The image shows the interior of the Sudbury Neutrino Observatory (SNO), a large spherical detector. The central part of the image is dominated by a dense array of photomultiplier tubes (PMTs) arranged in a circular pattern. A central detector module, likely a liquid scintillator, is visible in the middle. The overall lighting is a deep blue, highlighting the metallic and glass components of the detector. The text is overlaid in a bright orange color.

# Measurement of Solar Neutrino Flux with an Array of Neutron Detectors in SNO

Blair Jamieson

University of British Columbia

for

*the Sudbury Neutrino Observatory*

*Collaboration*

*ICHEP'08, July 30, 2008*

# SNO

6000 mwe  
overburden

1000 tonnes D<sub>2</sub>O

12 m Diameter  
Acrylic Vessel

1700 tonnes Inner  
Shield H<sub>2</sub>O

Support Structure  
for 9500 PMTs,  
60% coverage

5300 tonnes Outer  
Shield H<sub>2</sub>O

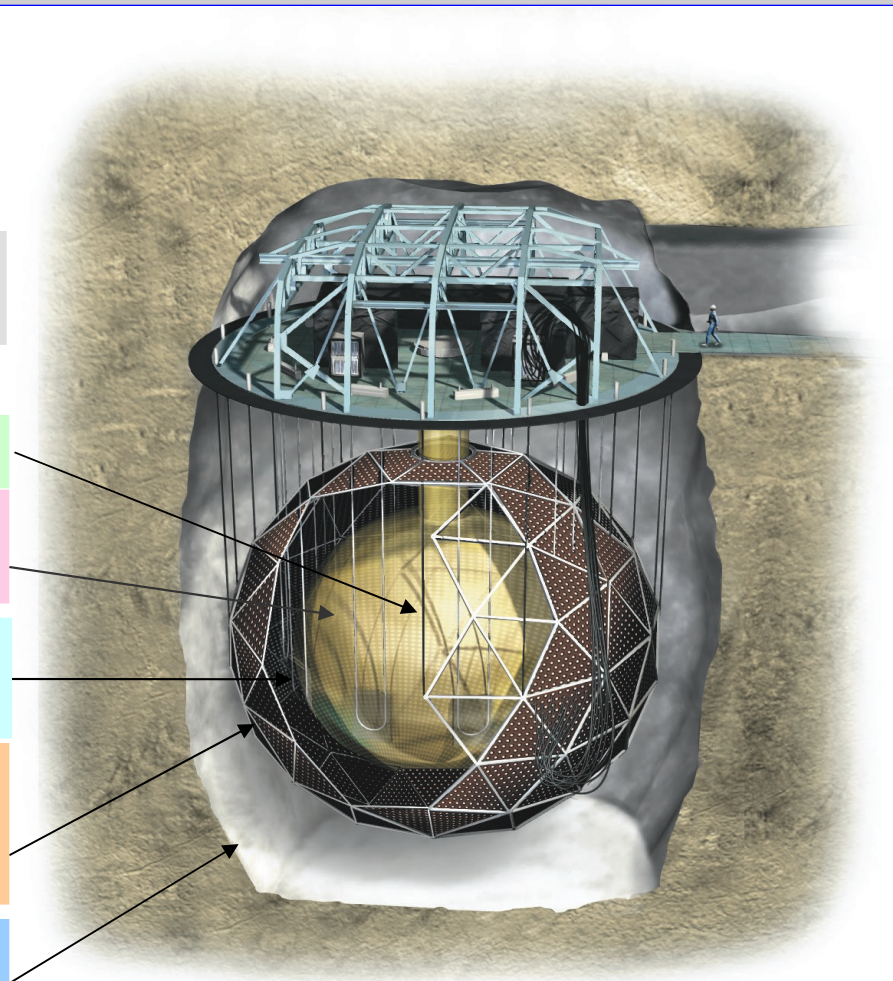
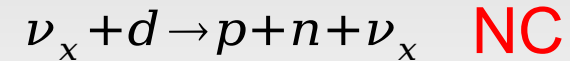
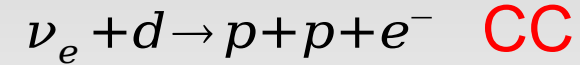
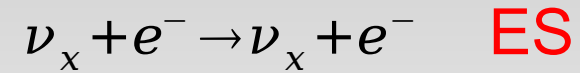
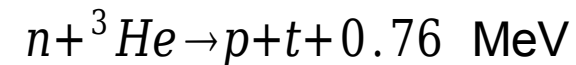
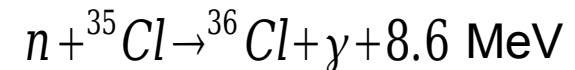
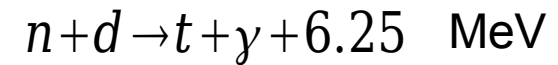


Image courtesy National Geographic

## 3 Reactions:



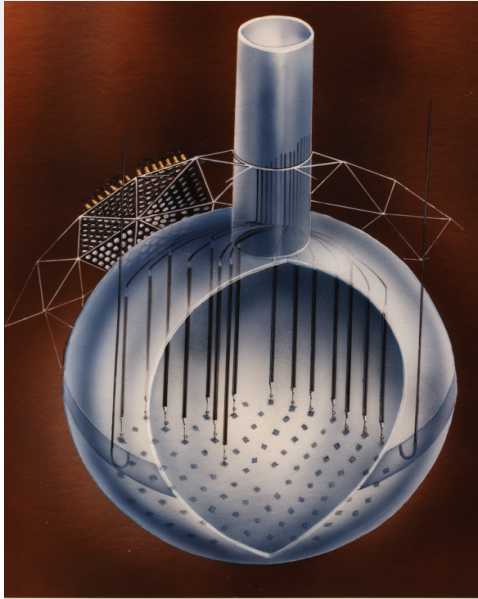
## 3 neutron detection methods:



