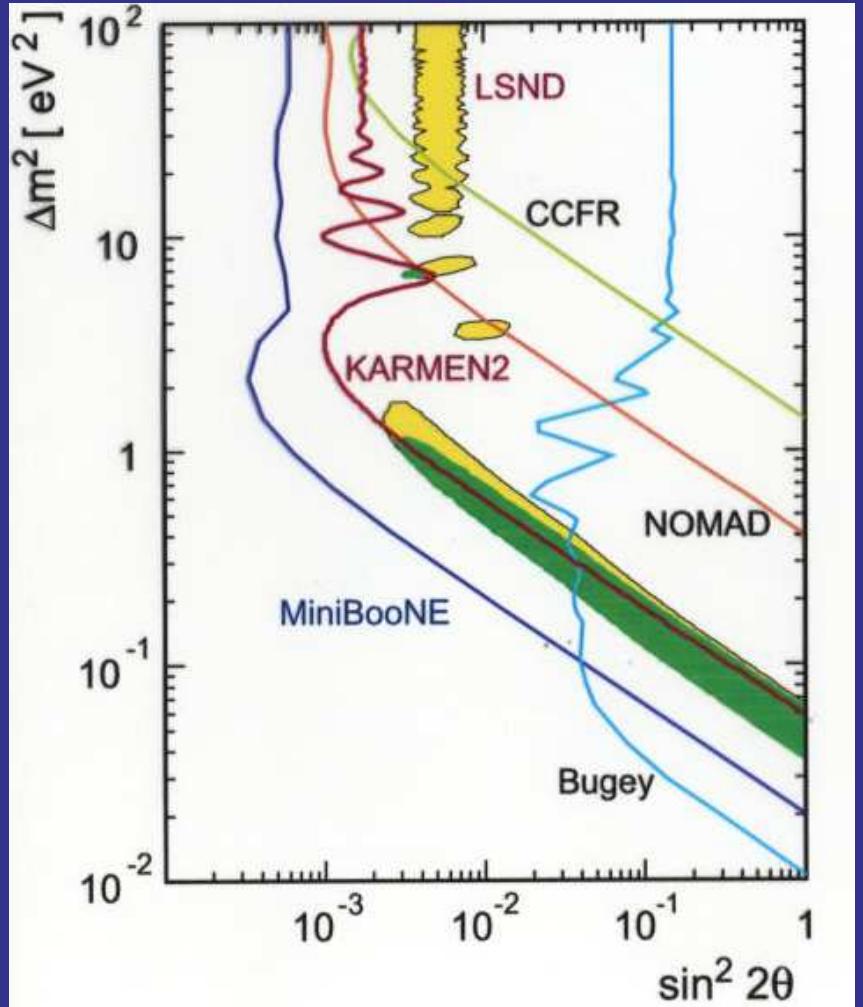
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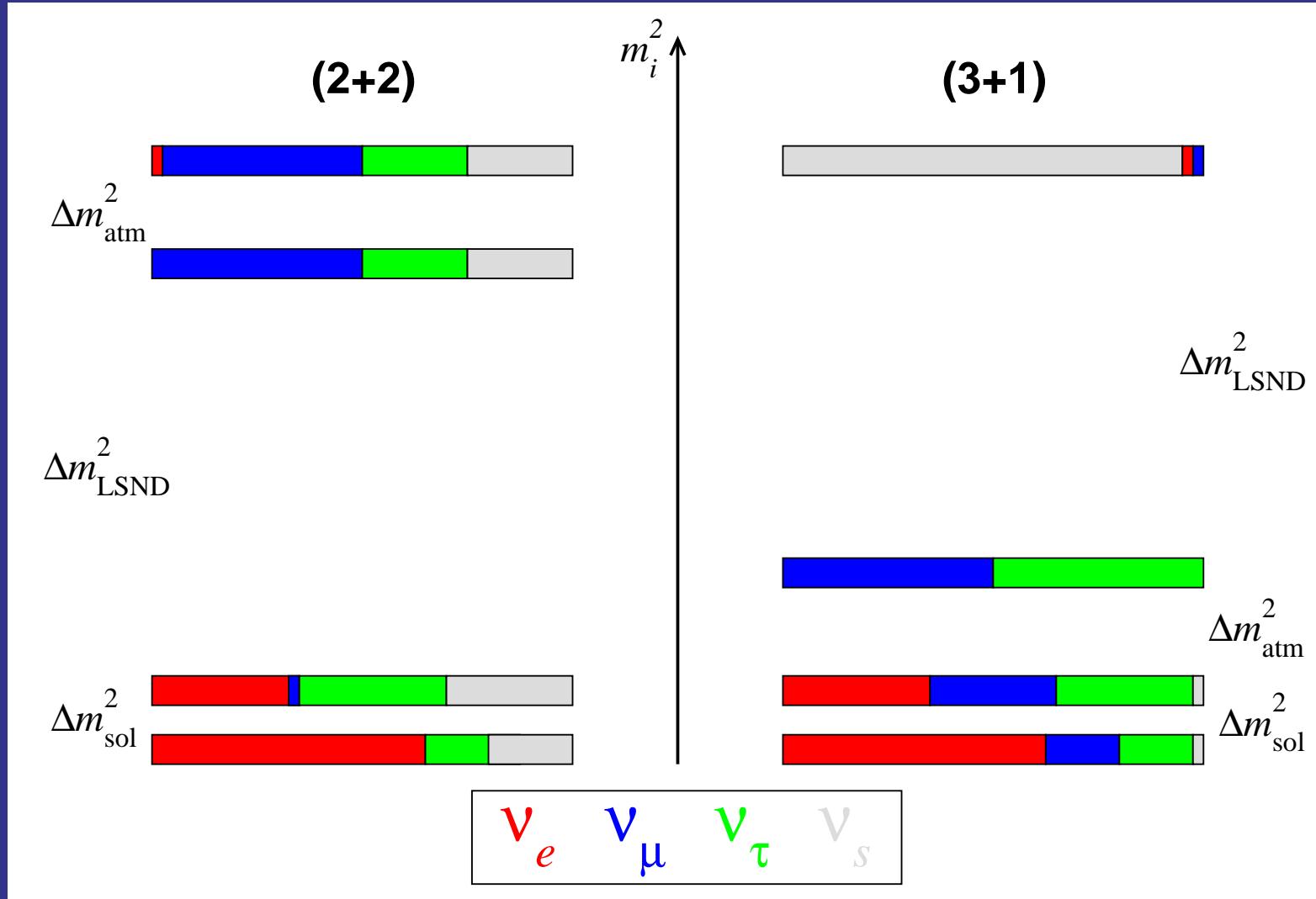
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→ MiniBooNE

results: 2005/2006?



# *Adding a sterile neutrino*



# *Four-neutrino oscillation data*

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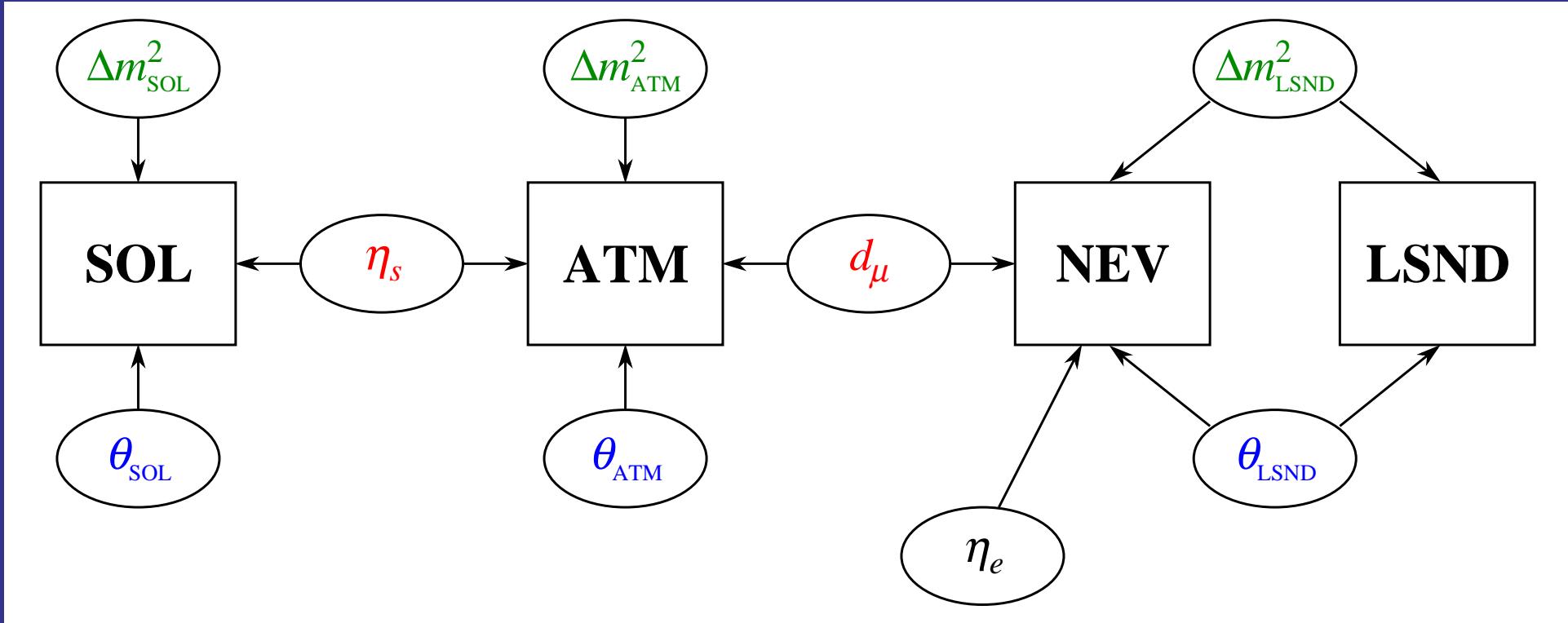
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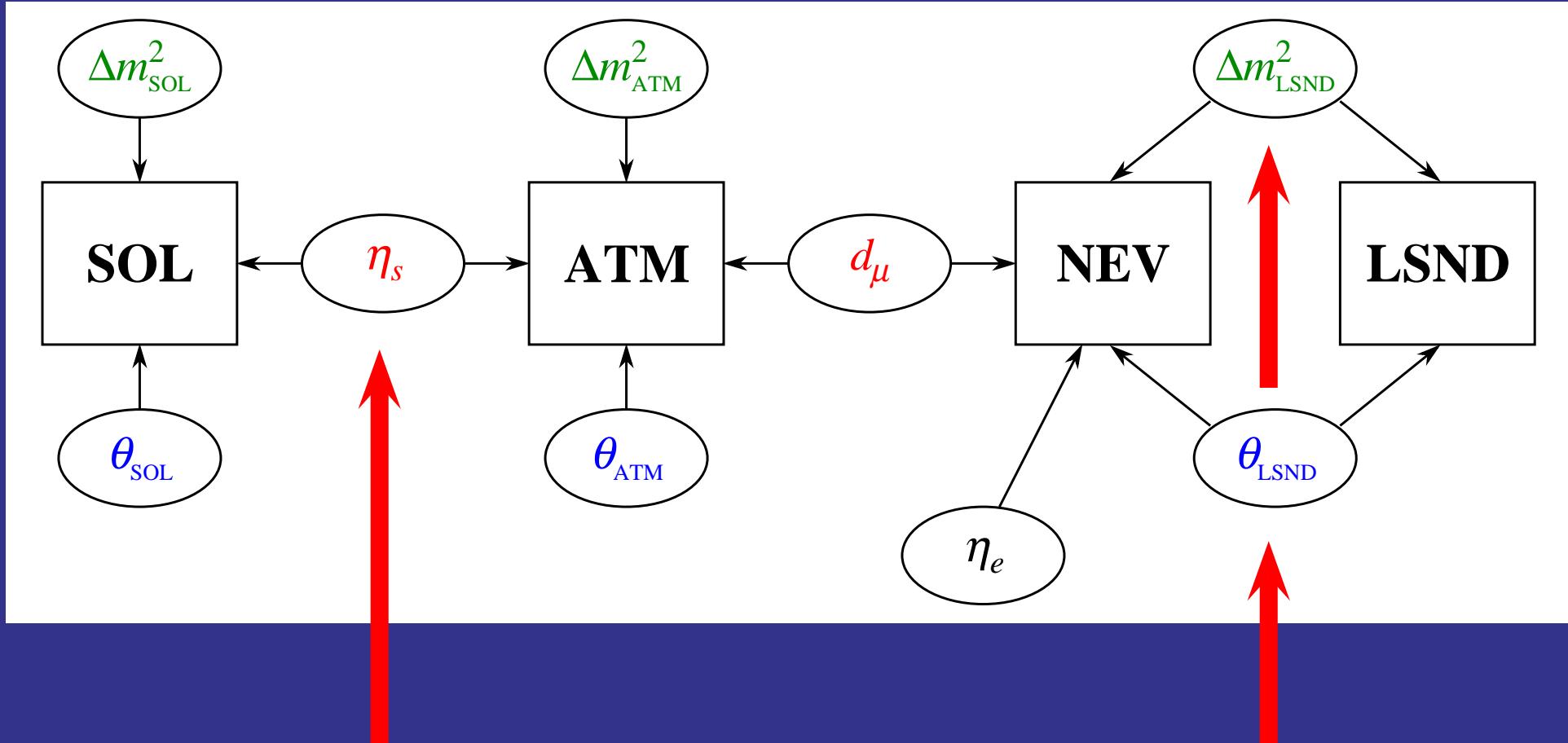
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- solar+KamLAND data
- atmospheric+K2K data
- LSND
- no-evidence short-baseline data (NEV)  
**(KARMEN, Bugey, CDHS)**  
provide strong constraints on neutrino mixing  
in the  $\sim 1 \text{ eV}^2$  range

# Coupling of the data sets



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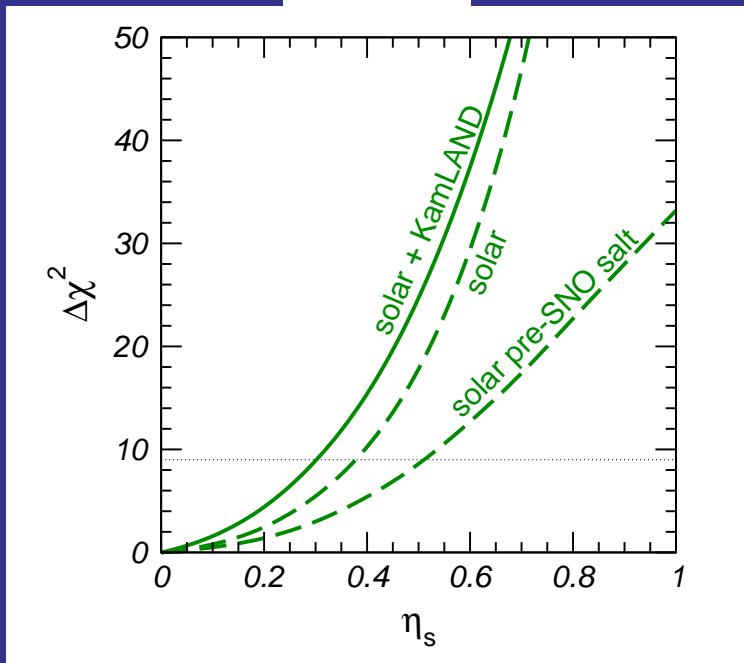
important for (2+2)

important for (3+1)

# *Global 4-neutrino analysis*

Maltoni, Schwetz, Tortola, Valle, hep-ph/0207157, hep-ph/0405172

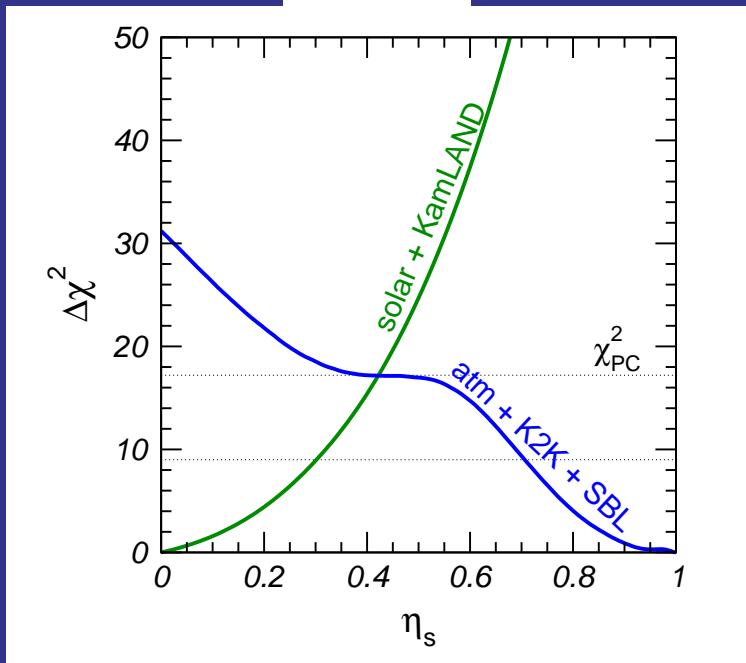
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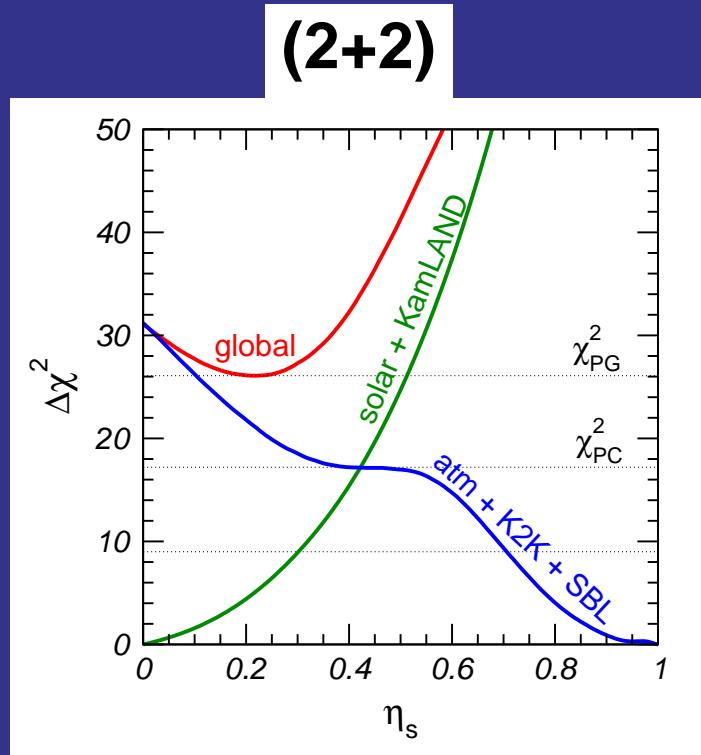
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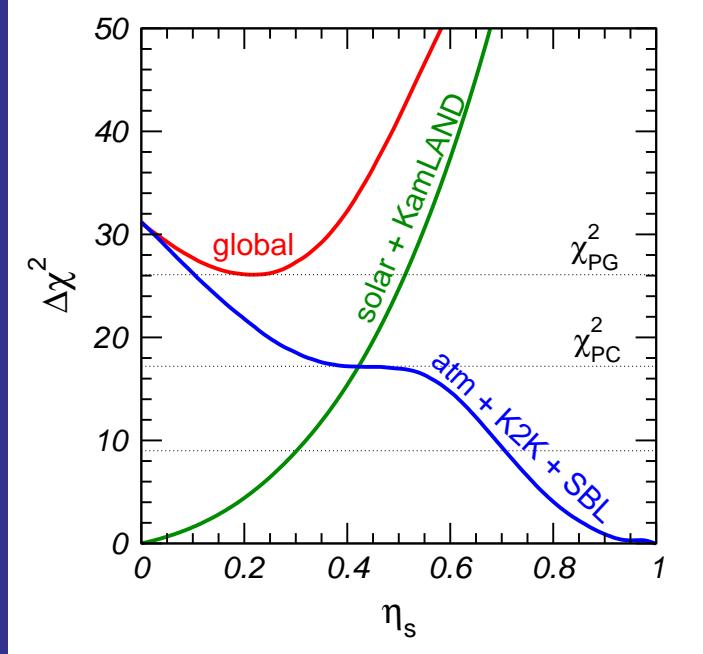
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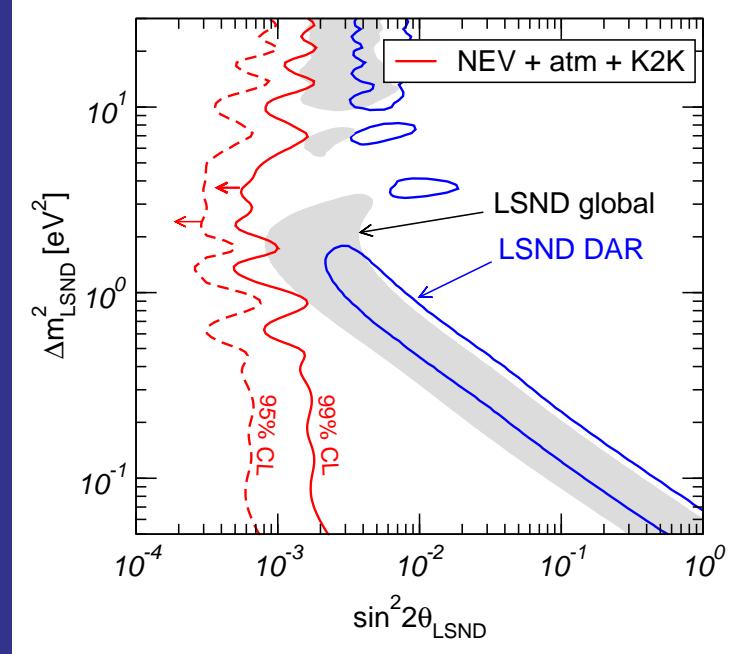
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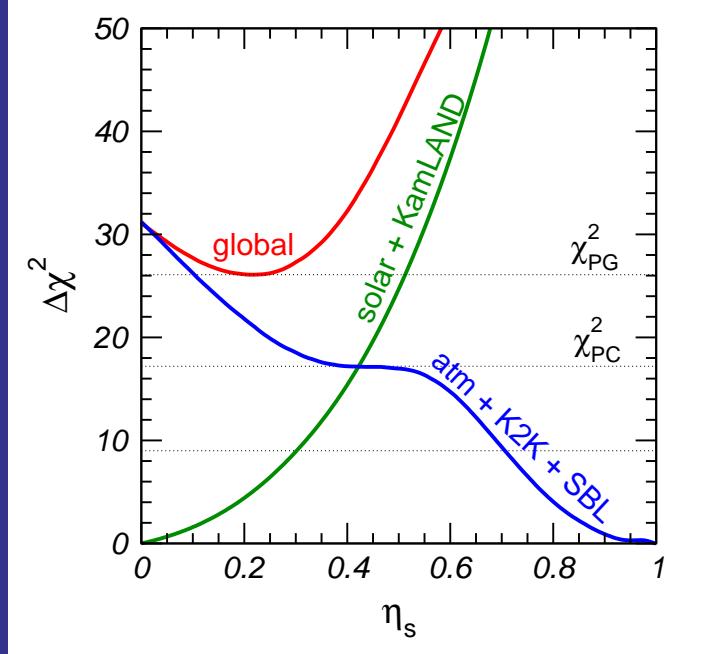
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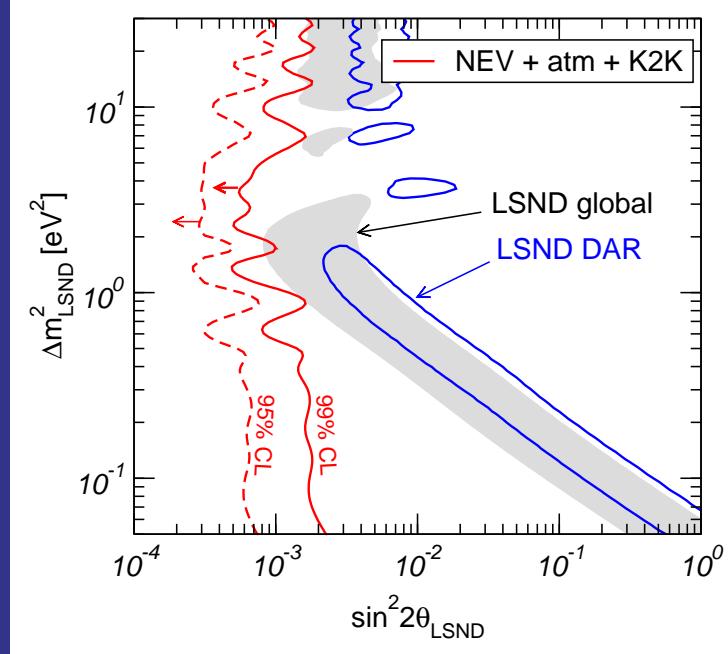
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**(2+2)**