## 3 Phases:

- Just D<sub>2</sub>O
- D<sub>2</sub>O + 2 tonnes NaCl
- D<sub>2</sub>O + <sup>3</sup>He Proportional Counters (“NCDs”)

# Why use NCDs?



## The features:

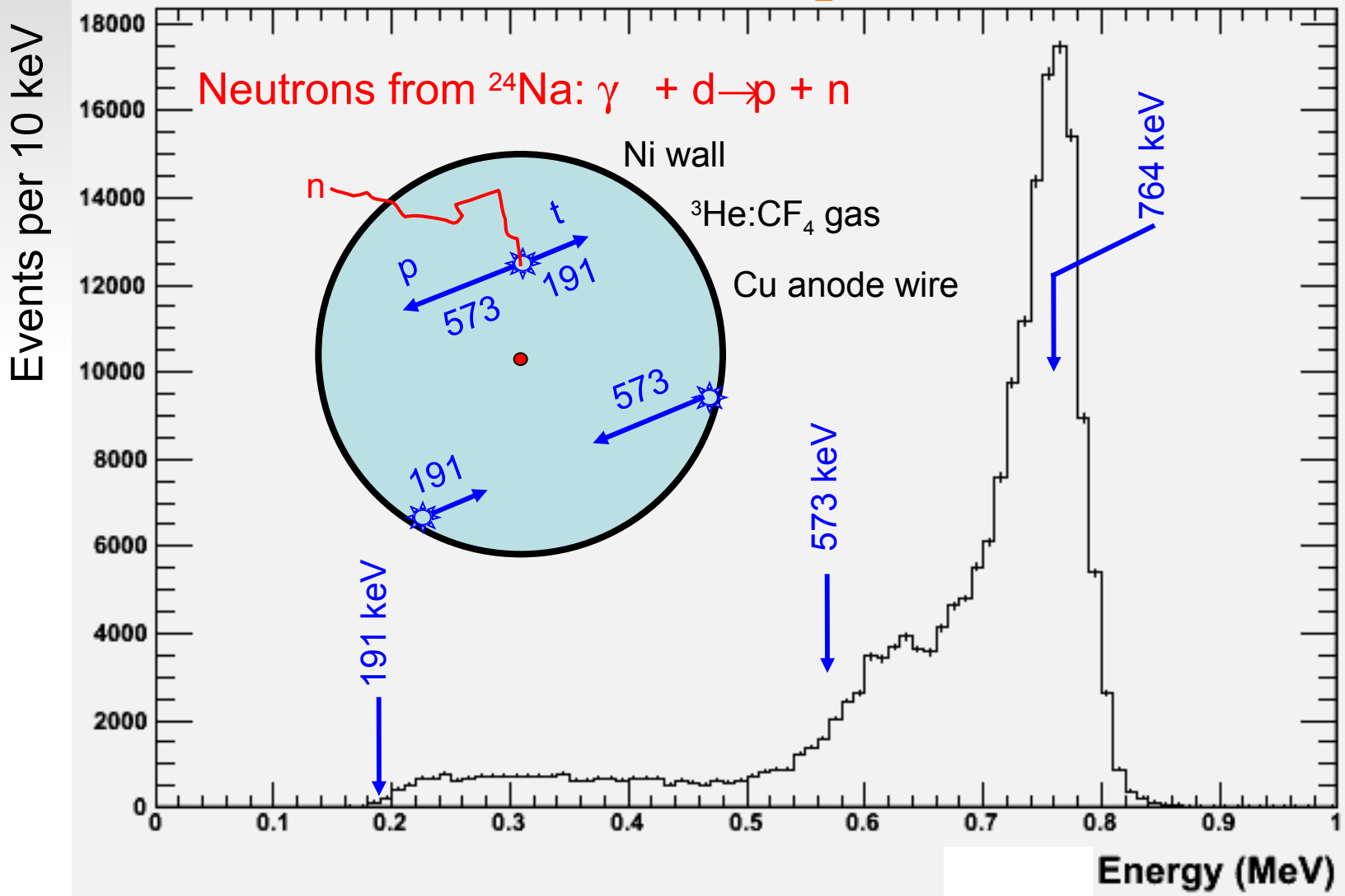
- Different systematics from other Phases.
- Separate signal paths: neutron capture no longer competes with *CC* events in Cherenkov light.
- Break correlation between *CC* and *NC* signals.
- *CC* spectrum contamination by 6.25-MeV capture gammas reduced by capture in *NCD* array, and determined independently.

## The difficulties:

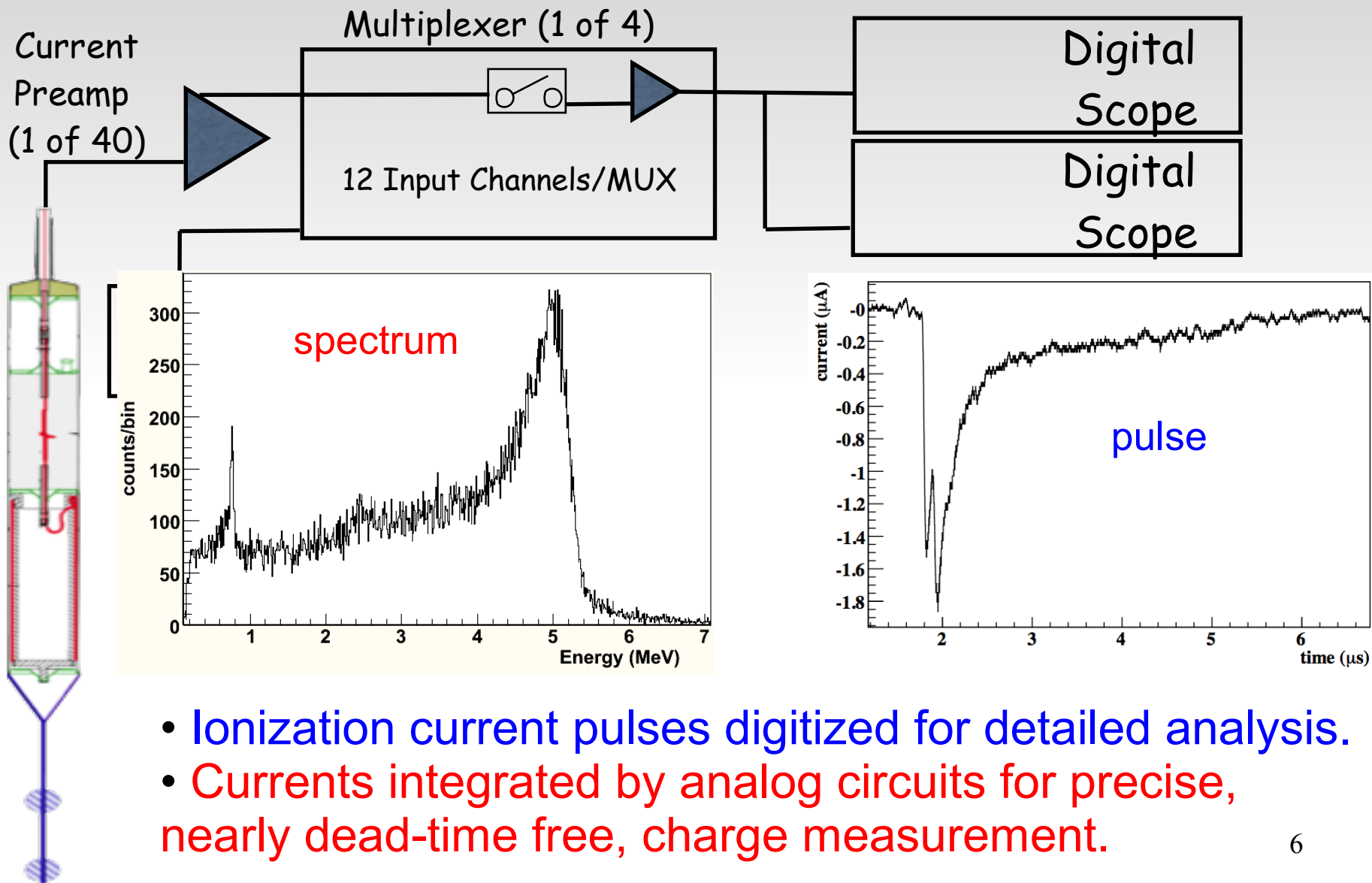
- Signal rate low:  $\sim 1000$  neutrons/year detected.
- Ultra-low background materials needed.
- Some light loss ( $\sim 10\%$ ) due to array.
- Complexity.



# Energy Spectrum from ${}^3\text{He}(n,p)t$



# NCD Electronics - Data Acquisition



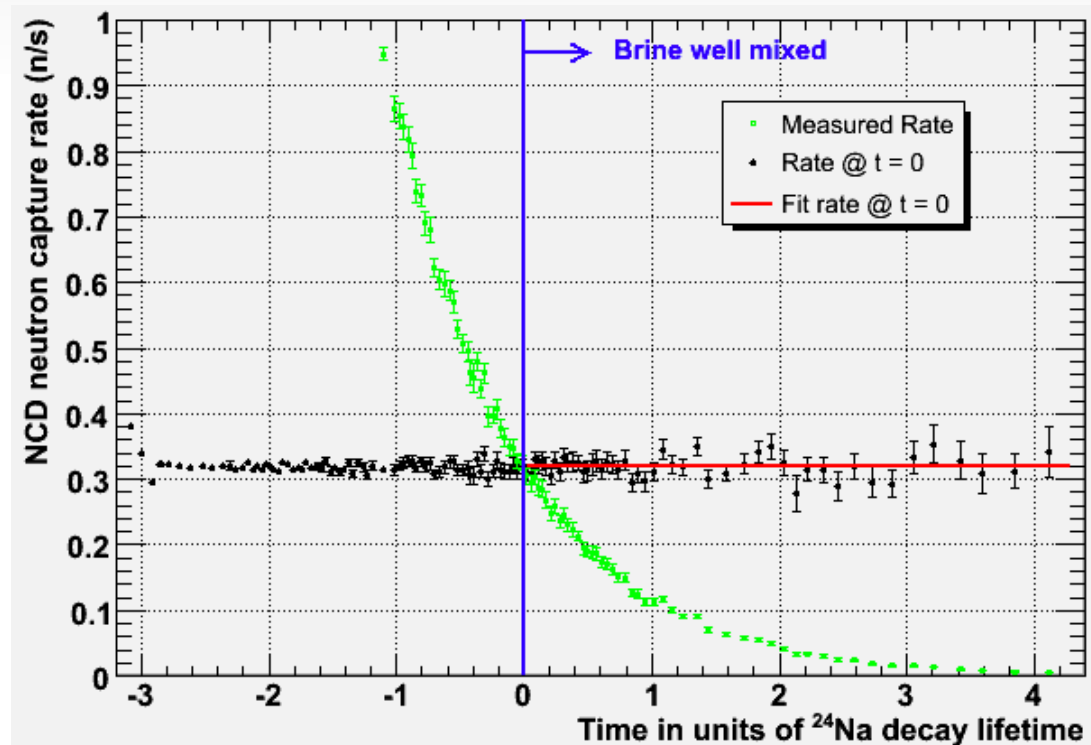
# Calibrating the Neutron Efficiency

- Solar neutrinos produce neutrons uniformly in the  $D_2O$ .
- Monte Carlo based on Los Alamos “MCNP” code yields efficiency of 0.210(3).
- Time-series analysis (which is independent of source strength) of neutron bursts from  $^{252}Cf$  fission confirms Monte Carlo precision.