**(3+1)**



	SOL	ATM	LSND	NEV	$\chi^2_{\text{PG}}$	parameter GOF (PG)	
<b>(3+1)</b>	0.0	0.4	5.7	10.9	17.0	$1.9 \times 10^{-3}$	$3.1\sigma$
<b>(2+2)</b>	5.3	20.8	0.6	7.3	33.9	$7.8 \times 10^{-7}$	$4.9\sigma$

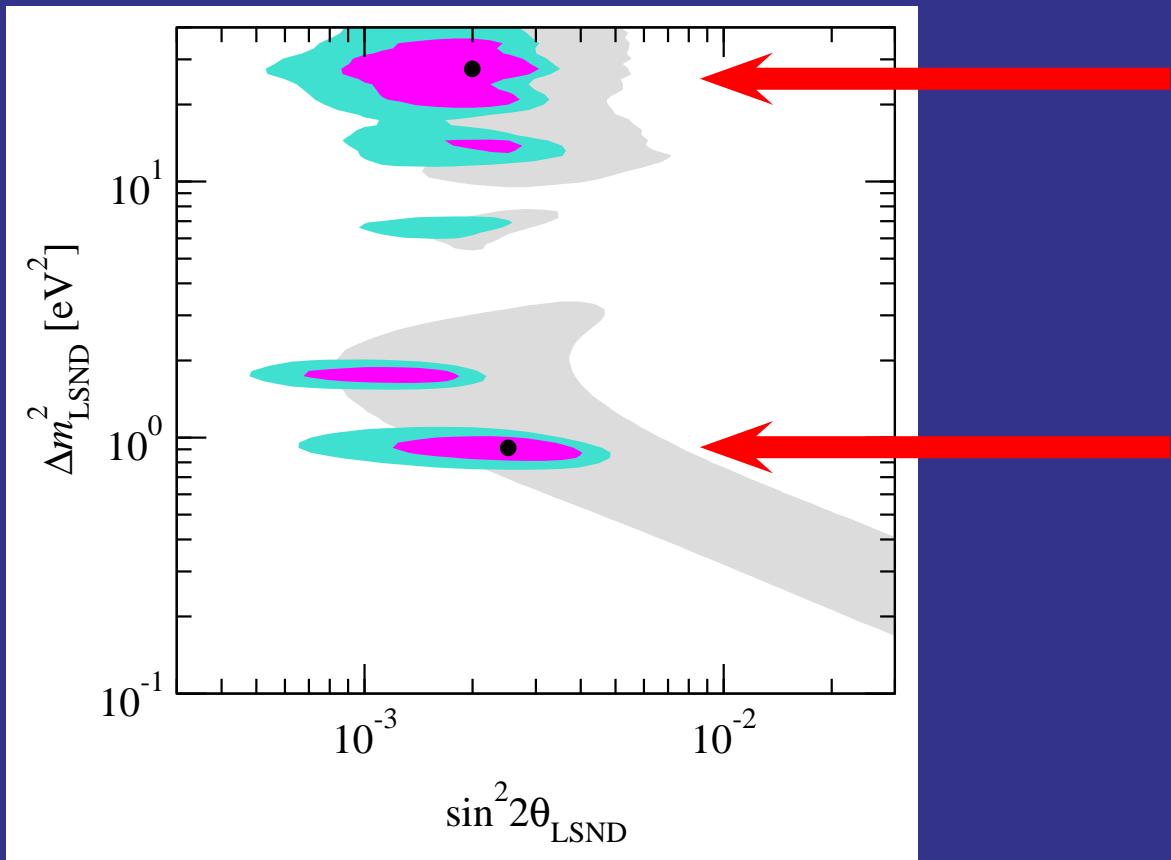
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$$\Delta m_{41}^2 \sim 20 \text{ eV}^2$$

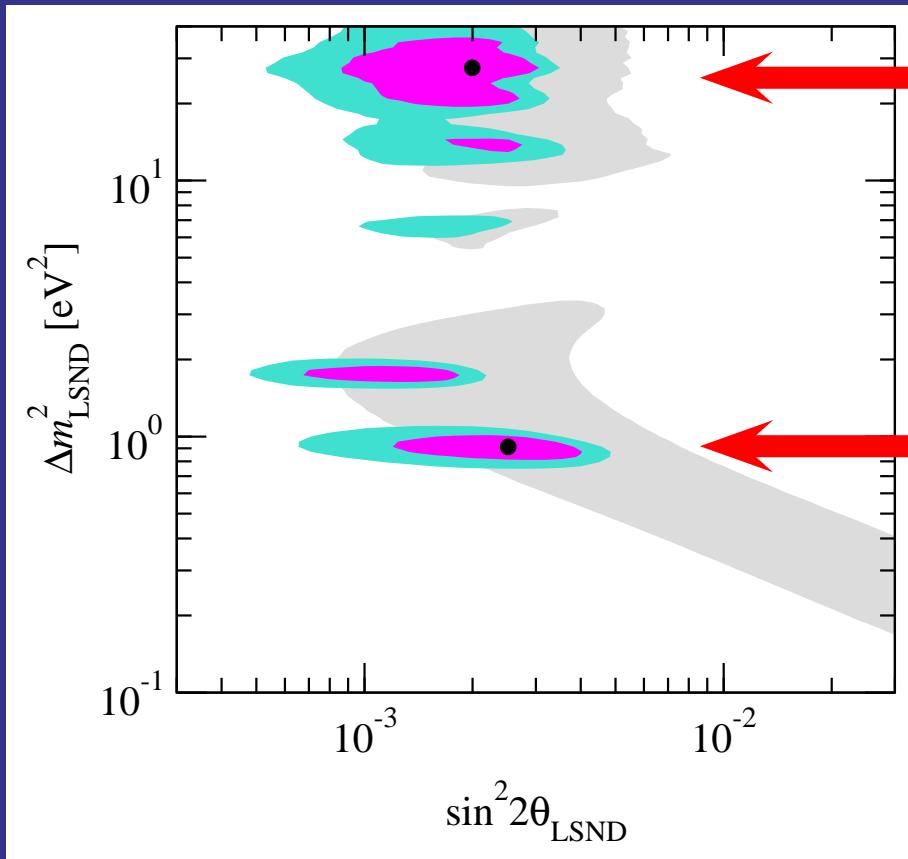
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$$\text{PG}_{(3+2)} = 2.1\%$$

$$\text{PG}_{(3+1)} = 0.032\%$$

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cosmology?

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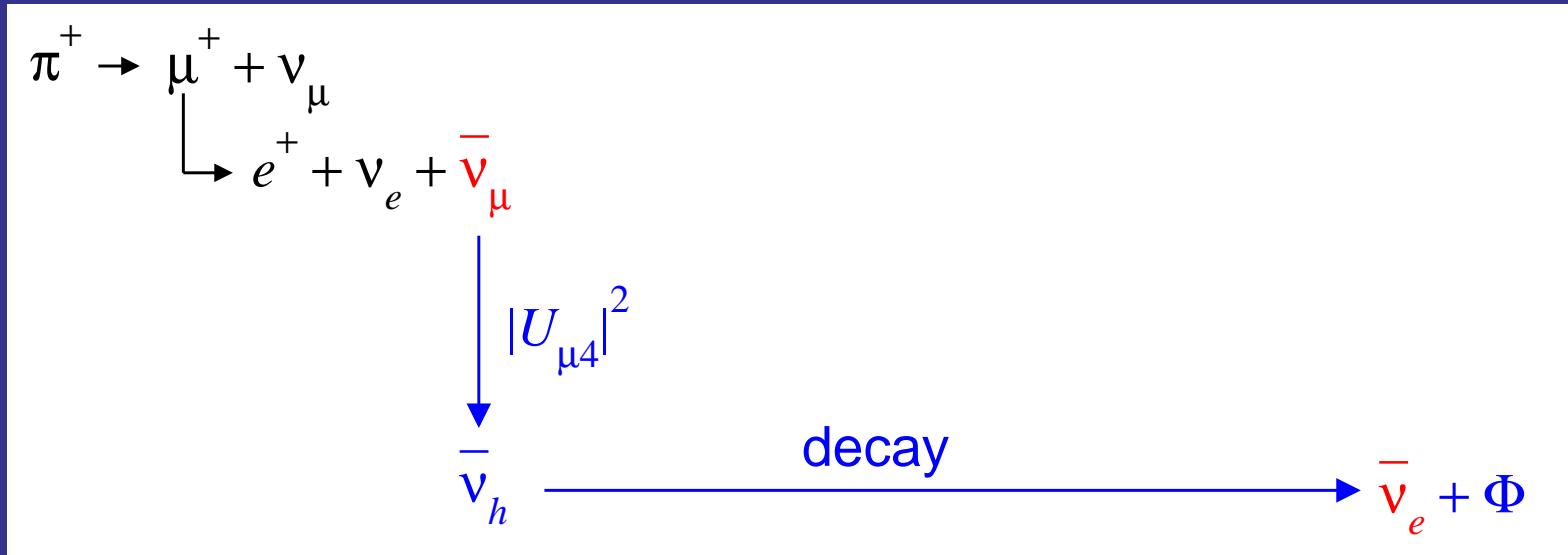
# *LSND and a decaying sterile neutrino*

oscillation interpretation



# *LSND and a decaying sterile neutrino*

Palomares-Riu, Pascoli, Schwetz, hep-ph/0505216



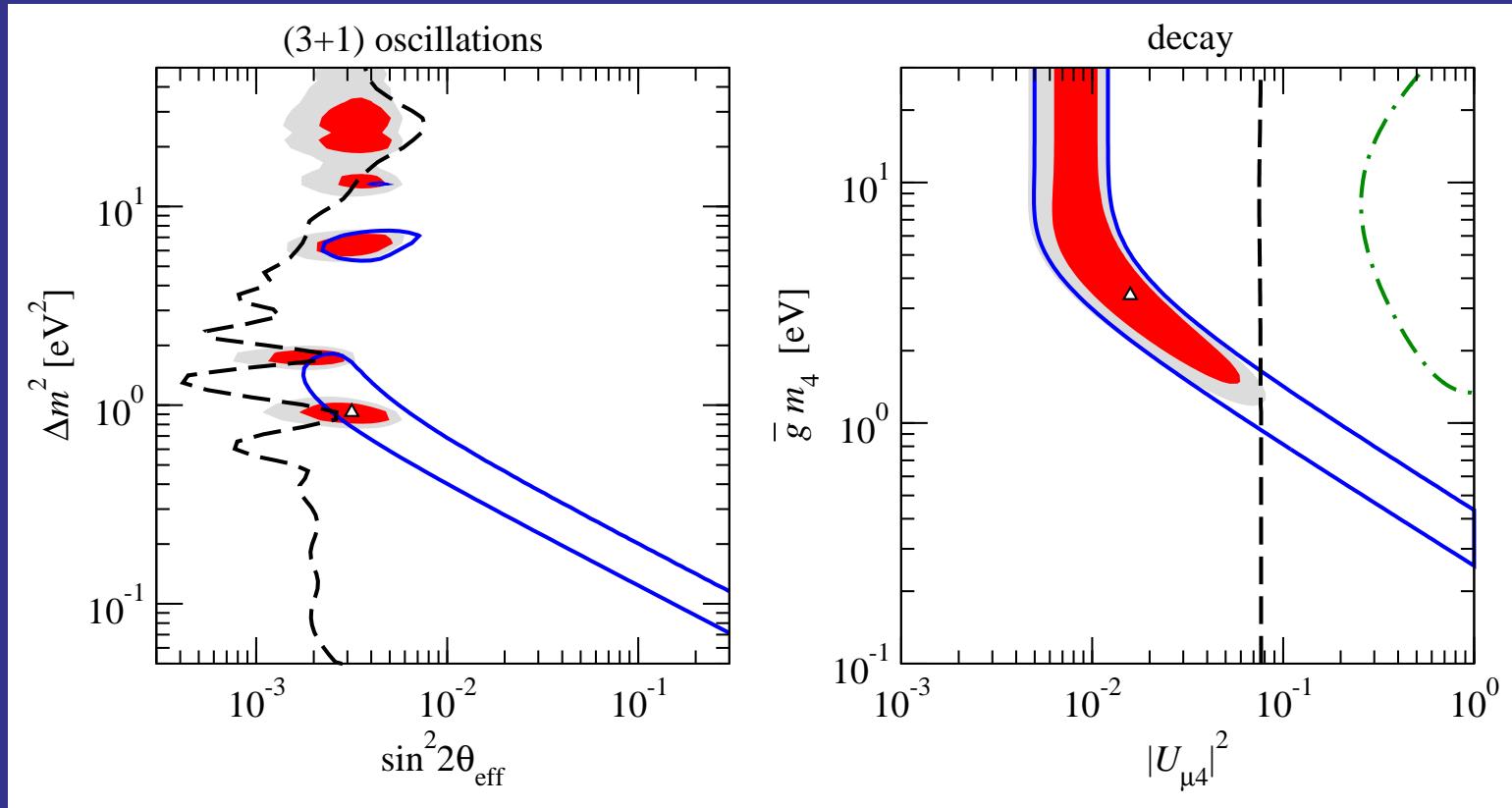
postulate decay of heavy neutrino  $\nu_h$  into  $\nu_l$  and a scalar  $\Phi$

$$\mathcal{L} = -g \bar{\nu}_{lL} \nu_{hR} \Phi + \text{h.c.}$$

need  $g m_h \sim \text{eV}$  and  $|U_{\mu 4}|^2 \sim 10^{-2}$  (e.g.,  $g \sim 10^{-6} - 10^{-3}$ ,  $m_h \sim \text{keV} - \text{MeV}$ )

# *LSND and a decaying sterile neutrino*

Palomares-Riu, Pascoli, Schwetz, hep-ph/0505216



$$\text{PG}_{(3+1)} = 0.002\%, \text{ PG}_{(3+2)} = 2.1\%$$

$$\text{PG}_{\text{decay}} = 4.6\%$$

---

for the rest of the talk I assume that

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→ **Standard three-neutrino oscillation framework**

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- Increase the precision on solar and atmospheric parameters (e.g. Is  $\theta_{23}$  exactly  $45^\circ$ ?)
- How small is  $\theta_{13}$ ?
- What is the value of the CP phase  $\delta$ ?