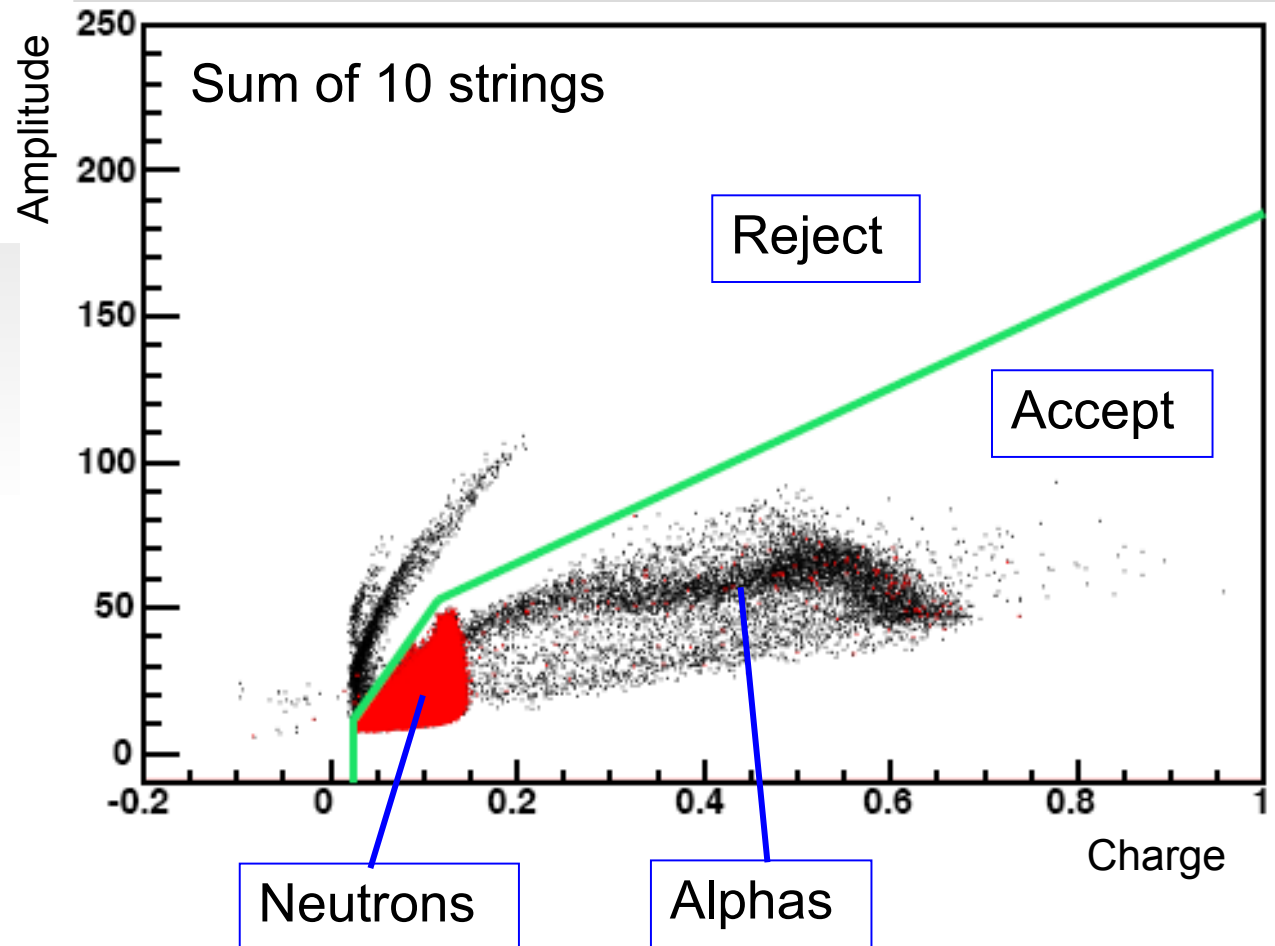
• Neutron efficiency can also be measured experimentally: Dissolve  $^{24}NaCl$  brine in the  $D_2O$ , mix well.

• 15-hr  $^{24}Na$ : 2.75-MeV  $\gamma$  breaks up deuteron, liberates a neutron.

• A uniform source!



# Cutting instrumental events



- Ionization events easily separated from instrumentals
- 6 strings with high instrumental were dropped from analysis



# Blind Analysis

## Three blindfolds for the analysts:

- First month of neutrino data open
- Then only 20% open to 12/05 to finalize instrumental background cuts
- Thereafter include hidden fraction of neutrons that follow muons, AND
- Omit an unknown fraction of candidate events

Detailed internal documentation, review by “topic committees”

## Box Opened May 2, 2008

- Results presented are as found, except...
- Difference between uncertainties from 3 signal-extraction codes: “Pilot errors” corrected, no change in central values, uncertainties agree.
- An incorrect algorithm in fitting the peak value of the ES posterior distributions replaced.

# Backgrounds

Source	PMT neutrons	NCD neutrons
D <sub>2</sub> O Radioactivity	$7.6 \pm 1.2$	$28.7 \pm 4.7$
Atmospheric $\nu$ , <sup>16</sup> N	$24.7 \pm 4.6$	$13.6 \pm 2.7$
Other backgrounds	$0.7 \pm 0.1$	$2.3 \pm 0.3$
NCD Bulk PD, <sup>17,18</sup> O( $\alpha$ ,n)	$4.6^{+2.1}_{-1.6}$	$27.6^{+12.9}_{-10.3}$
NCD hotspots	$17.7 \pm 1.8$	$64.4 \pm 6.4$
NCD cables	$1.1 \pm 1.0$	$8.0 \pm 5.2$
External-source neutrons	$20.6 \pm 10.4$	$40.9 \pm 20.6$
<b>TOTAL</b>	<b><math>77^{+12}_{-10}</math></b>	<b><math>185^{+25}_{-22}</math></b>

# NCD Simulation Results

## ■ model:

- alpha energy loss
- alpha energy straggling
- alpha multiple scattering
- electron-ion pair generation
- electron drift, diffusion
- electron multiple scattering
- ion mobility
- electron avalanche
- space charge
- signal generation
- propagation through electronics

## ■ from calibration data:

- Po/Bu ratio
- energy scale
- energy resolution
- alpha depth
- contributions from different parts of the NCD

neutron signal

surface polonium decay

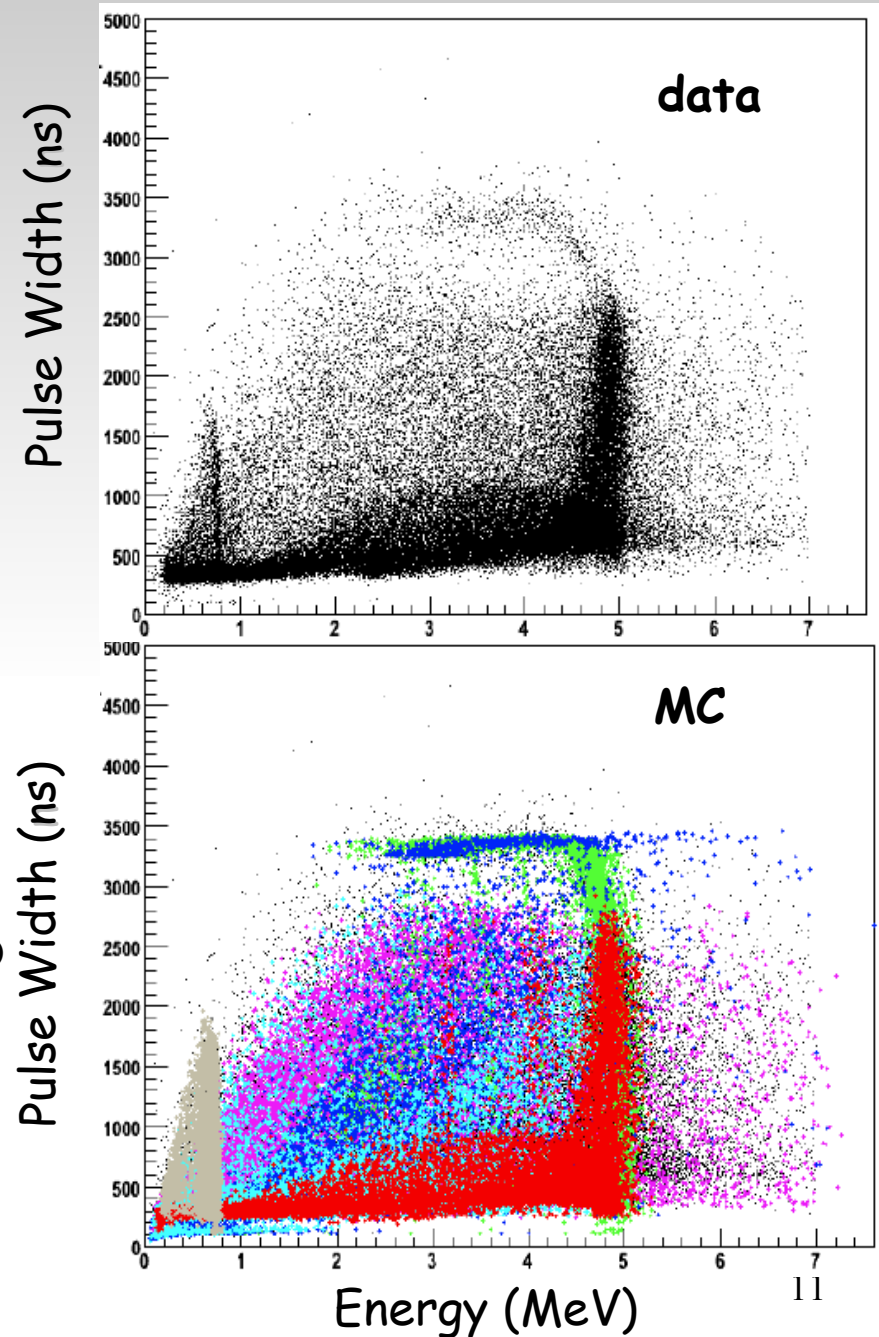
bulk U and Th decay

wire polonium decay

wire bulk decay

insulator polonium decay

insulator bulk U and Th decay

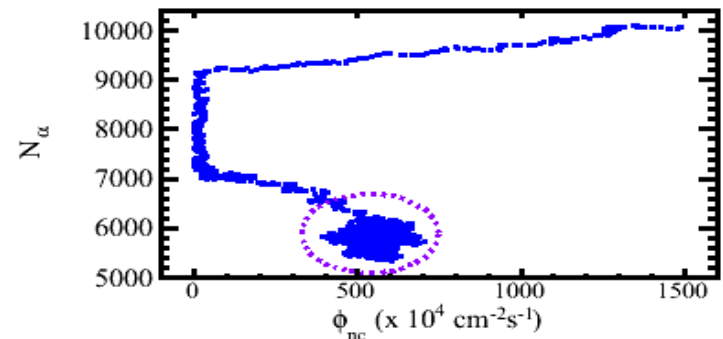
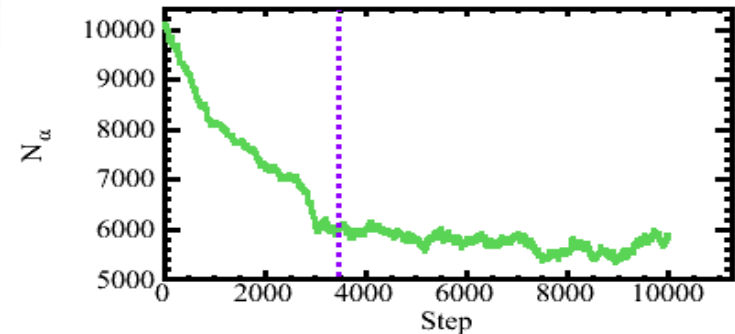
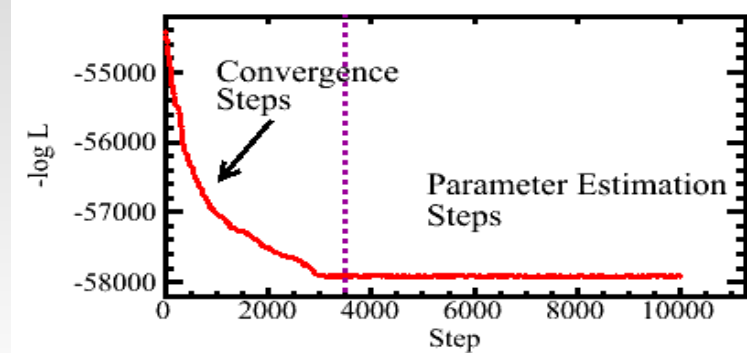
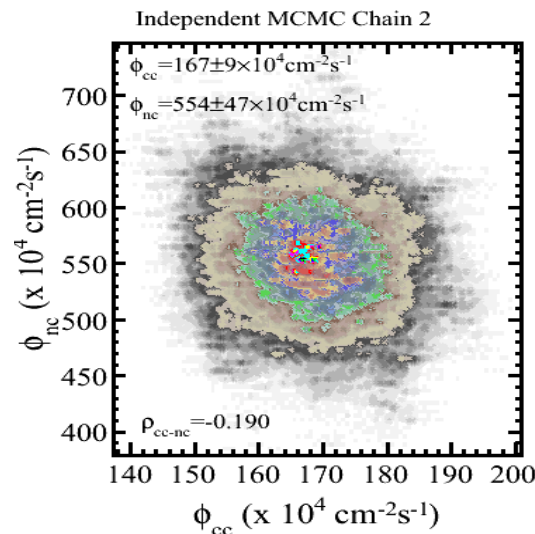
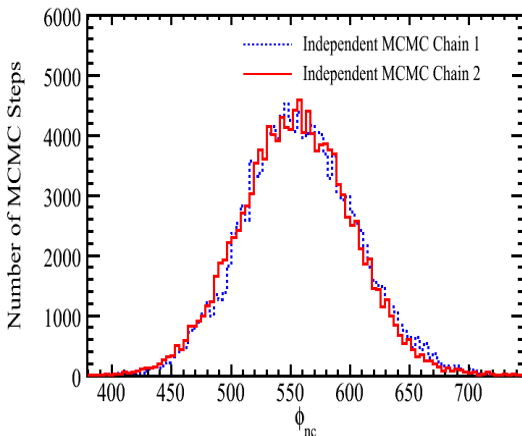


# Markov-Chain Monte Carlo: A random walk that samples parameter space with probabilities $\propto$ the likelihood function

- Float 27 Flux parameters ( $\phi_{\text{NC}}, \phi_{\text{CC1...13}}, \phi_{\text{ES1...13}}$ ) and 35 Systematic uncertainty parameters (efficiency, MC input, scale/resol, n backgrounds,...)
- Results are posterior distributions and correlations between all of the fit parameters
- Convergence check by comparing posterior