# *3-flavour oscillation*

---

## Open questions:

- Increase the precision on solar and atmospheric parameters (e.g. Is  $\theta_{23}$  exactly  $45^\circ$ ?)
- How small is  $\theta_{13}$ ?
- What is the value of the CP phase  $\delta$ ?
- Type of the neutrino mass ordering (sign of  $\Delta m_{31}^2$ )

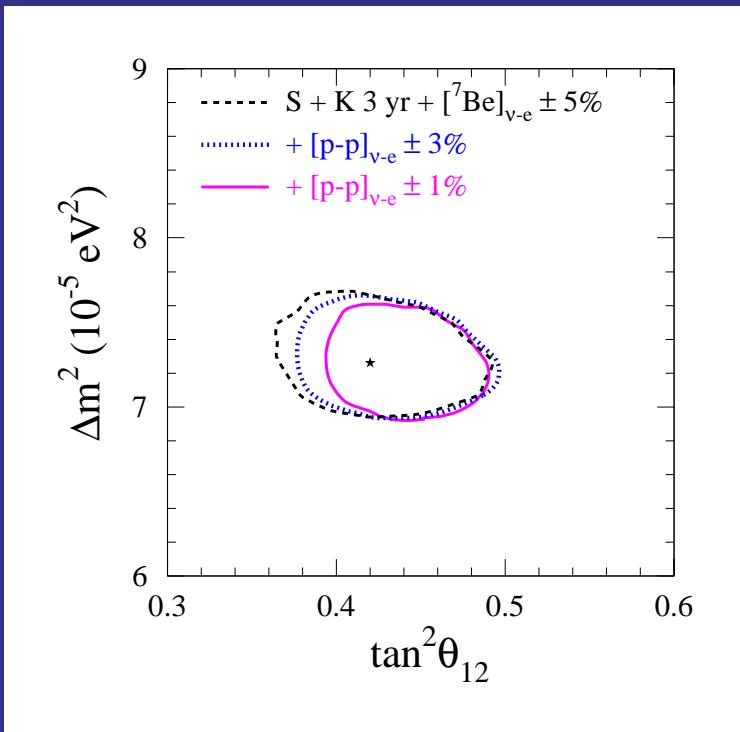
---

## Improving on the ‘solar’ parameters

$\theta_{12}$  **and**  $\Delta m_{21}^2$

# *Low energy solar neutrino experiments*

J.N. Bahcall, Pena-Garay, hep-ph/0305159



- Solar neutrino data 2003
- 3 years simulated KamLAND data
- 5% measurement ( $1\sigma$ ) of the  ${}^7\text{Be}$  flux
- 3% and 1% measurement ( $1\sigma$ ) of the  $pp$  flux

see also S. Choubey, S.T. Petcov, hep-ph/0410283

# *Long-baseline reactor neutrino experiment*

---

S. Choubey, S.T. Petcov, hep-ph/0404103

99% CL Data set	range $\Delta m_{21}^2 / 10^{-5} \text{eV}^2$	spread $\Delta m_{21}^2$	range $\sin^2 \theta_{12}$	spread $\sin^2 \theta_{12}$
only solar	3.2 – 14.9	65%	0.22 – 0.37	25%
solar+1 kTy KL	6.5 – 8.0	10%	0.23 – 0.37	23%
solar+2.6 kTy KL	6.7 – 7.7	7%	0.23 – 0.36	22%

---

$$\text{spread}(x) = \frac{x^{\text{upper}} - x^{\text{lower}}}{x^{\text{upper}} + x^{\text{lower}}}$$

# *Long-baseline reactor neutrino experiment*

S. Choubey, S.T. Petcov, hep-ph/0404103

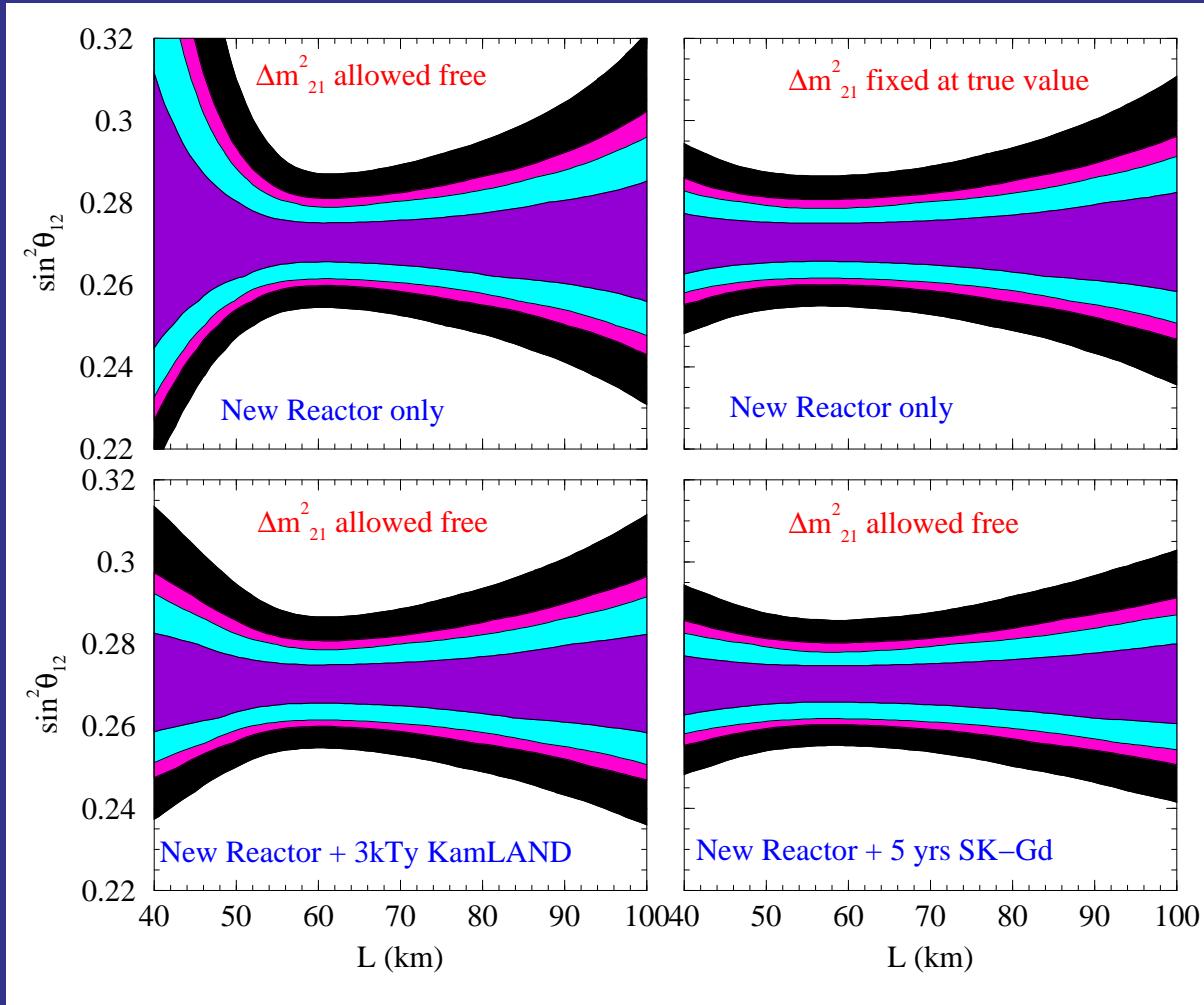
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solar+2.6 kTy KL	6.7 – 7.7	7%	0.23 – 0.36	22%
3 yrs SK-Gd	7.0 – 7.4	3%	0.25 – 0.37	19%
5 yrs SK-Gd	7.0 – 7.3	2%	0.26 – 0.35	15%

J.F. Beacom, M.R. Vagins, hep-ph/0309300

SK doped with 0.2% Gadolinium (**GADZOOKS!**)  
tag neutrons from the reaction  $\bar{\nu}_e + p \rightarrow e^+ + n$

# *Long-baseline reactor neutrino experiment*

%-level determination of  $\theta_{12}$ : dedicated reactor exp. at  $\sim 60$  km



S. Choubey, S.T. Petcov,  
hep-ph/0410283

73 GW kt yr  
2% syst. uncert.

$\rightarrow \sin^2 \theta_{12}$  with  
2% (6%) at  $1\sigma$  ( $3\sigma$ )

see also J. Bouchiat, hep-ph/0304253; Minakata et al., hep-ph/0407326

---

## Improving on the ‘atmospheric’ parameters

$\theta_{23}$  **and**  $|\Delta m_{31}^2|$

# *Atmospheric parameters $|\Delta m_{13}^2|$ and $\theta_{23}$*

---

$\nu_\mu$ -disappearance in LBL accelerator experiments

# *Atmospheric parameters $|\Delta m_{13}^2|$ and $\theta_{23}$*

---

$\nu_\mu$ -disappearance in LBL accelerator experiments

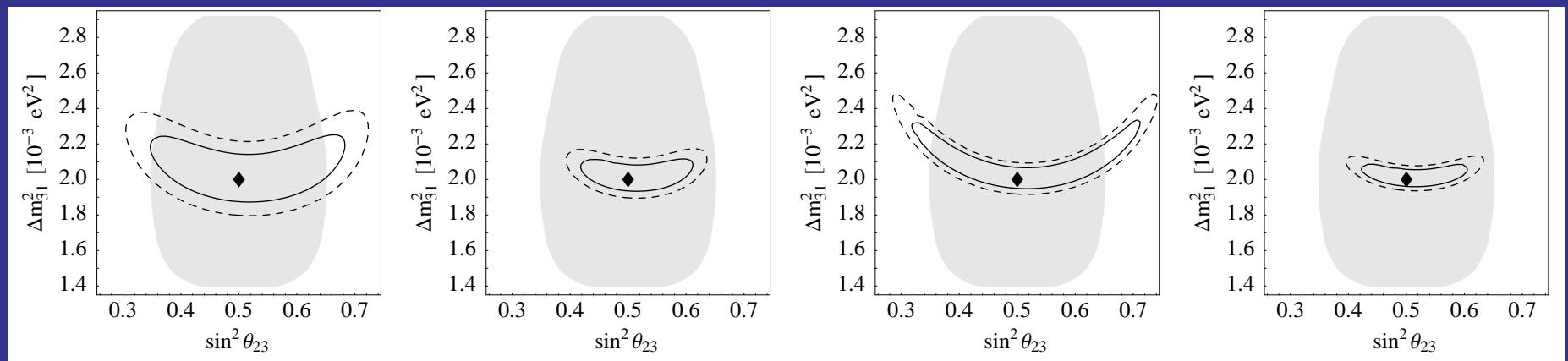
upcoming experiments:

- conventional beam experiments  
**MINOS, CNGS**
- superbeam experiments  
**T2K, NO $\nu$ A**

assume 5 yrs of running in neutrino mode

# *Atmospheric parameters $|\Delta m_{13}^2|$ and $\theta_{23}$*

**MINOS+CNGS**      **T2K**      **NO $\nu$ A**      **combined**



Huber, Lindner, Rolinec, Schwetz, Winter, hep-ph/0403068

# *Atmospheric parameters $|\Delta m_{13}^2|$ and $\theta_{23}$*

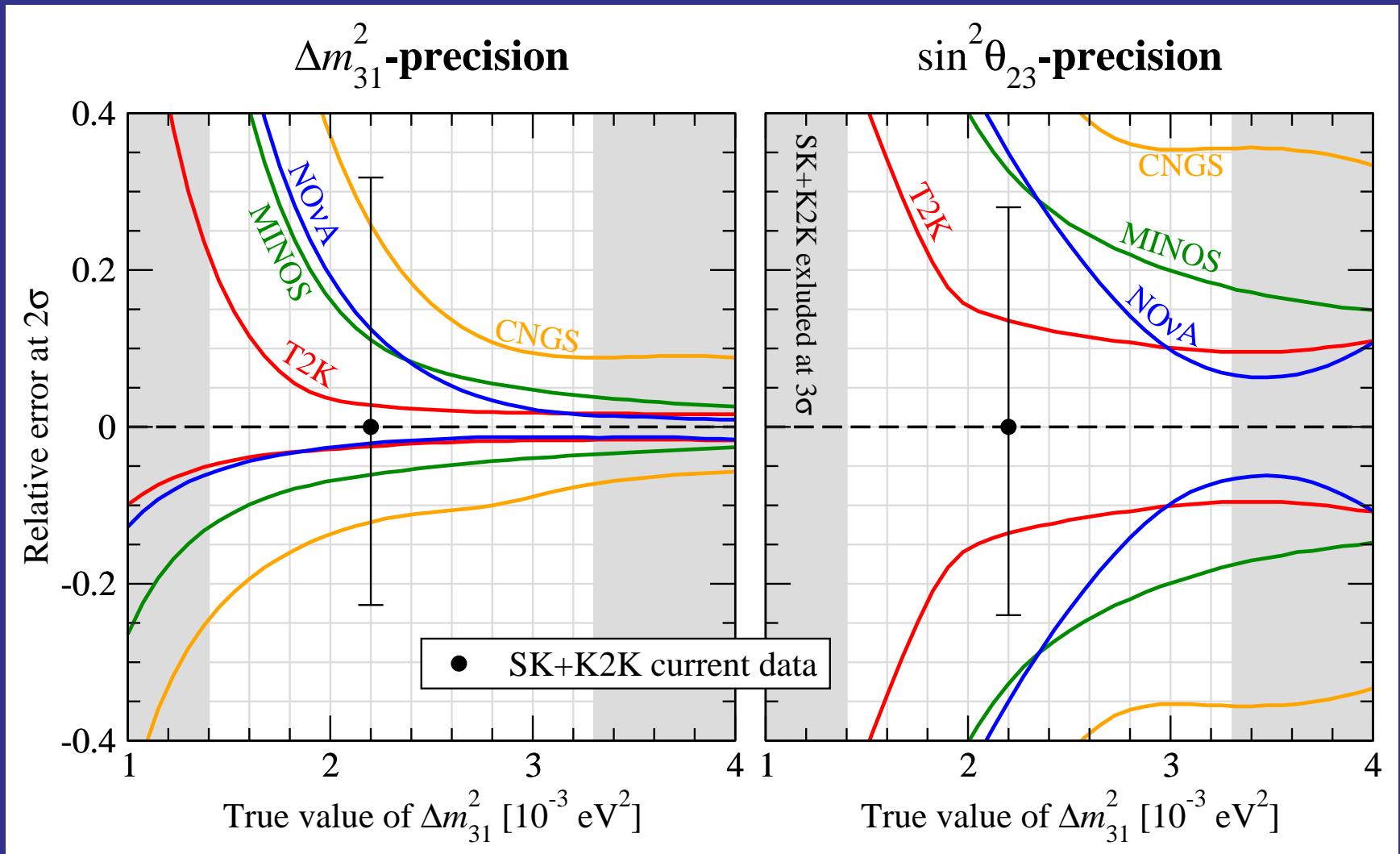
---

precision at  $3\sigma \equiv \frac{\text{upper}^{(3\sigma)} - \text{lower}^{(3\sigma)}}{\text{true value}}$

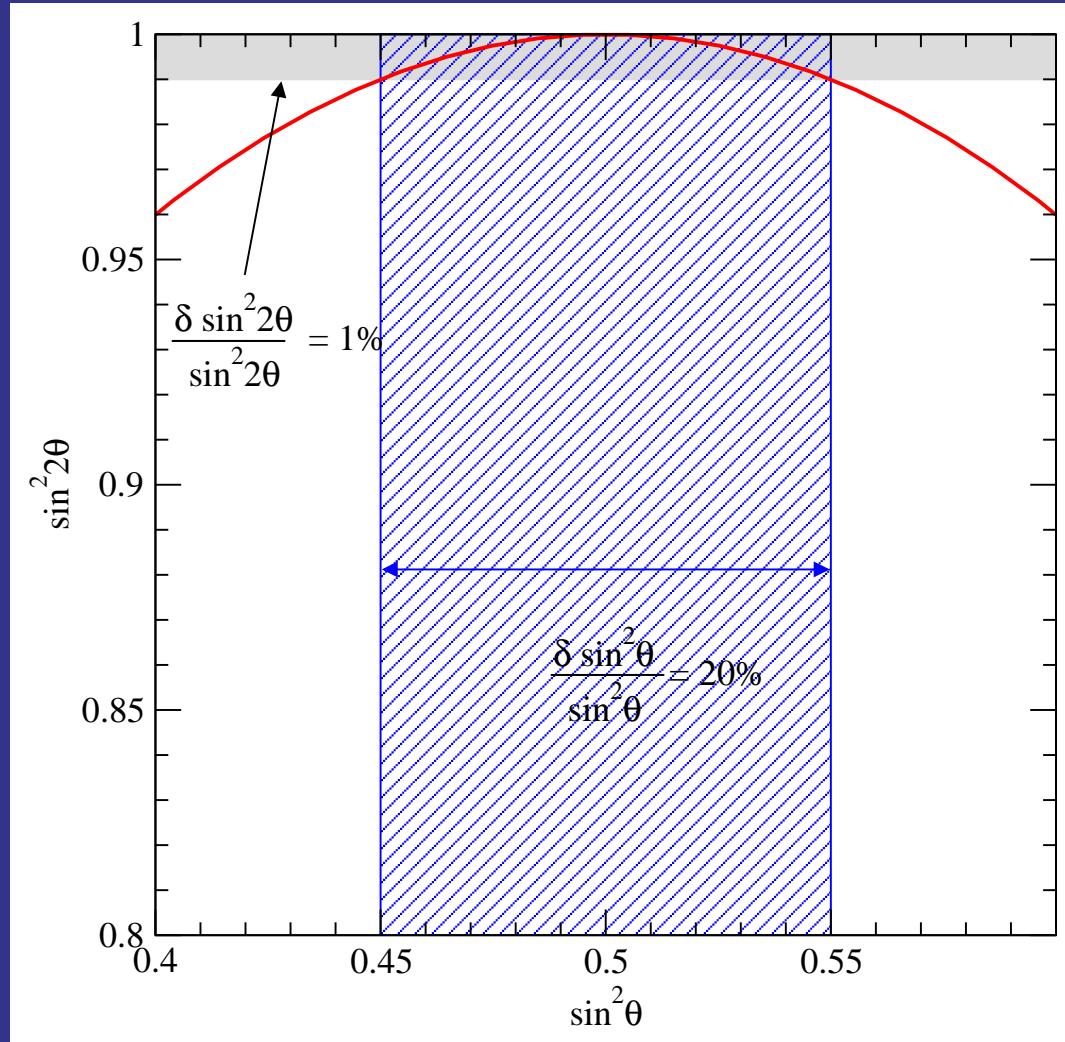
for true values  $|\Delta m_{31}^2| = 2 \cdot 10^{-3} \text{ eV}^2$  and  $\sin^2 \theta_{23} = 0.5$ :

	$ \Delta m_{31}^2 $	$\sin^2 \theta_{23}$
current	86%	68%
<b>MINOS+CNGS</b>	26%	78%
<b>T2K</b>	12%	46%
<b>NO<math>\nu</math>A</b>	25%	86%
Combination	9%	42%

# Atmospheric parameters $|\Delta m_{13}^2|$ and $\theta_{23}$



# *Atmospheric parameters $|\Delta m_{13}^2|$ and $\theta_{23}$*



H. Minakata, M. Sonoyama and H. Sugiyama, hep-ph/0406073

# *Atmospheric parameters $|\Delta m_{13}^2|$ and $\theta_{23}$*

---

subsequent generation of LBL experiments like

**T2HK**, CERN-Frejus exps (**SPL**, **BB**), **NuFact**

will provide a  
sub-percent determination of  $|\Delta m^2|$  and  $\sin^2 2\theta_{23}$ !

---

**What is the value of  $\theta_{13}$ ?**

---

## What is the value of $\theta_{13}$ ?

- naively one would expect  $\theta_{12} \sim \theta_{23} \sim \theta_{13}$   
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---

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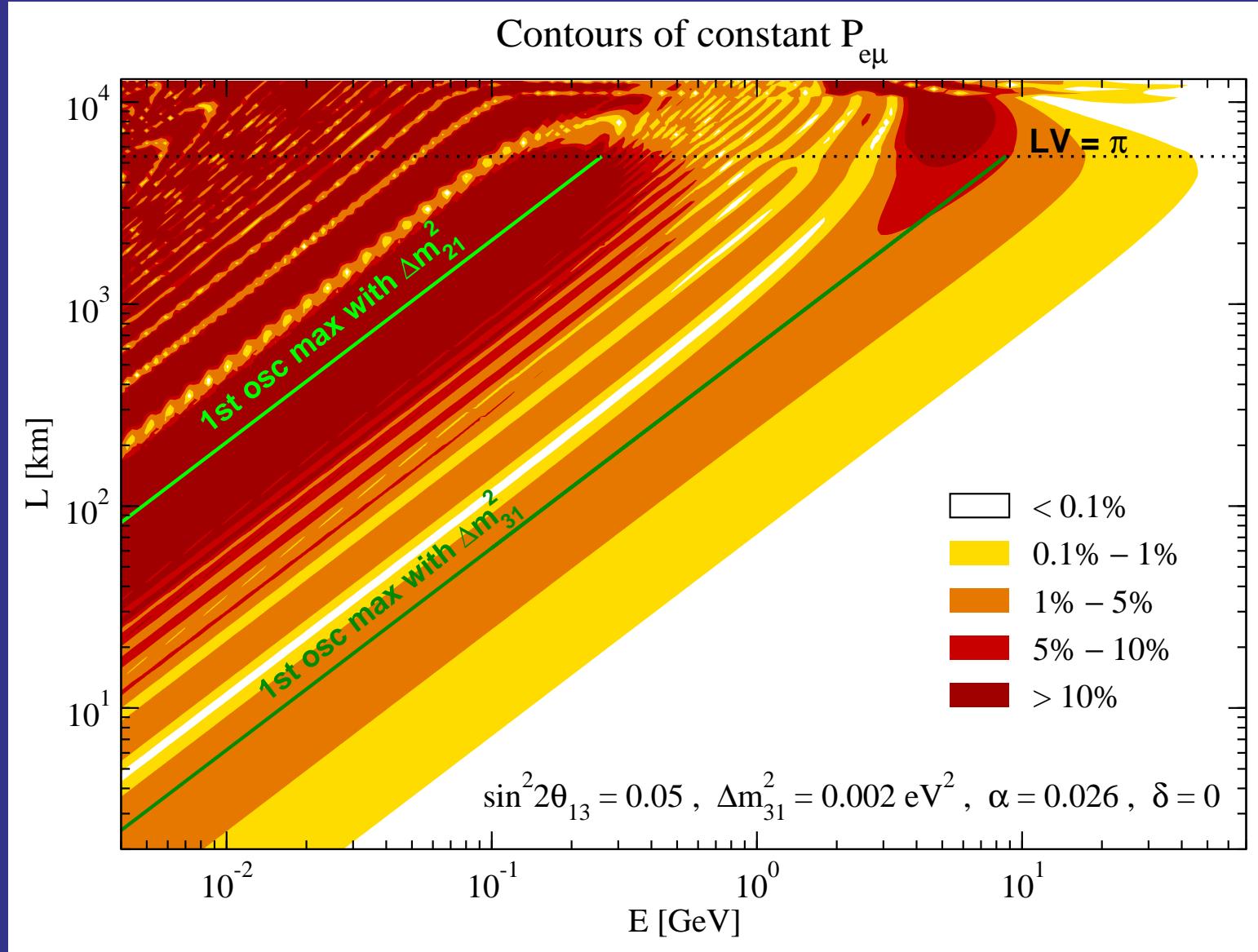
- naively one would expect  $\theta_{12} \sim \theta_{23} \sim \theta_{13}$   
→  $\theta_{13}$  around the corner
- $\theta_{13} \ll 1$  hint for some symmetry
- relatively large  $\theta_{13}$  opens the possibility to observe generic 3-flavour effects (CP-violation)