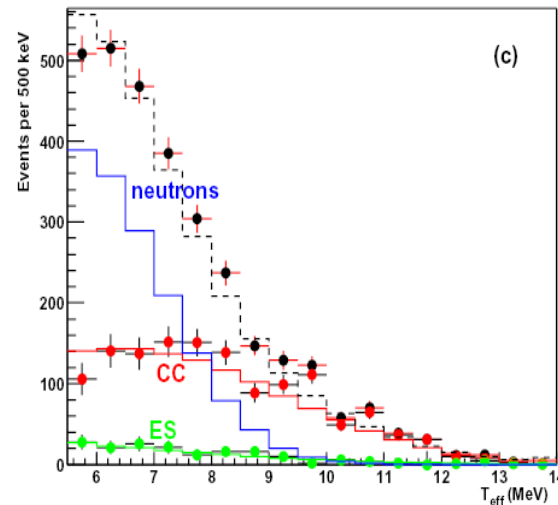
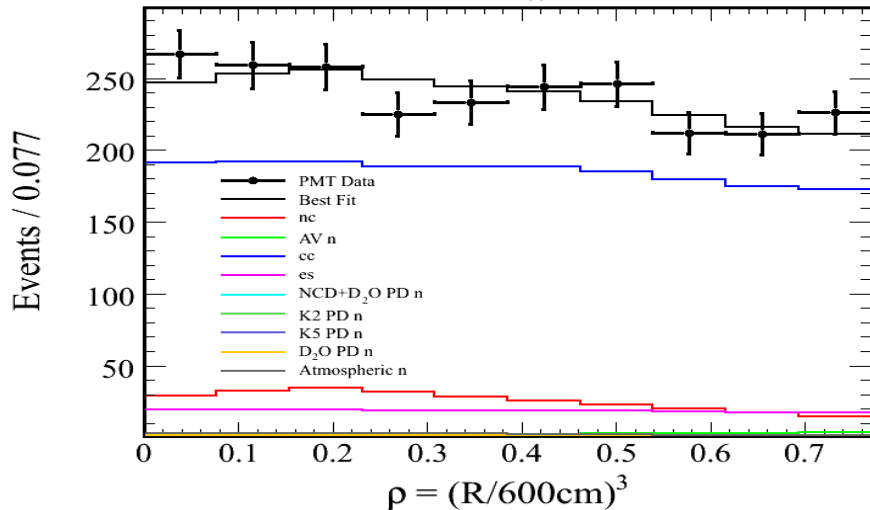
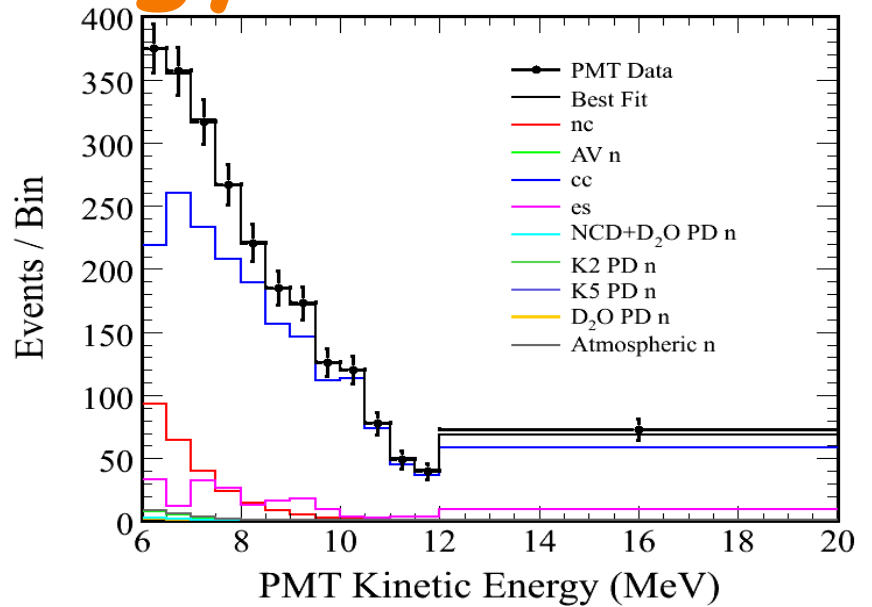
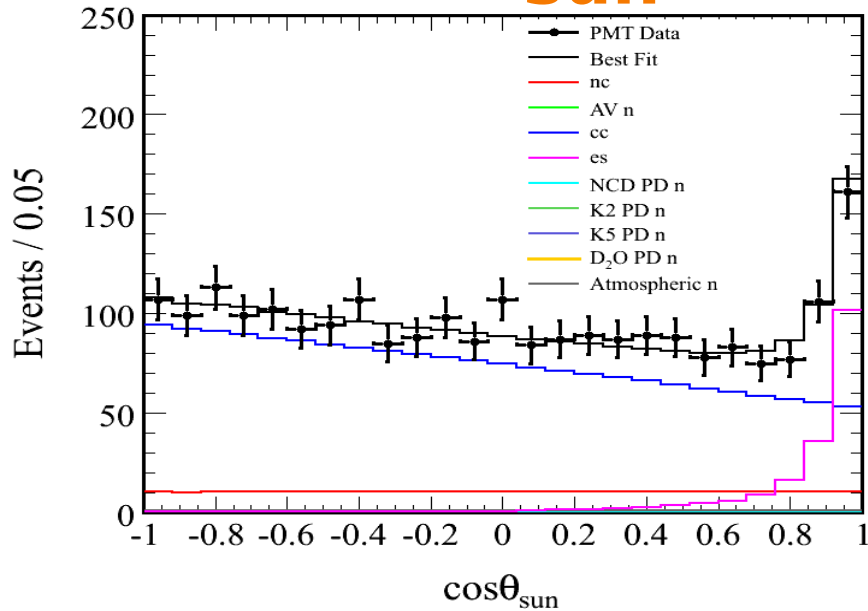
$$\phi_{\text{nc}}^{\text{chain1}} = 555 \pm 47 \times 10^4 \text{ cm}^{-2} \text{ s}^{-1}$$

$$\phi_{\text{nc}}^{\text{chain2}} = 554 \pm 47 \times 10^4 \text{ cm}^{-2} \text{ s}^{-1}$$



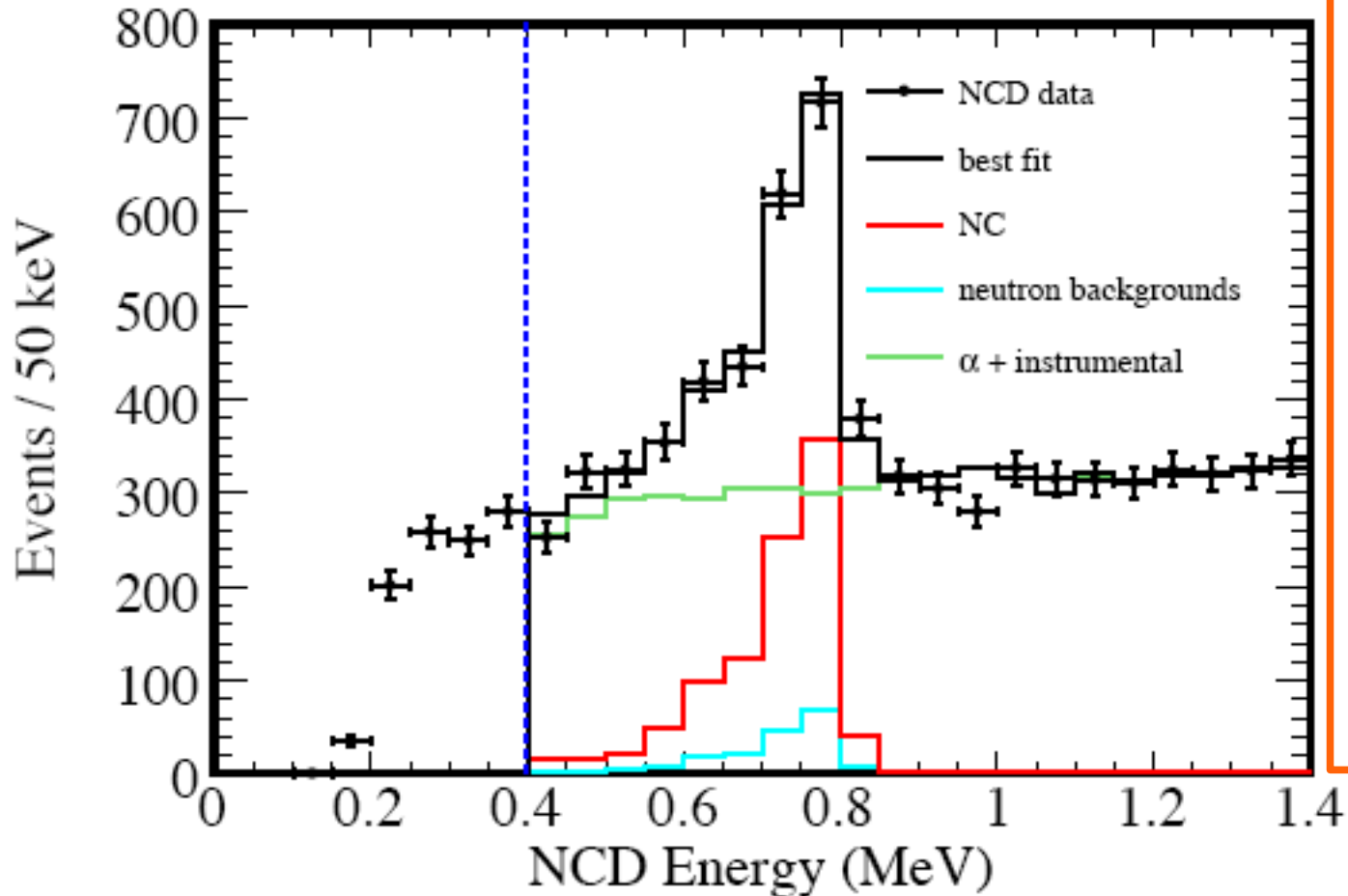
# Fit PMT Distributions :