# *Measuring $\theta_{13}$*

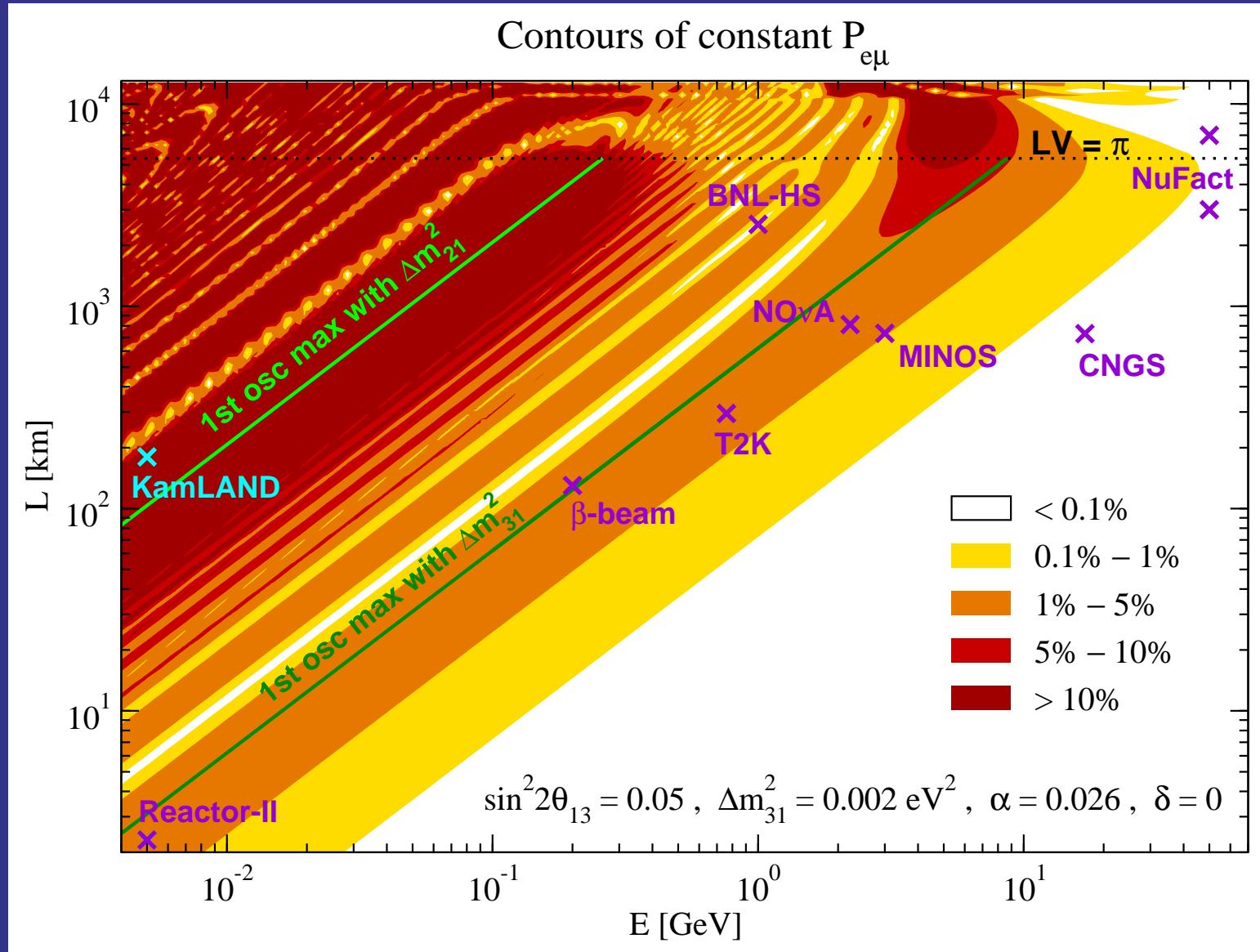
---

- reactor experiments with near and far detectors  
**D-Chooz, KASKA, Daya Bay, Angra, Braidwood, RENO**
- LBL  $\nu_\mu \rightarrow \nu_e$  appearance experiments  
**MINOS, CNGS, T2K, NO $\nu$ A, T2HK, SPL, BB, NuFact**

# Measuring $\theta_{13}$



# Measuring $\theta_{13}$



# *Measuring $\theta_{13}$ by $\nu_\mu \rightarrow \nu_e$ at beams*

---

The measurement of  $\theta_{13}$  with the  $\nu_\mu \rightarrow \nu_e$  appearance channel suffers from **correlations** and **degeneracies**:

G.L. Fogli, E. Lisi, Phys. Rev. D54 (1996) 3667

J. Burguet-Castell et al., Nucl. Phys. B608 (2001) 301

H. Minakata, H. Nunokawa, JHEP 10 (2001) 001

V.Barger, D.Marfatia, K.Whisnant, Phys. Rev. D65 (2002) 073023; D66 (2002) 053007

P.Huber, M.Lindner, W.Winter, Nucl. Phys. B645 (2002) 3; Nucl. Phys. B654 (2003) 3

and many more

Not  $\sin^2 2\theta_{13}$ , but only a specific **parameter combination** is measured very accurately

# *The $\nu_\mu \rightarrow \nu_e$ oscillation probability in vacuum*

---

$$\begin{aligned} P_{\mu e} \simeq & \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \Delta_{31} \\ & \mp \alpha \sin 2\theta_{12} \sin 2\theta_{13} \sin \delta \cos \theta_{13} \sin 2\theta_{23} \sin^3 \Delta_{31} \\ & - \alpha \sin 2\theta_{12} \sin 2\theta_{13} \cos \delta \cos \theta_{13} \sin 2\theta_{23} \cos \Delta_{31} \sin^2 \Delta_{31} \\ & + \alpha^2 \sin^2 2\theta_{12} \cos^2 \theta_{23} \sin^2 \Delta_{31}, \end{aligned}$$

with

$$\Delta_{31} \equiv \frac{\Delta m_{31}^2 L}{4E_\nu}, \quad \alpha \equiv \frac{\Delta m_{21}^2}{\Delta m_{31}^2} = 0.035^{+0.009}_{-0.004}$$

# *Measuring $\sin^2 2\theta_{13}$ at reactors*

---

“Clean” measurement of  $\sin^2 2\theta_{13}$ :

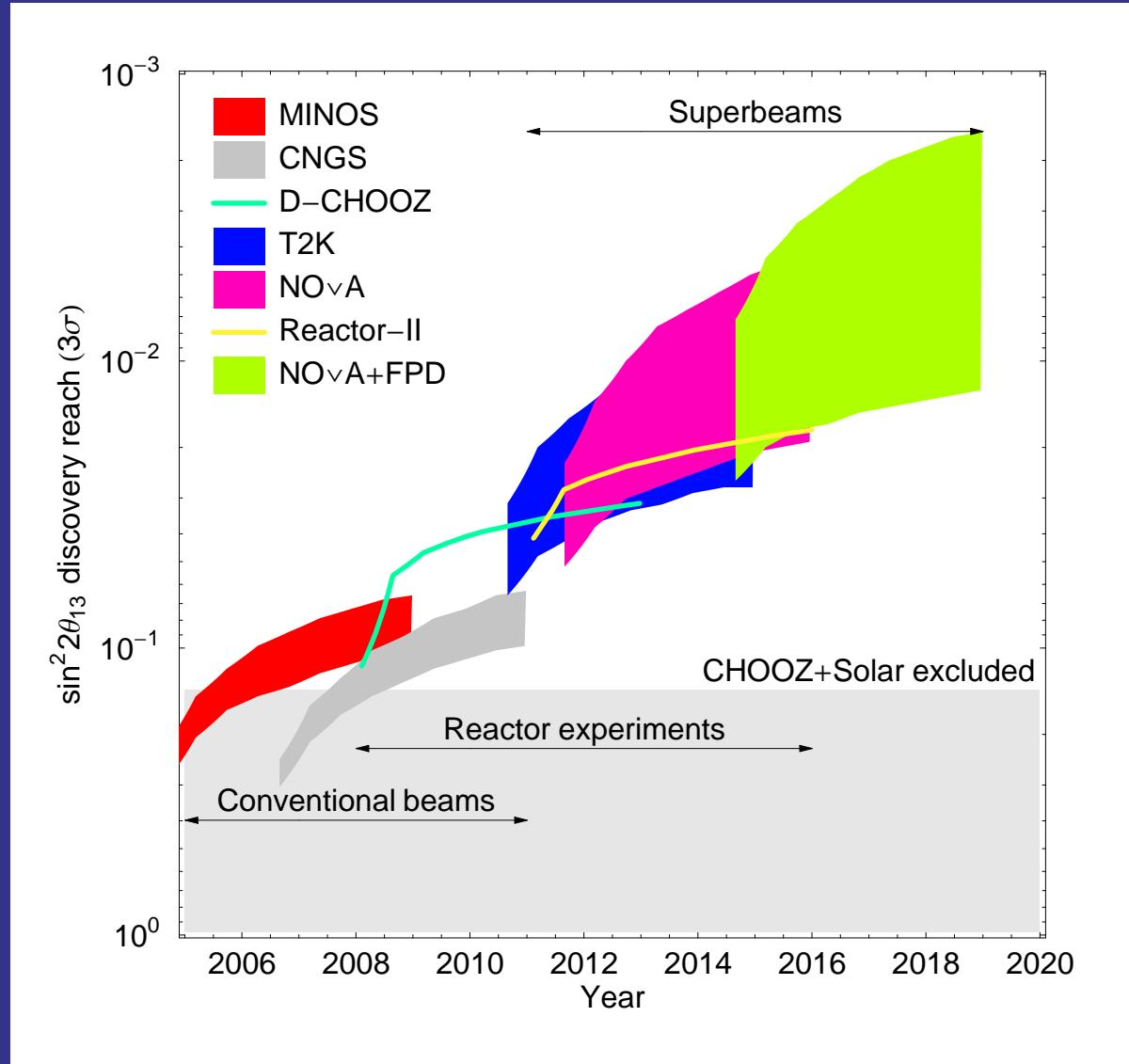
$$P_{ee} \approx 1 - \sin^2 2\theta_{13} \sin^2 \frac{\Delta m_{31}^2 L}{4E_\nu} + \left( \frac{\Delta m_{21}^2 L}{4E_\nu} \right)^2 \cos^4 \theta_{13} \sin^2 2\theta_{12}$$

last term negligible for  $\frac{\Delta m_{31}^2 L}{4E_\nu} \sim \pi/2$  and  $\sin^2 2\theta_{13} \gtrsim 10^{-3}$

determination of  $\theta_{13}$  is free of correlations and degeneracies

- P. Huber, M. Lindner, T. Schwetz and W. Winter, Nucl. Phys. B **665** (2003) 487 [hep-ph/0303232]  
H. Minakata, H. Sugiyama, O. Yasuda, K. Inoue and F. Suekane, Phys. Rev. D **68** (2003) 033017

# $\sin^2 2\theta_{13}$ discovery reach evolution

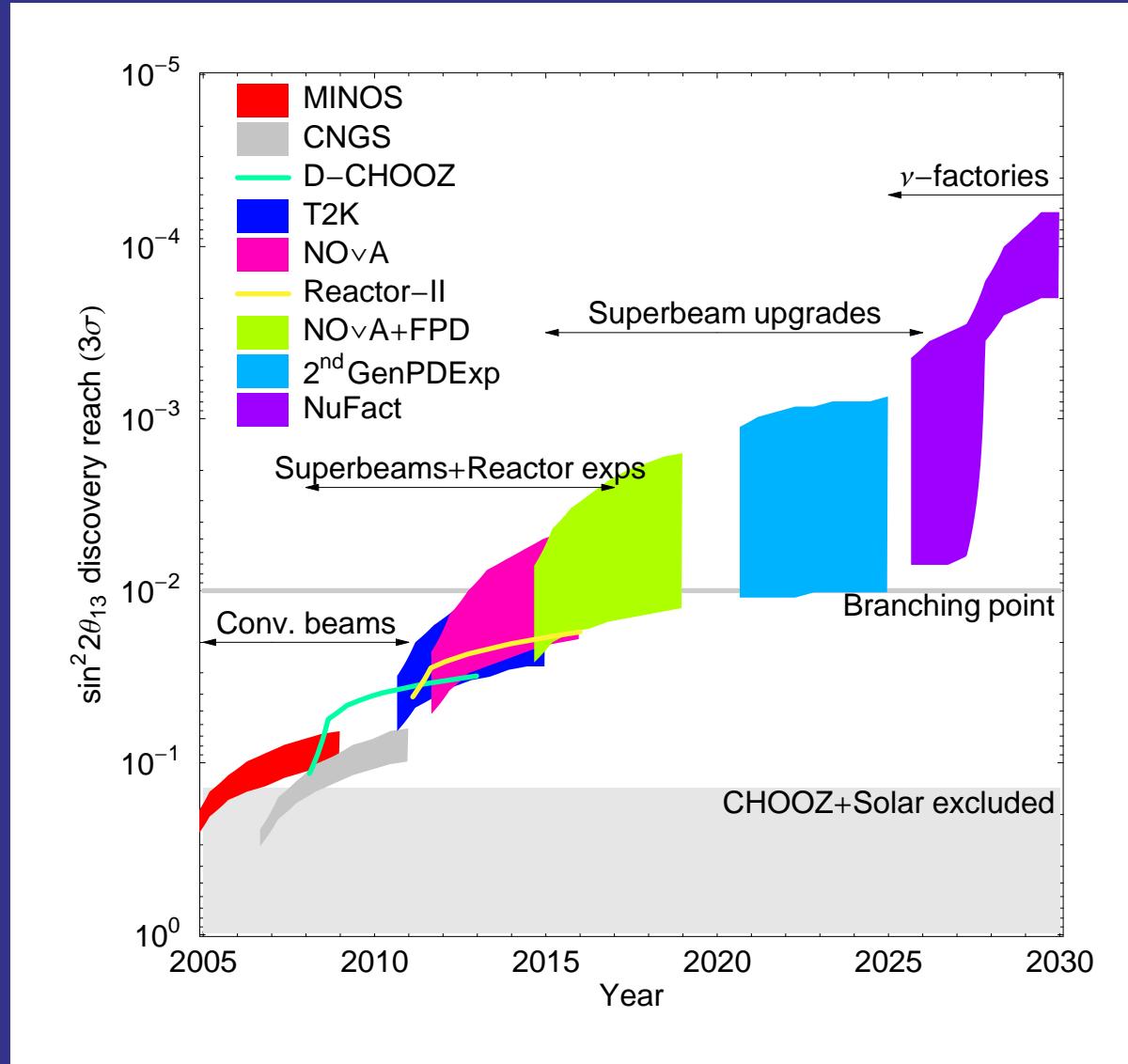


plot by W. Winter from  
Albrow et al., hep-ex/0509019

$$\Delta m_{31}^2 = +2.5 \times 10^{-3} \text{ eV}^2$$
$$\sin^2 2\theta_{23} = 1$$

FPD = Fermilab Proton Driver  
LBL exps.: neutrinos only

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2<sup>nd</sup> GenPDExp = T2HK  
NuFact anti-ν after 2.5 yr

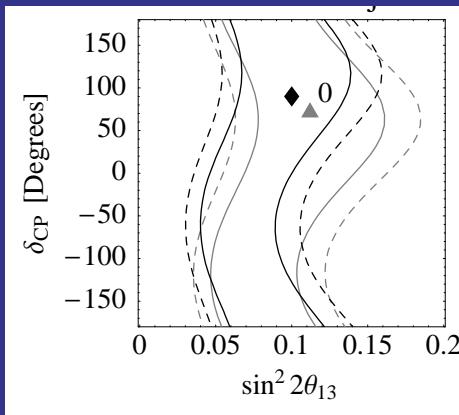
---

# The CP-phase $\delta$ and the type of the mass hierarchy

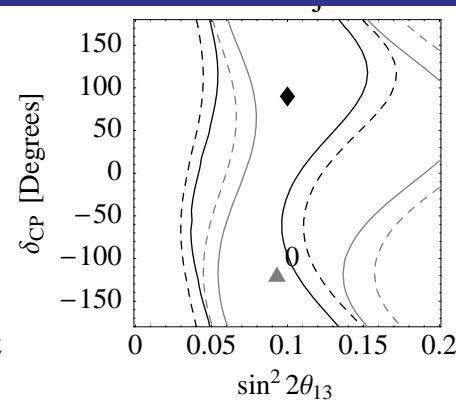
# *CP-phase and hierarchy within ten years*

assume  $\sin^2 2\theta_{13} = 0.1$

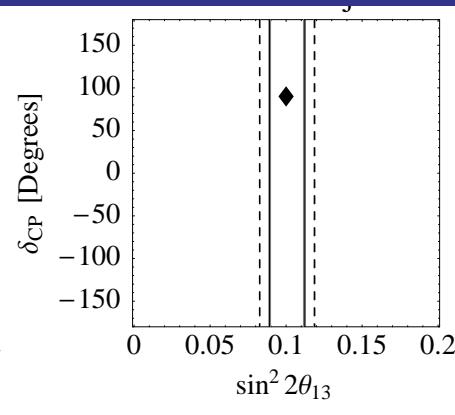
T2K



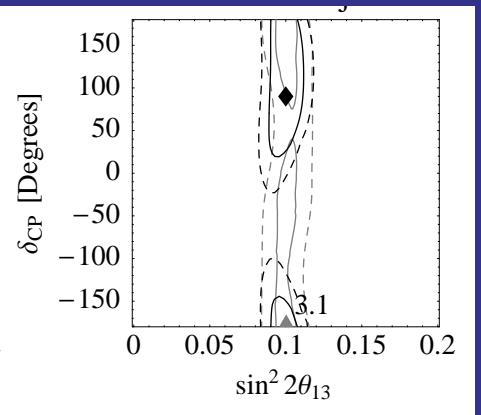
NO $\nu$ A



Reactor-II

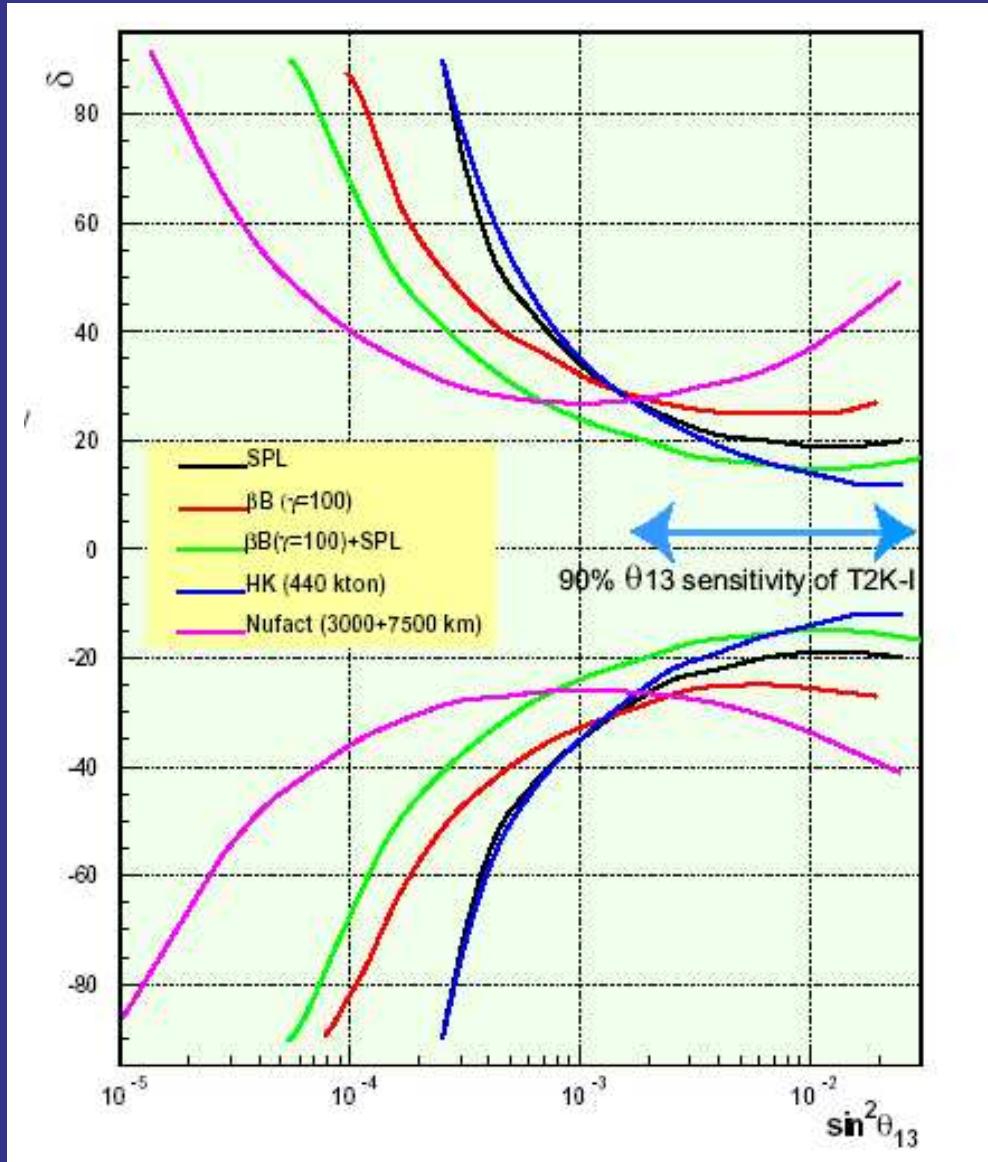


combined



Huber, Lindner, Rolinec, Schwetz, Winter, hep-ph/0403068

# Sensitivity to CP-violation at $3\sigma$



M.Mezzetto, talk at NuFact 2006

SPL:  $2\nu+8\bar{\nu}$  yr, 440 kton

$\beta B$ :  $5\nu+5\bar{\nu}$  yr, 440 kton

$\beta B + SPL$

T2HK:  $2\nu+8\bar{\nu}$  yr, 440 kton

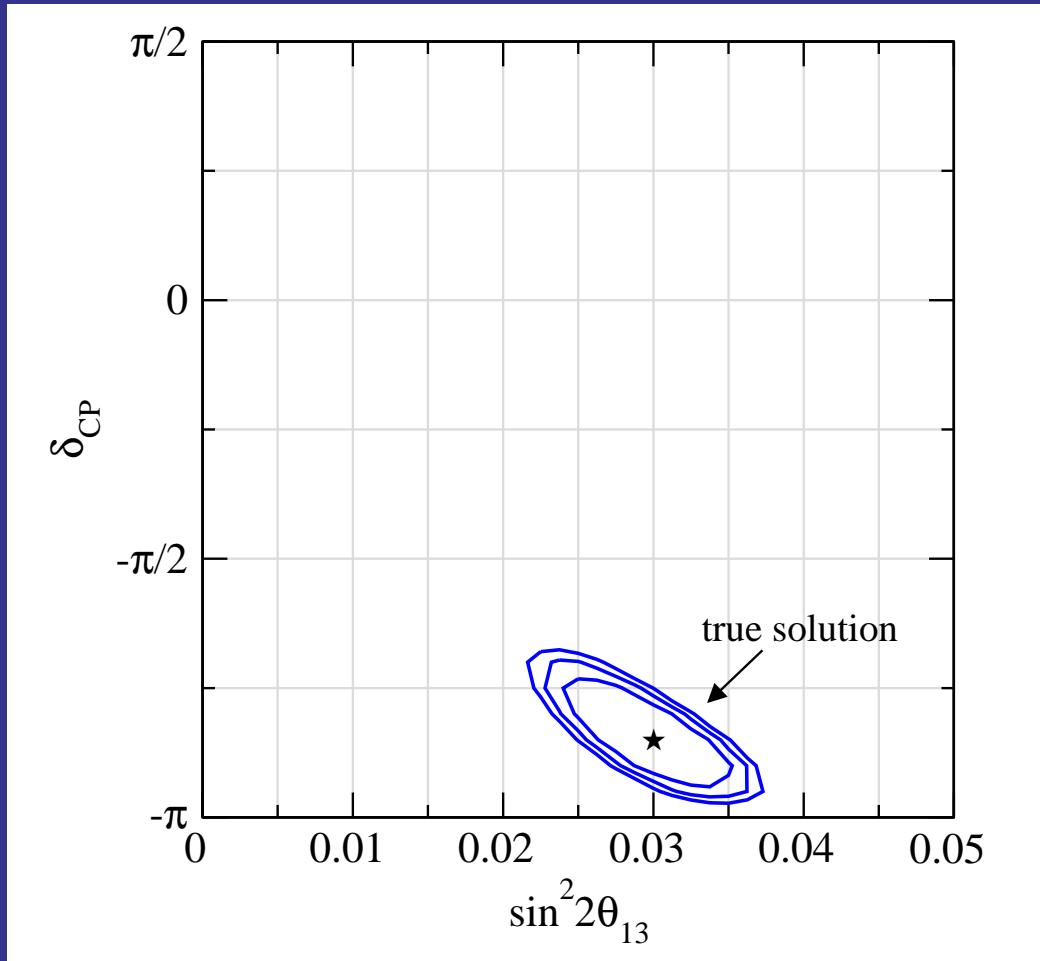
NuFact:  $5\nu+5\bar{\nu}$  yr,  $2 \times 50$  kton  
at 3500 and 7000 km

# *The problem of degeneracies*

---

Parameter degeneracies in LBL experiments provide a severe limitation for the determination of  $\theta_{13}$ , the CP phase  $\delta$  and the hierarchy!

# *Degeneracies and T2HK*



allowed regions at  
 $2\sigma$ , 99%,  $3\sigma$  CL

true values:

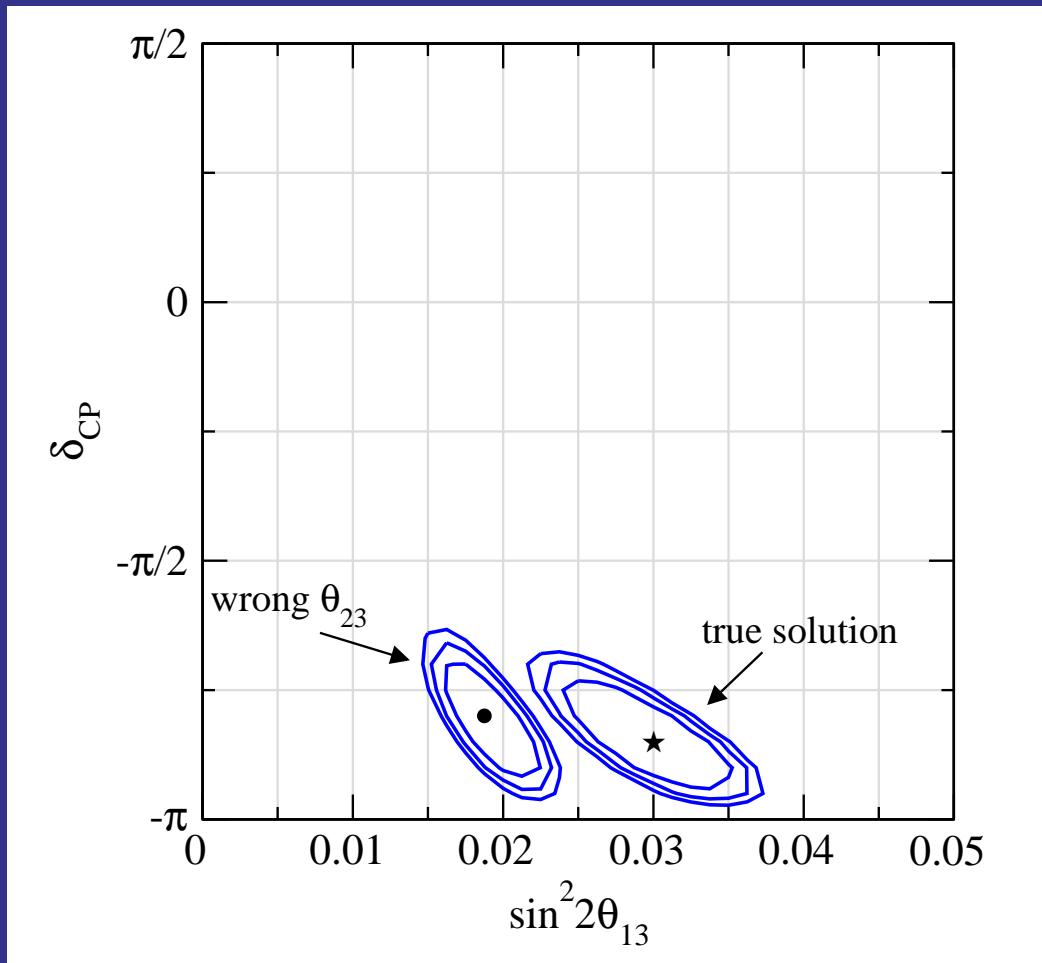
$$\sin^2 2\theta_{13} = 0.03$$

$$\delta = -0.85\pi$$

$$\sin^2 \theta_{23} = 0.4$$

$$\Delta m_{31}^2 = 2.2 \times 10^{-3} \text{ eV}^2$$

# Degeneracies and T2HK



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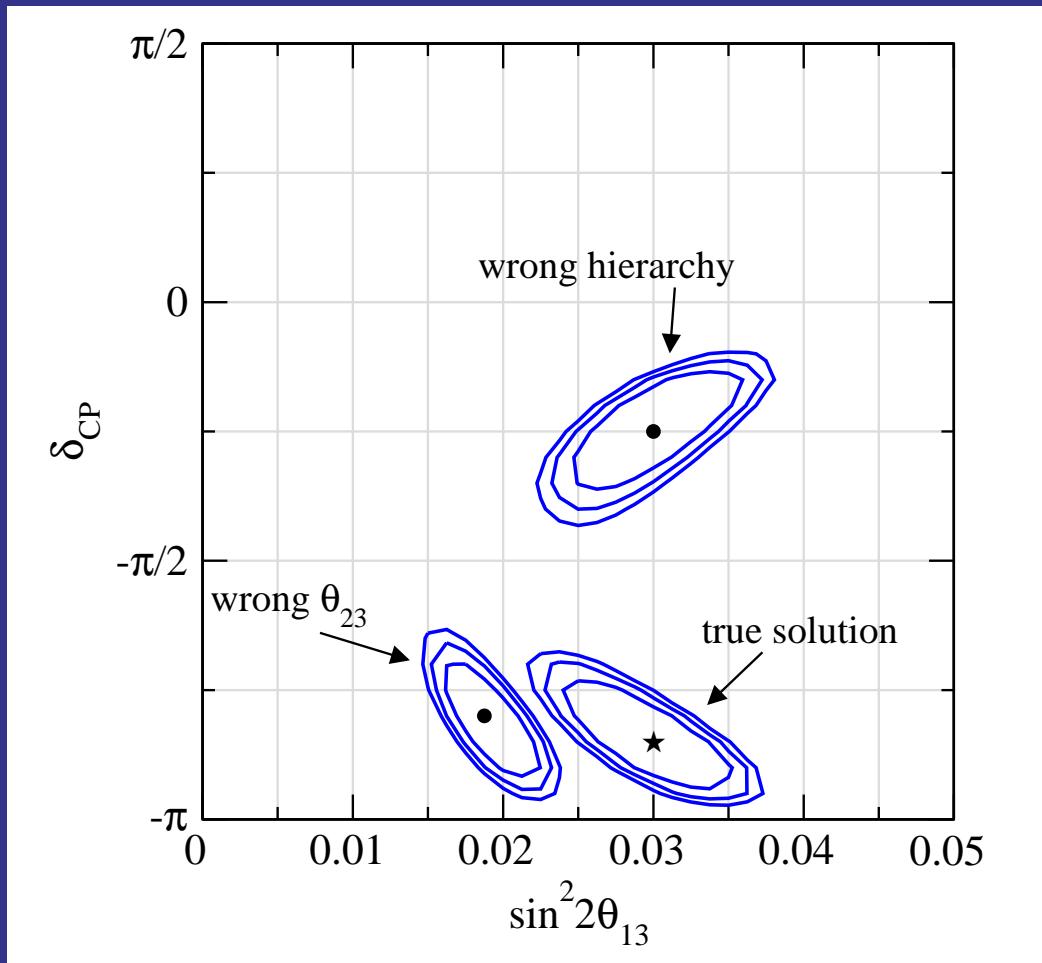
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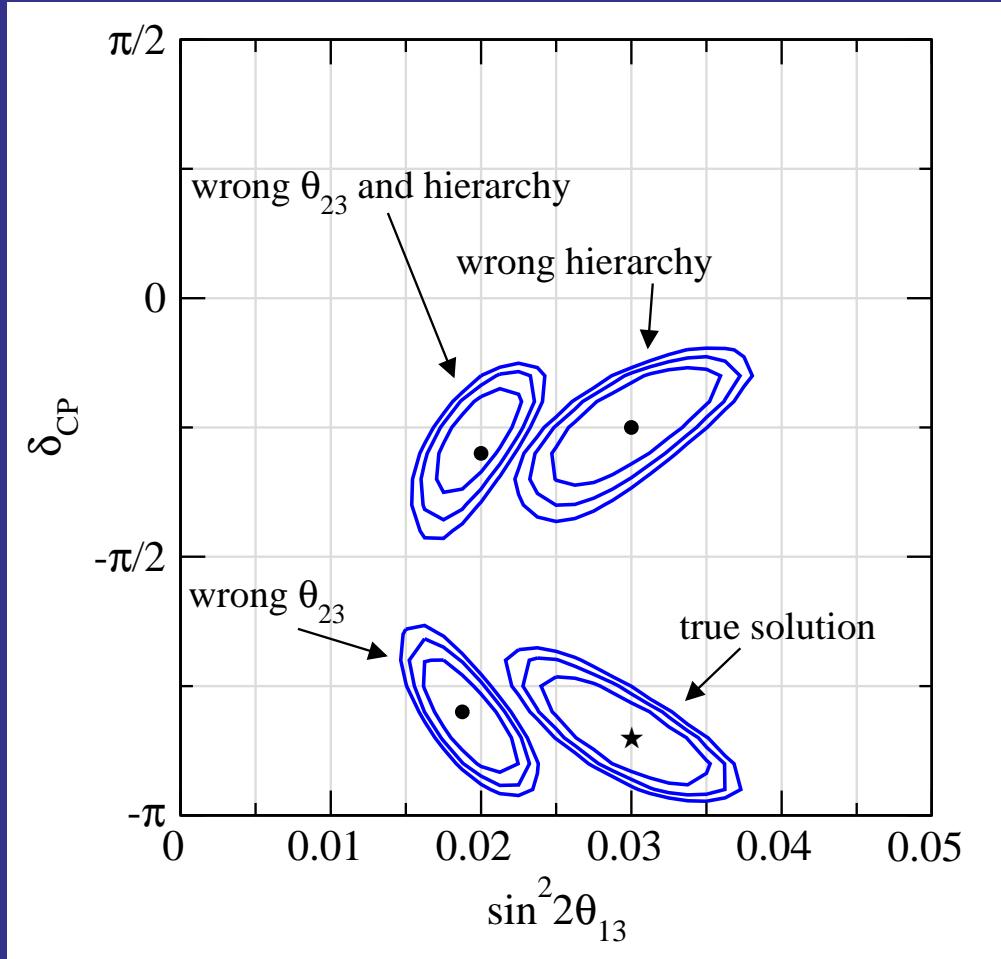
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ambiguities in  $\theta_{13}$  and  $\delta$   
no information on the hierarchy

# *Resolving the degeneracies*

---

several possibilities to resolve the degeneracies are known:

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---

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- combining information from detectors at different baselines and/or energies  
e.g., second osc. maximum, different off-axis angle

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- adding information on  $\theta_{13}$  from a reactor experiment
- combining data from LBL and atmospheric neutrino experiments

---

# **Some comments on the hierarchy determination**

# *Determining the neutrino mass hierarchy*

---

- it's hard experimentally but very interesting for theory

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---

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# *Determining the neutrino mass hierarchy*

---

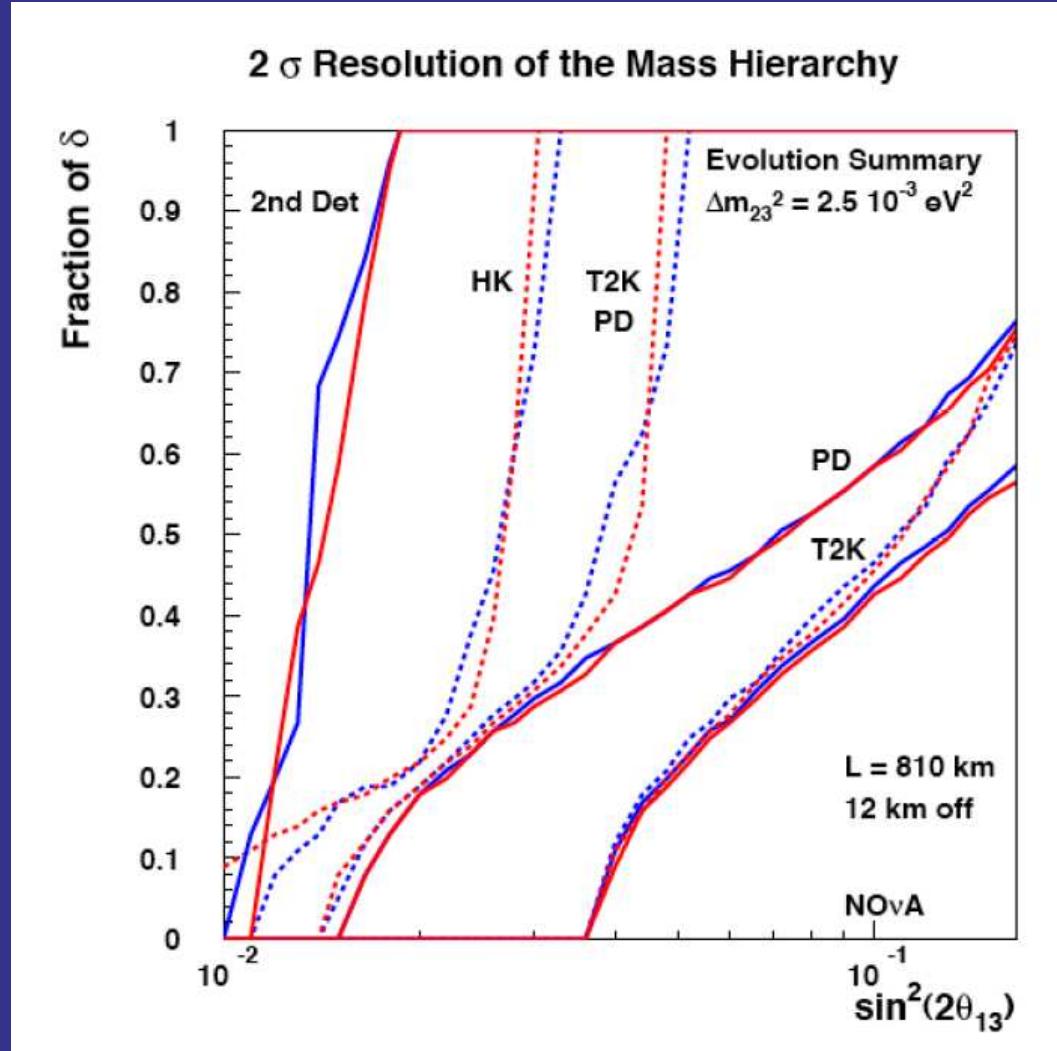
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# *Determining the neutrino mass hierarchy*

---

- it's hard experimentally but very interesting for theory
- needs a large  $\theta_{13}$ :  $\sin^2 2\theta_{13} \gtrsim 0.01$
- needs matter effects
  - very long baseline ( $\gtrsim 700$  km) in beam exps.
  - atmospheric neutrinos
  - supernova neutrinos

# Determining the neutrino mass hierarchy



NO $\nu$ A proposal, hep-ex/0503053

NO $\nu$ A: 30 kt at 810 km  
3 $\nu$ +3 $\bar{\nu}$  yrs

PD = proton driver

2<sup>nd</sup> Det: 50 kt detector  
at 710 km, 30 km off-axis

3 $\nu$ +3 $\bar{\nu}$  yrs NO $\nu$ A+PD +  
3 $\nu$ +3 $\bar{\nu}$  yrs NO $\nu$ A+PD+2<sup>nd</sup> Det  
= 12 yrs total

# *Determining the neutrino mass hierarchy*

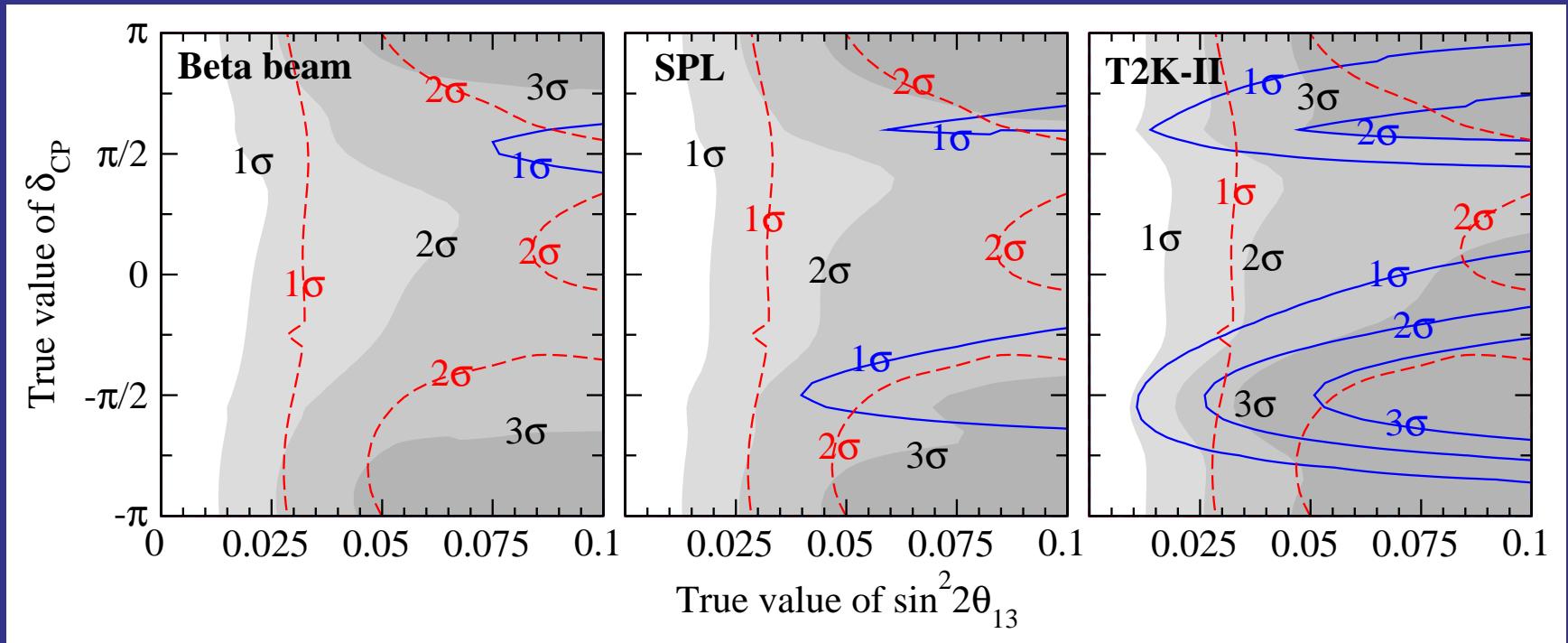
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Combining LBL and atmospheric neutrino data

# Determining the neutrino mass hierarchy

## Combining LBL and atmospheric neutrino data

Huber, Maltoni, Schwetz, PRD71, 053006 (2005) [hep-ph/0501037]



blue: LBL only, red: ATM only, shading: LBL+ATM

450 kton,  $2\nu+8\bar{\nu}$  yrs LBL data, 50 present SK ATM data

# *Determining the neutrino mass hierarchy*

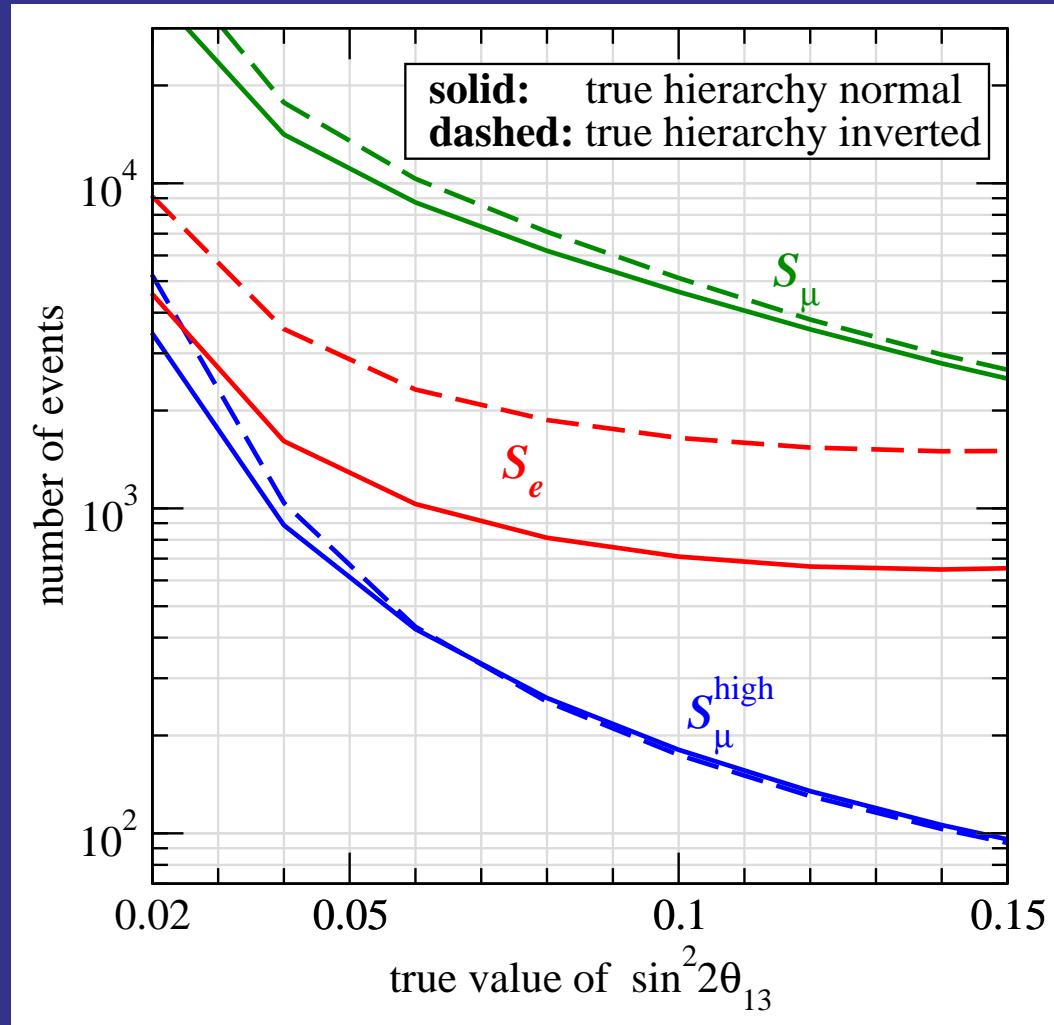
---

atmospheric  $\nu$ s with a magnetized iron detector (**INO**)

# Determining the neutrino mass hierarchy

## atmospheric $\nu$ s with a magnetized iron detector (INO)

# of events needed for a  $2\sigma$  hierarchy determination



Petcov, Schwetz, in preparation

$S_\mu$  ( $S_\mu^{\text{high}}$ ):  $\mu$ -like data with  
15% (5%) energy,  
15° (5°) direction resolution  
 $S_e$ :  $e$ -like data with  
85% charge identification

30 kt, 10 yrs  $\rightarrow$   
 $\sim 1200 \mu$ -events

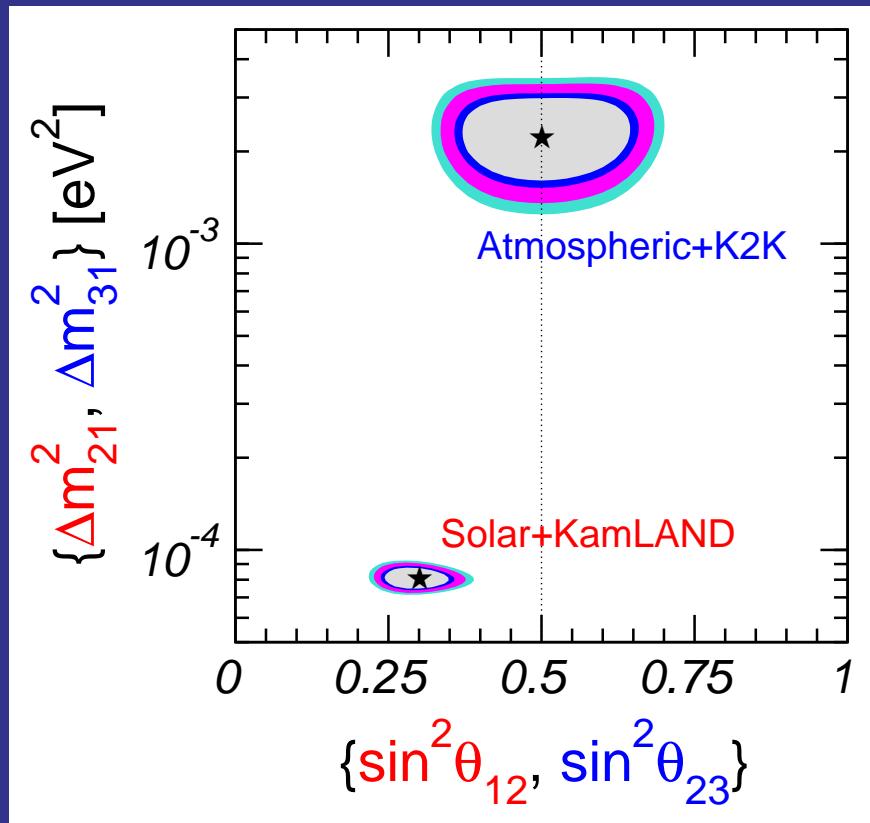
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# Summary

# *Summary*

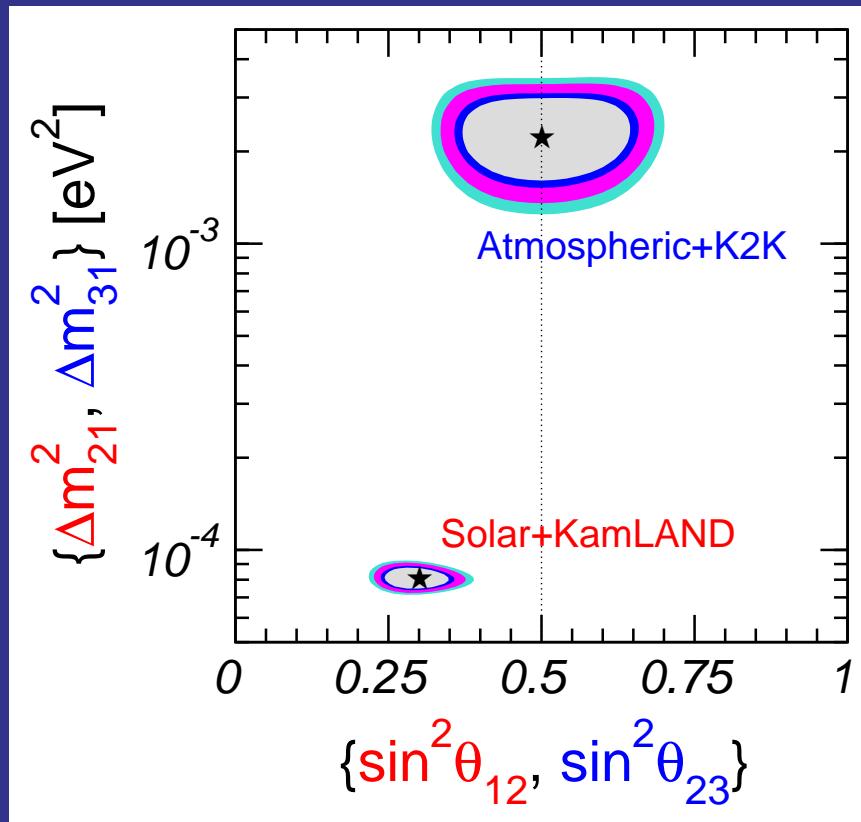
---

present

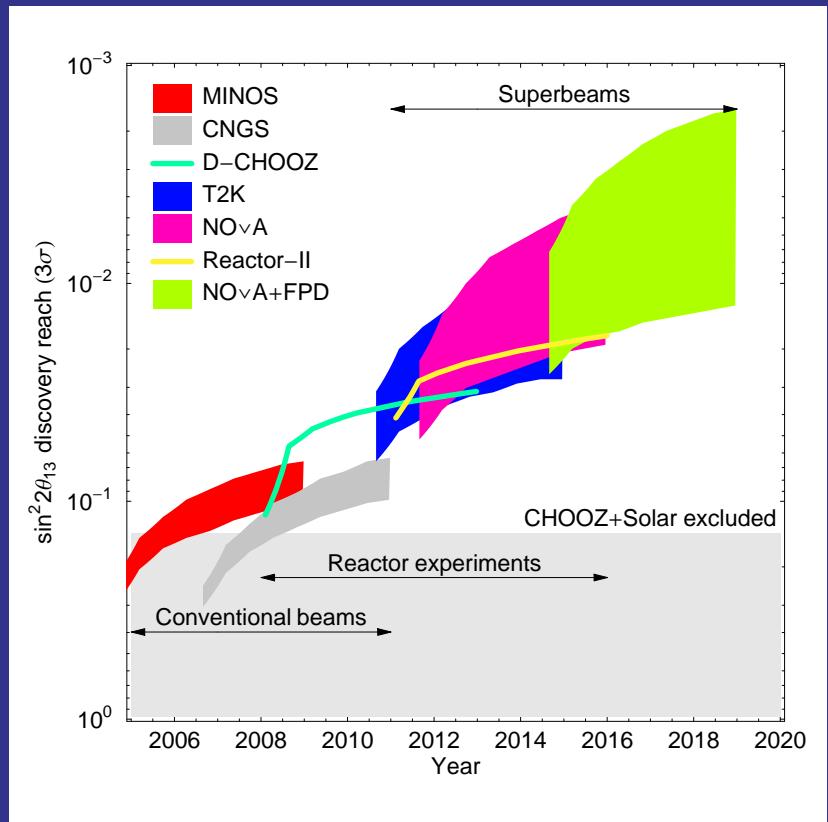


# Summary

present

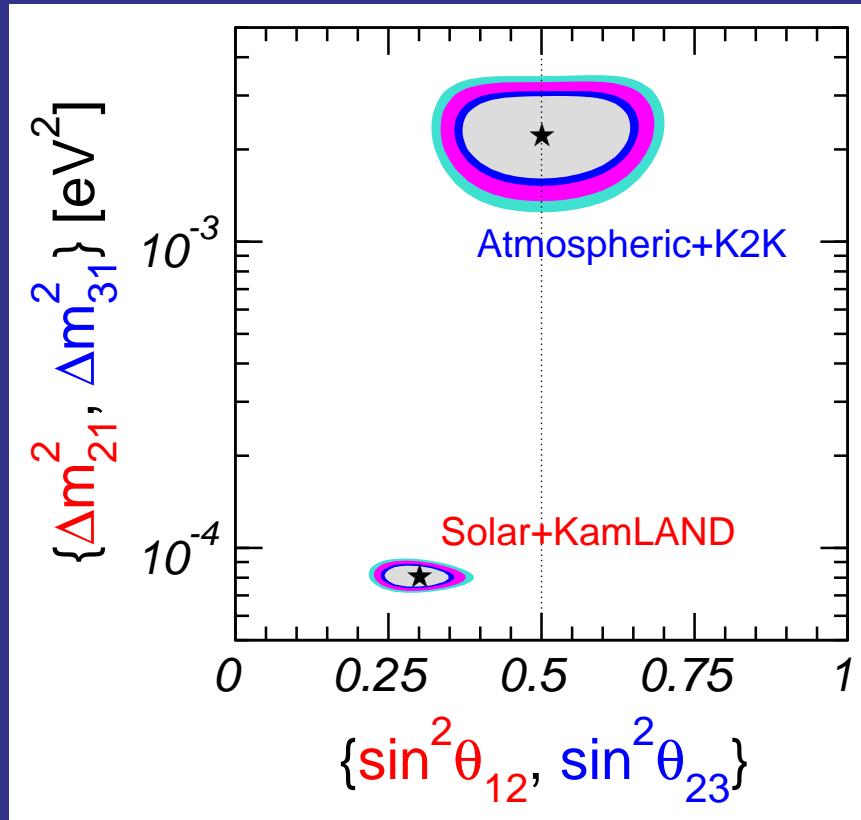


future

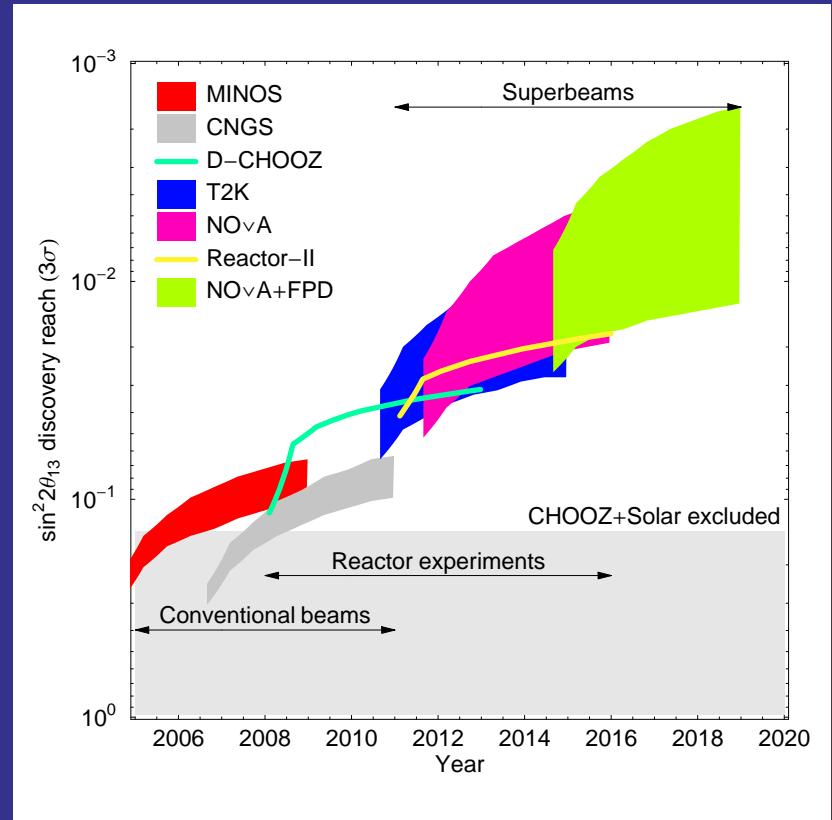


# Summary

present



future



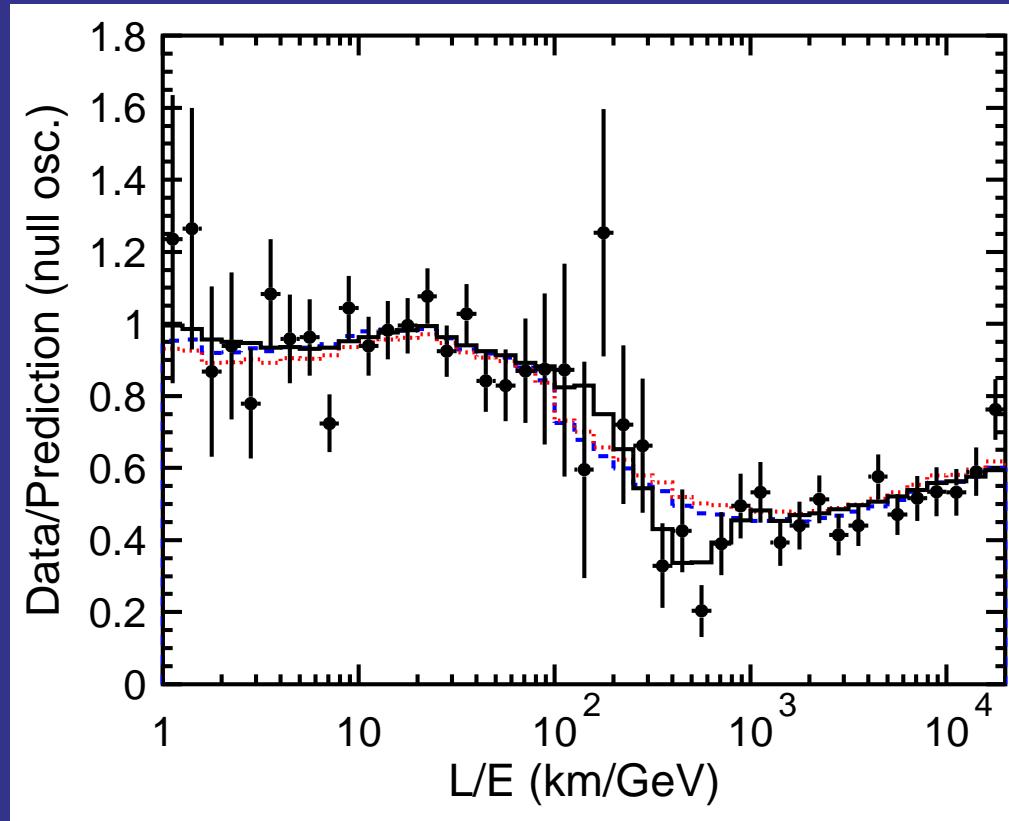
be prepared for surprises: **MiniBooNE**

---

**additional slides**

# Oscillatory signal in atmospheric neutrinos

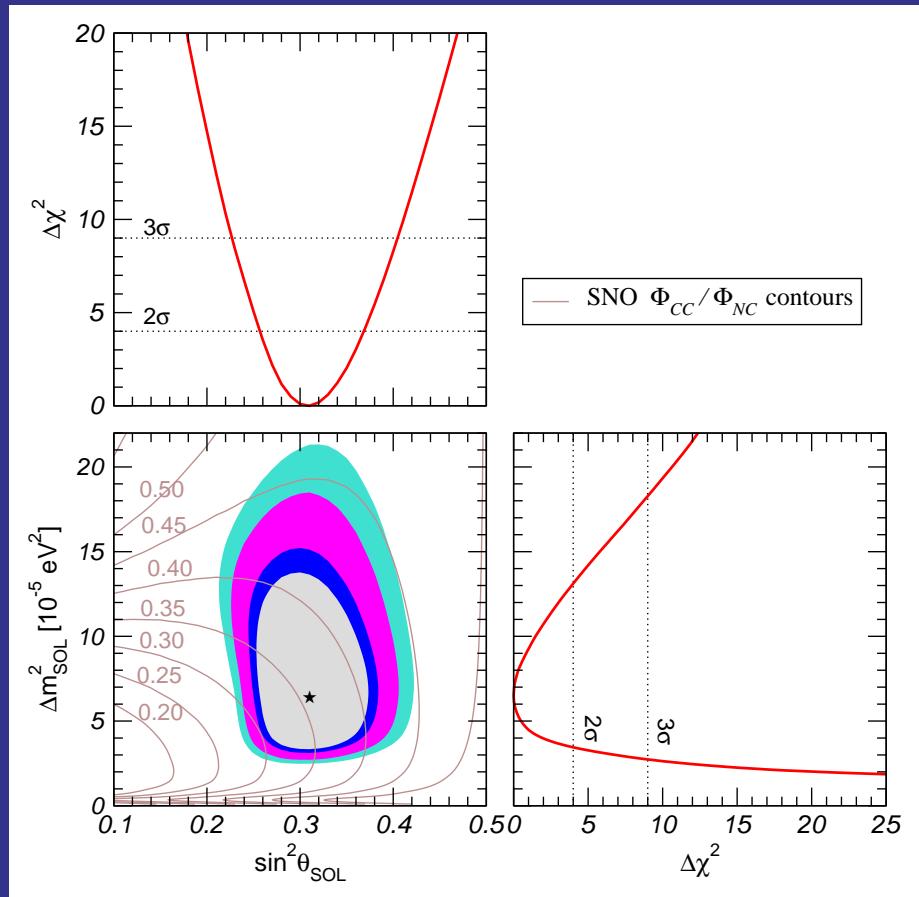
Super-K Coll., Phys. Rev. Lett. **93** (2004) 101801



$$P_{2\nu} = 1 - \sin^2 2\theta \sin^2 \left( \frac{\Delta m^2}{4} \frac{L}{E_\nu} \right)$$

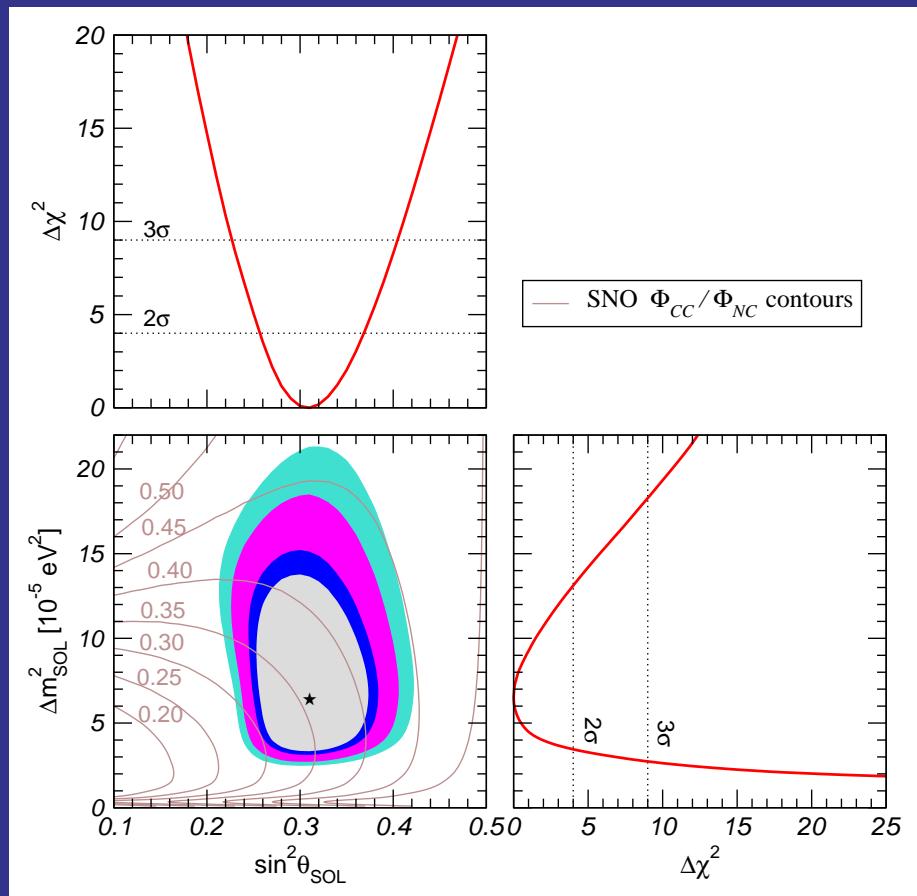
# 'Solar' parameters

global solar neutrino data:  
Homestake, SAGE, GNO, SK, SNO



# 'Solar' parameters

global solar neutrino data:  
Homestake, SAGE, GNO, SK, SNO



$$\sin^2 \theta_{12} = 0.30^{+0.02}_{-0.03} \rightarrow 0.31^{+0.02}_{-0.03}$$

The SNO experiment:



SNO-II 391d nucl-ex/0502021

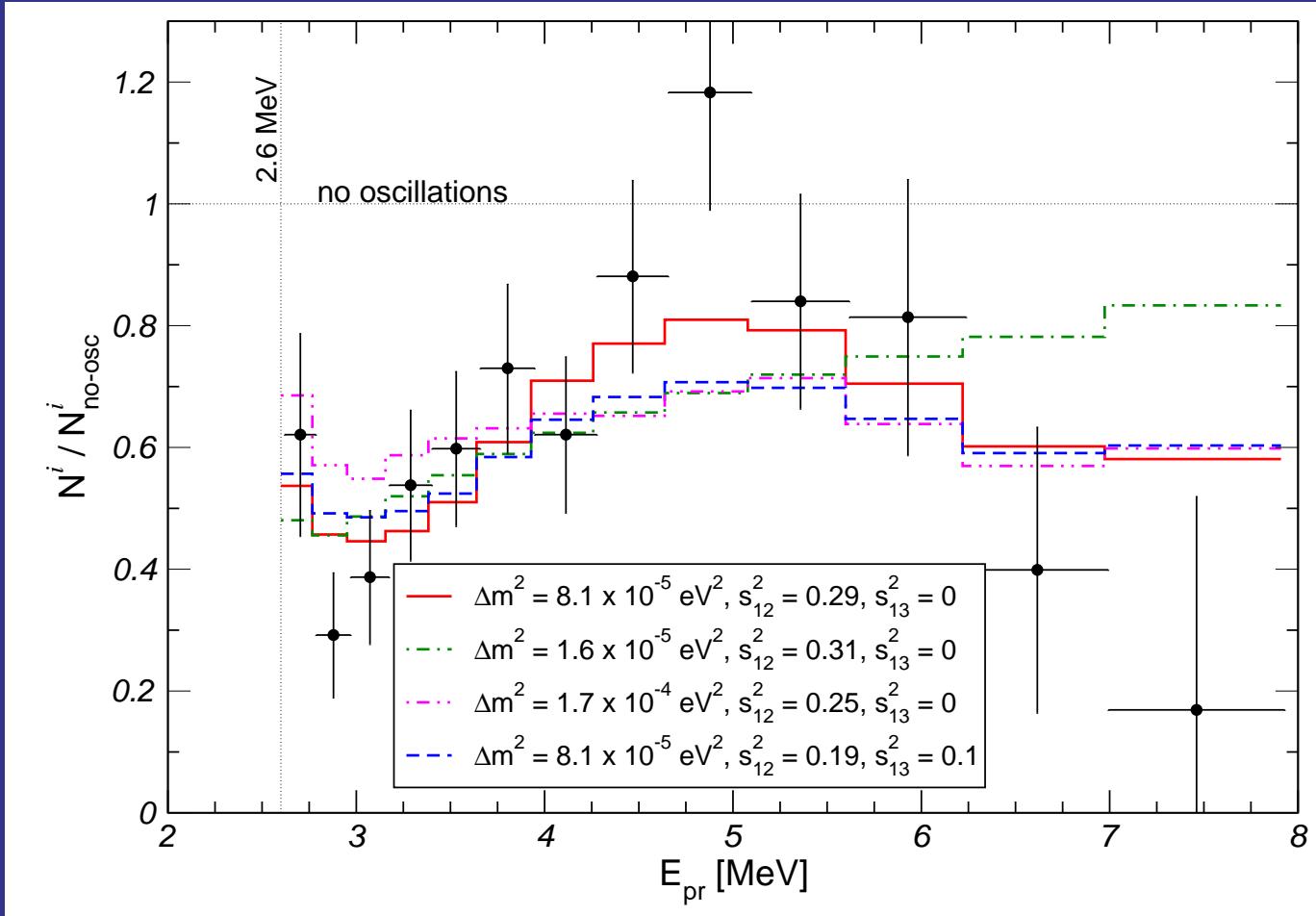
$$\frac{\phi_{CC}}{\phi_{NC}} = 0.340 \pm 0.023 \pm 0.030$$

7 $\sigma$  evidence for a non-zero  
 $\nu_{\mu,\tau}$  flux from the sun

constraint on  $\theta_{12}$ :

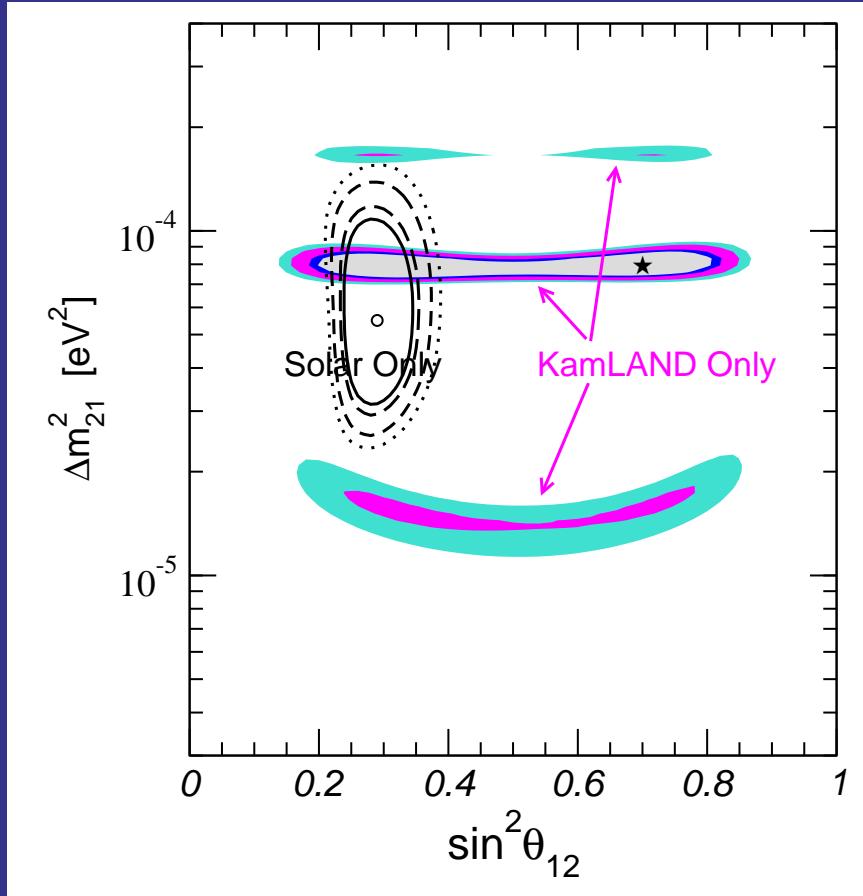
$$\frac{\phi_{CC}}{\phi_{NC}} \approx P_{ee}^{\text{SNO}} \approx \sin^2 \theta_{12}$$

# The KamLAND energy spectrum

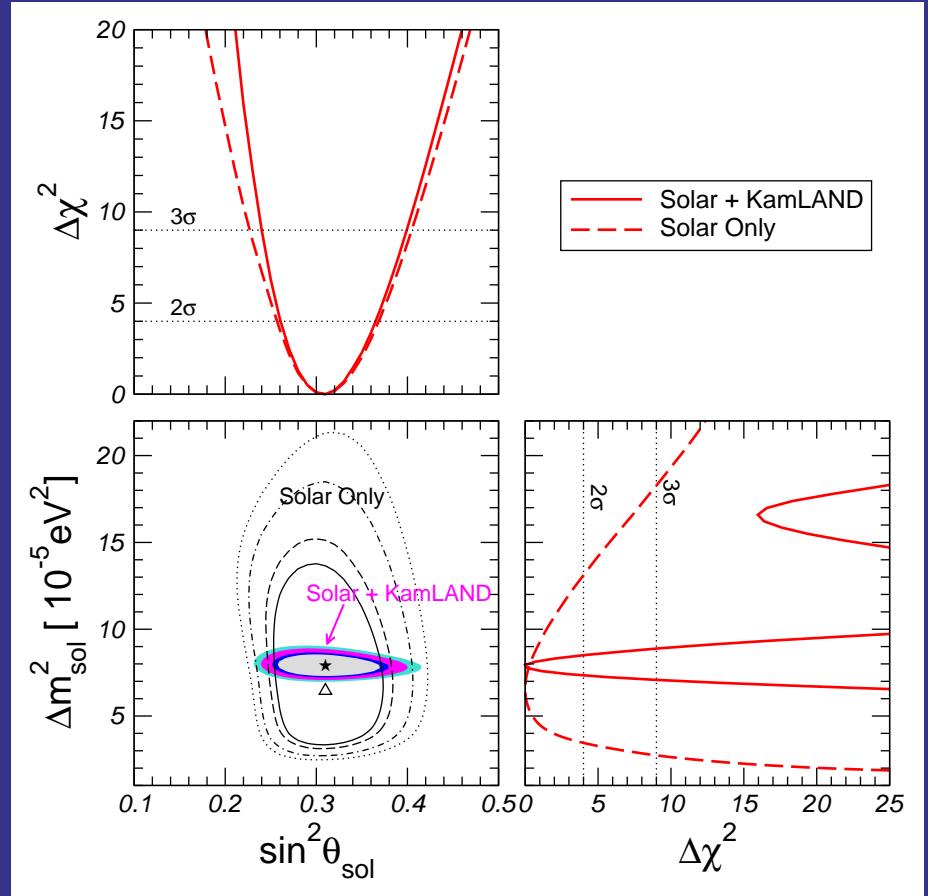
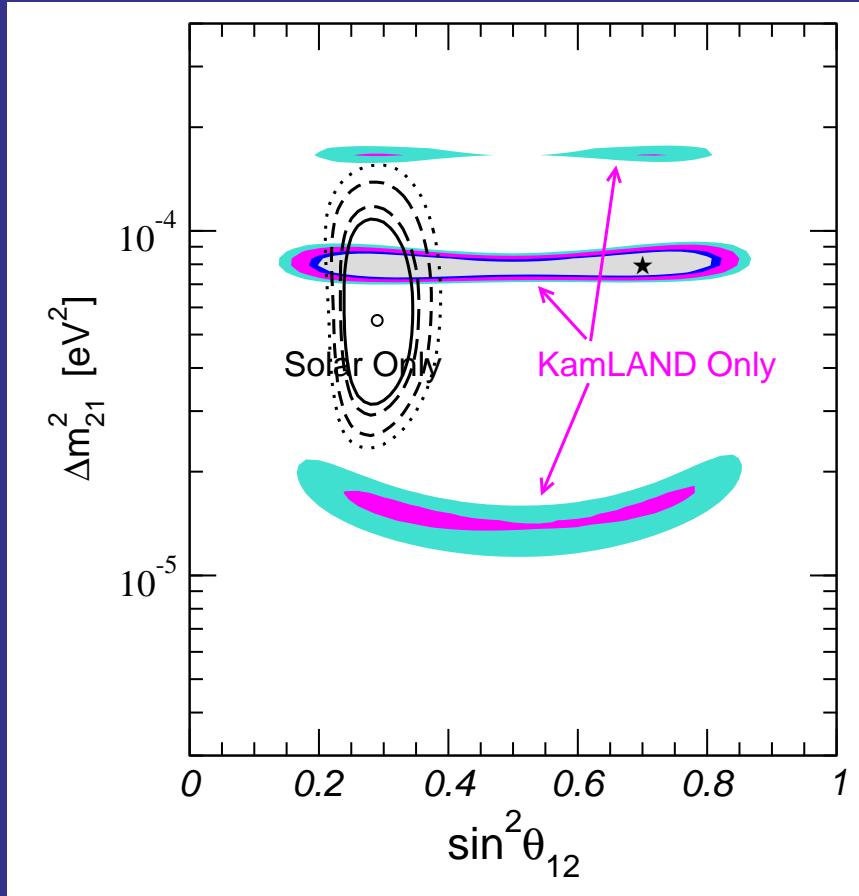


evidence for flux suppression and spectral distortion

# *KamLAND vs solar data*



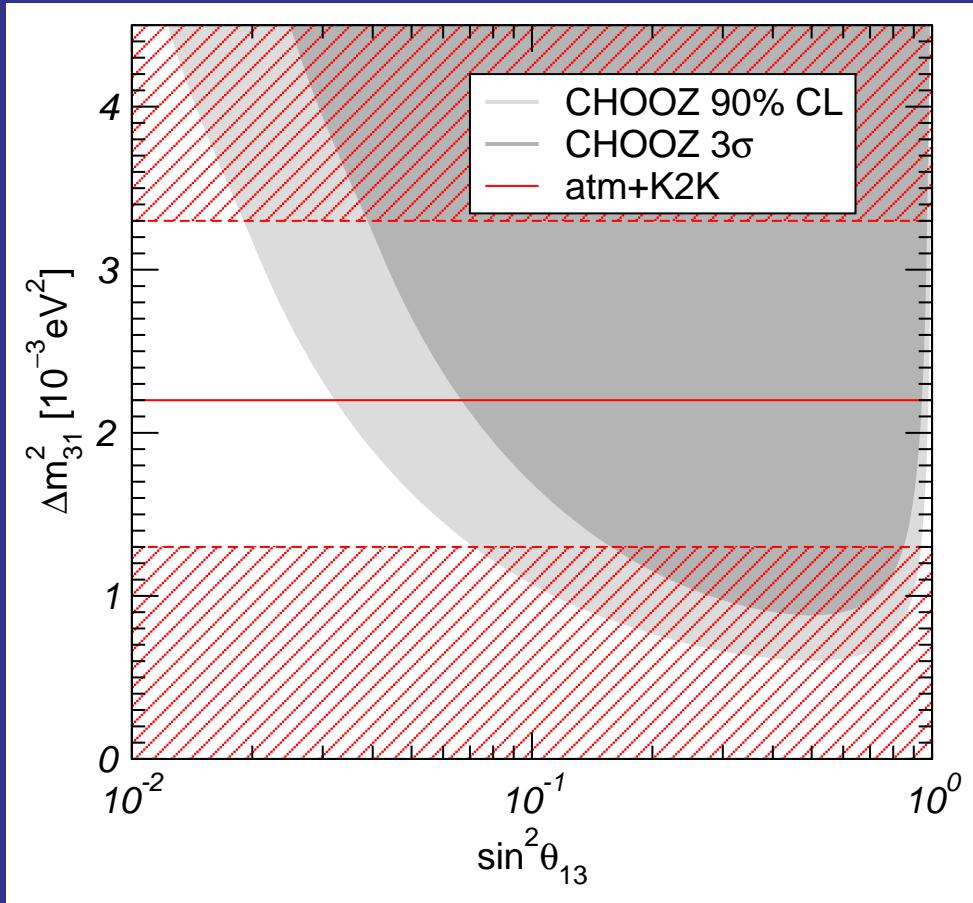
# KamLAND vs solar data



$$\Delta m^2 = 7.9 \pm 0.3 \times 10^{-5} \text{ eV}^2, \sin^2 \theta_{12} = 0.31^{+0.02}_{-0.03}$$

# *The bound on $\theta_{13}$*

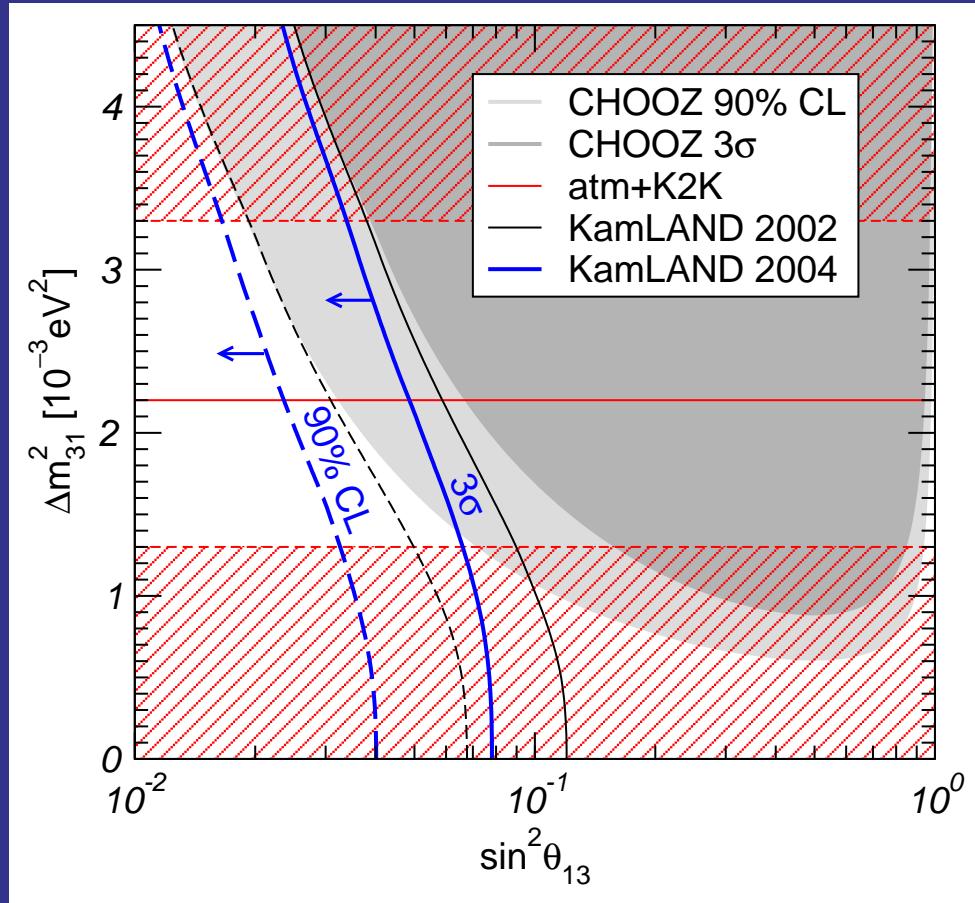
CHOOZ bound depends on the value of  $\Delta m_{13}^2$



CHOOZ+atm+K2K:  
 $\sin^2 \theta_{13} < 0.029$  (0.067)

# *The bound on $\theta_{13}$*

solar data contribute for low  $\Delta m_{13}^2$



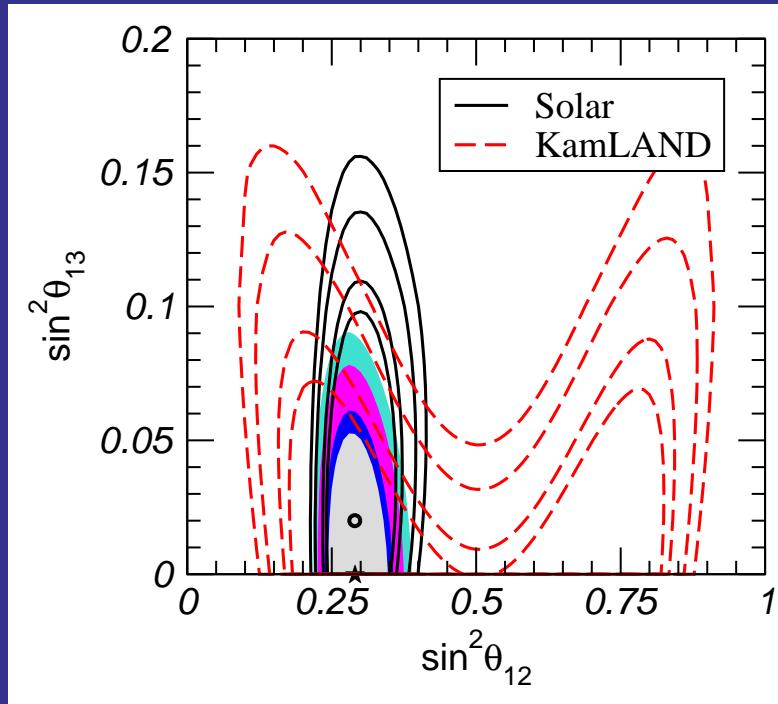
CHOOZ+atm+K2K:  
 $\sin^2 \theta_{13} < 0.029$  (0.067)

solar+KamL:  
 $\sin^2 \theta_{13} < 0.041$  (0.079)

global:  
 $\sin^2 \theta_{13} < 0.021$  (0.046)

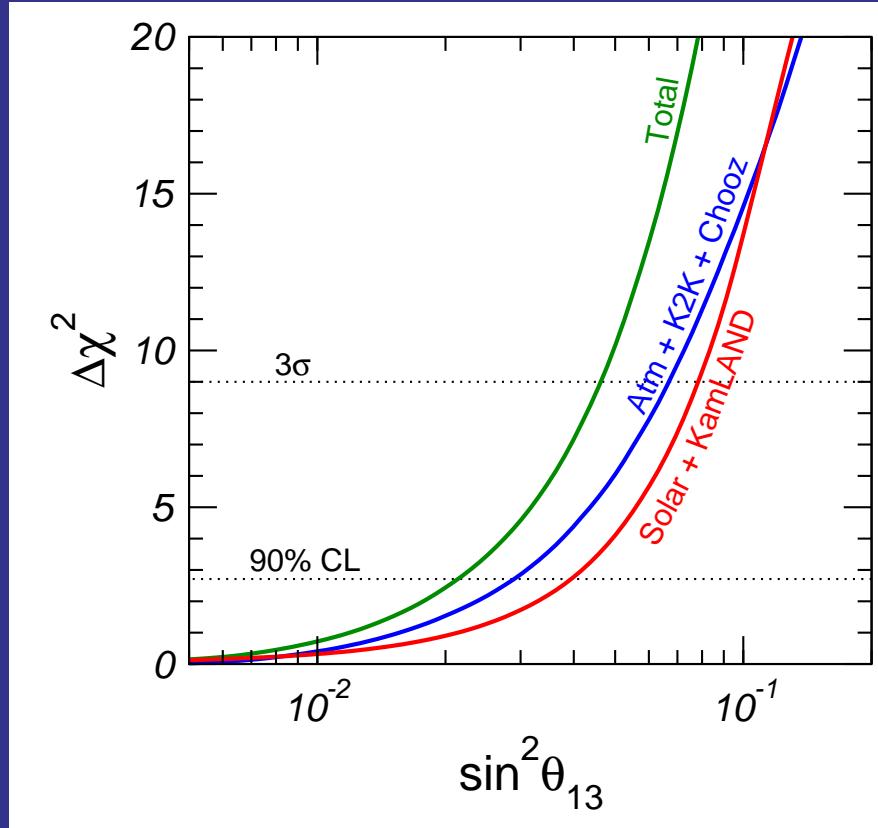
# The $\theta_{13}$ bound from KamLAND and solar

complementarity between solar and KamLAND data



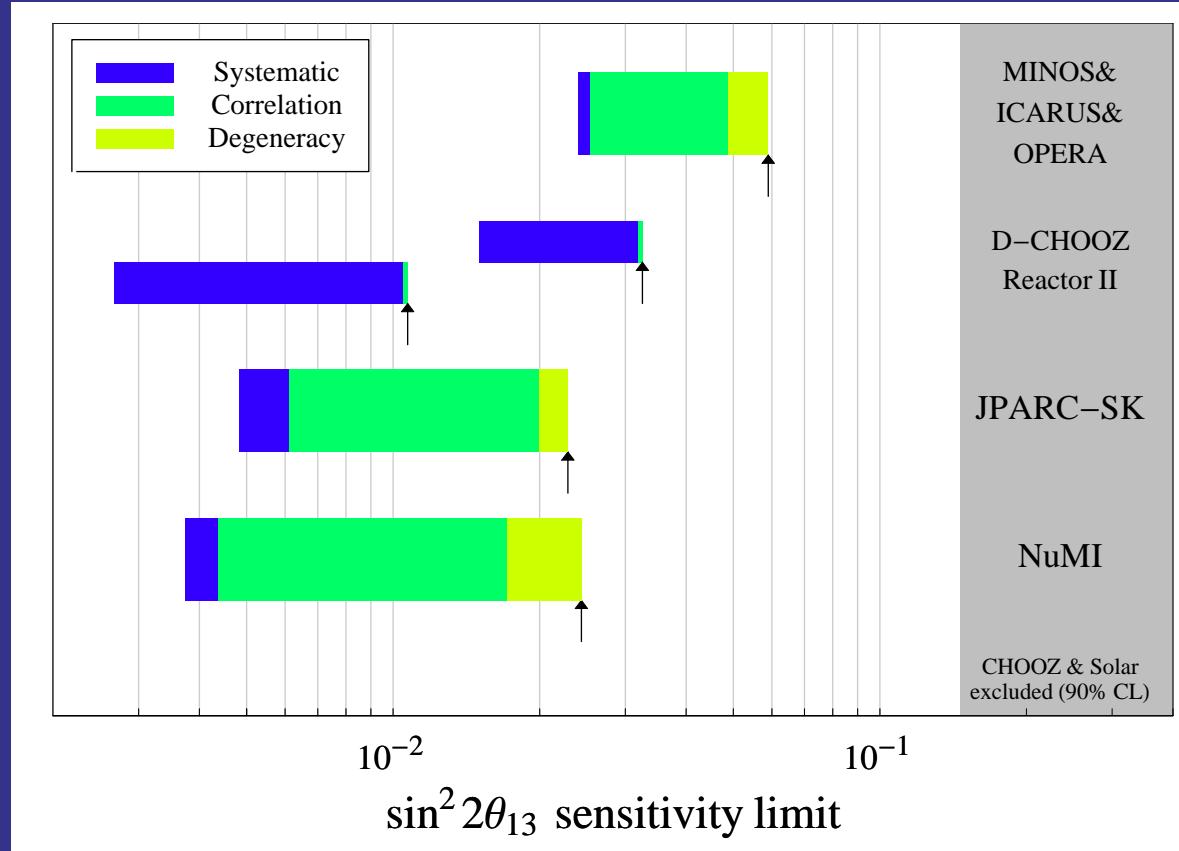
$$P_{\text{KL}} = (1 - 2 \sin^2 \theta_{13}) \left( 1 - \sin^2 2\theta_{12} \sin^2 \frac{\Delta m_{21}^2 L}{4E_\nu} \right)$$
$$P_{\text{Sol}} \approx (1 - 2 \sin^2 \theta_{13}) \begin{cases} \sin^2 \theta_{12} & \text{high } E_\nu \\ (1 - 0.5 \sin^2 2\theta_{12}) & \text{low } E_\nu \end{cases}$$

# *The global bound on $\theta_{13}$*



$\sin^2 \theta_{13} < 0.021$  (0.046) at 90% CL ( $3\sigma$ )

# $\sin^2 2\theta_{13}$ -limit within the next ten years



true values:

$$\sin^2 2\theta_{12} = 0.8$$

$$\sin^2 2\theta_{23} = 1.0$$

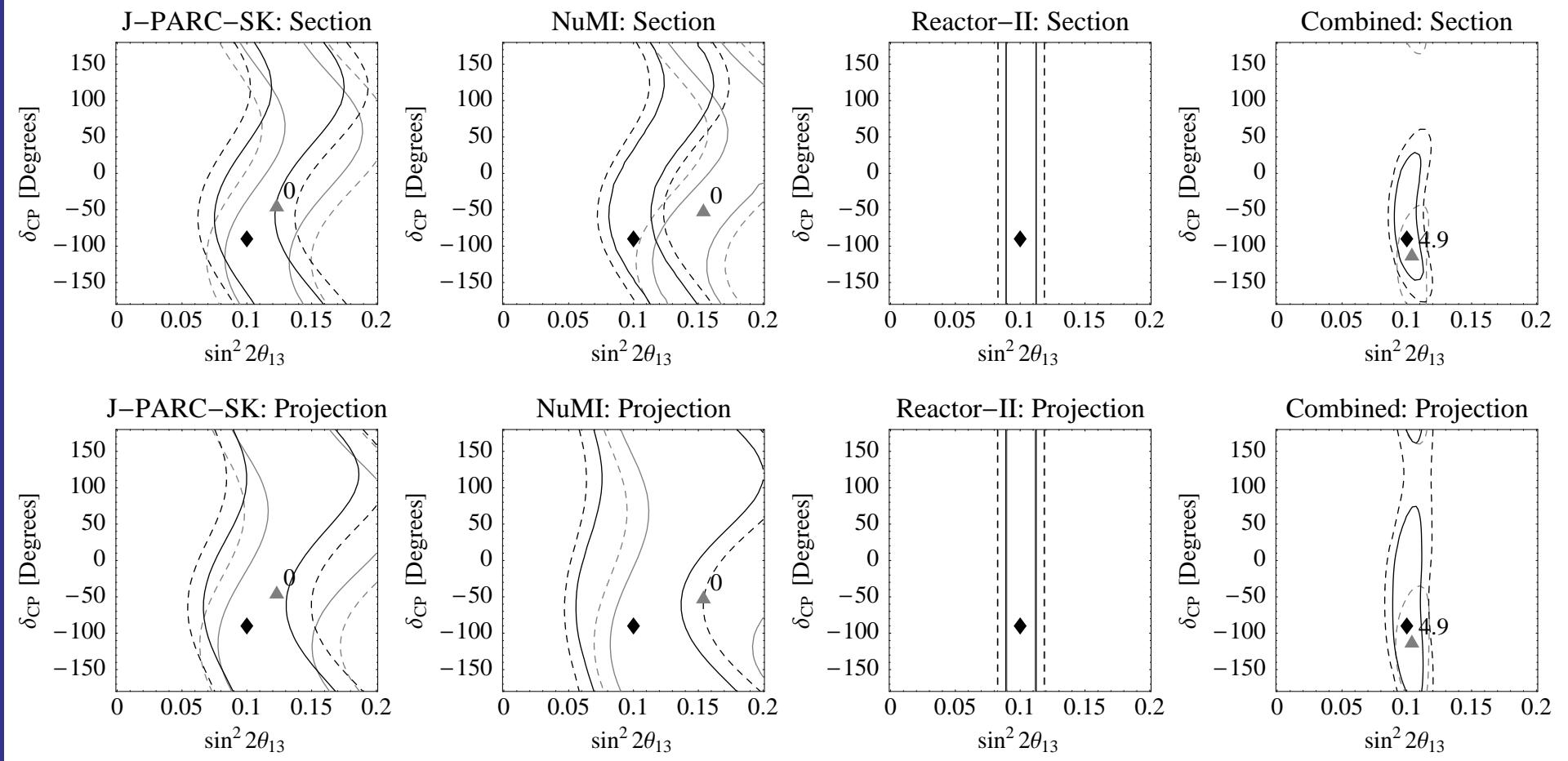
$$\sin^2 2\theta_{13} = 0.0$$

$$\Delta m_{21}^2 = 7.0 \cdot 10^{-5} \text{ eV}^2$$

$$\Delta m_{31}^2 = 2.0 \cdot 10^{-3} \text{ eV}^2$$

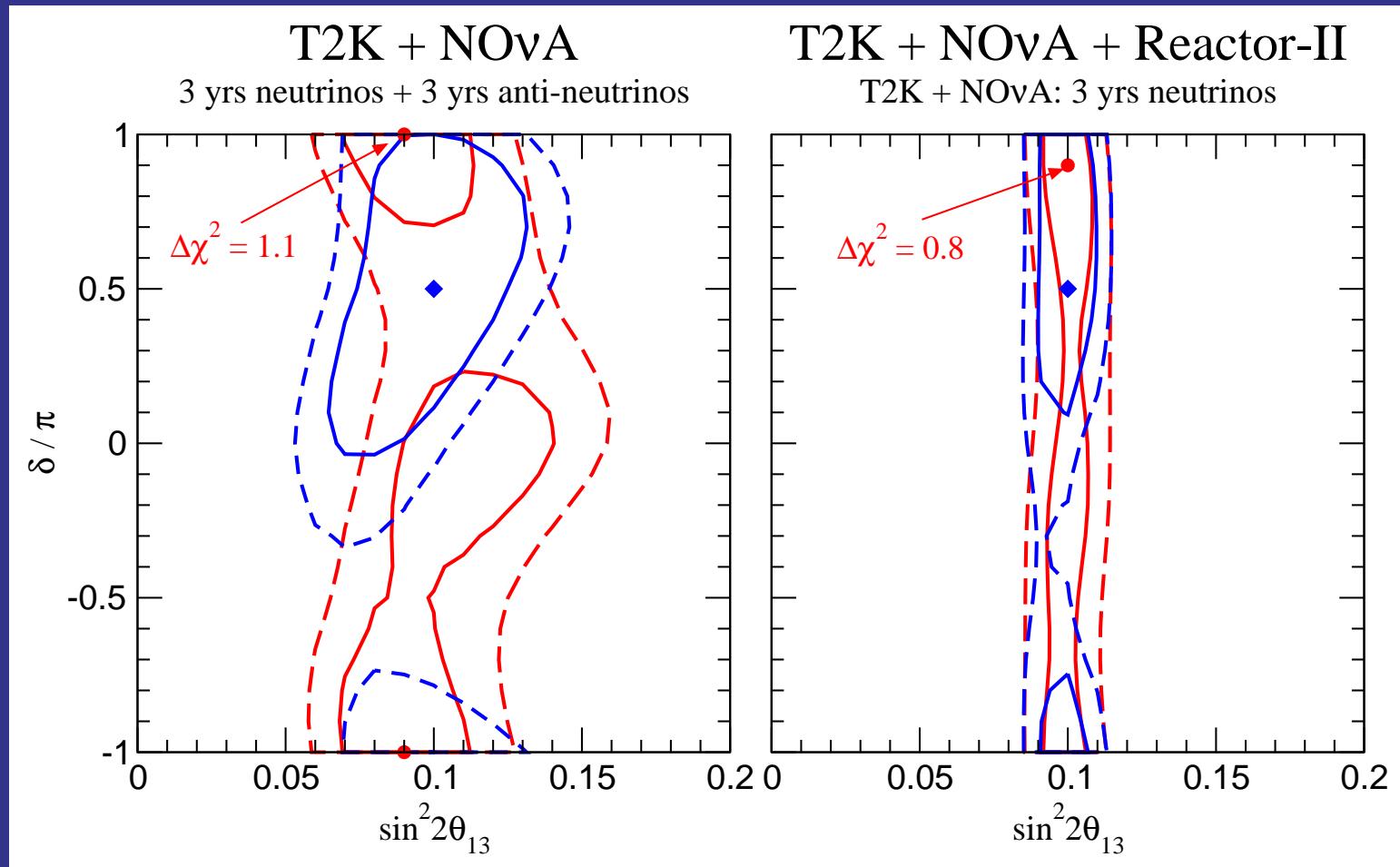
Huber, Lindner, Rolinec, Schwetz, Winter, hep-ph/0403068

# Potential if $\sin^2 2\theta_{13}$ turns out to be large



# Potential if $\sin^2 2\theta_{13}$ turns out to be large

Superbeam anti-neutrino running vs reactor experiments



# $\theta_{13}$ limit