## $\cos(\theta_{\text{sun}})$ , Energy, Radius



Data from salt phase

# Neutrons from solar neutrino interactions

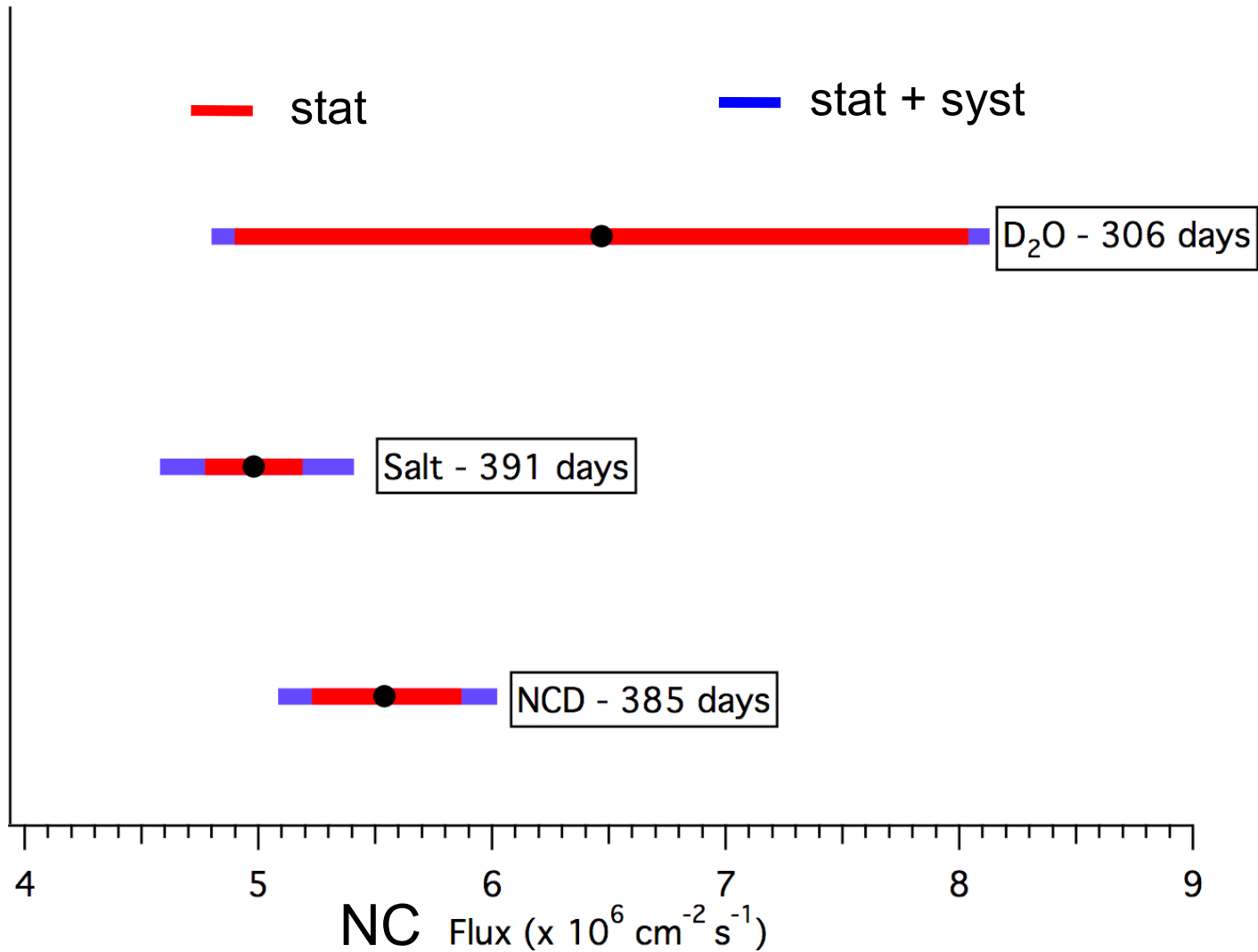


NC Signal:  
 $983 \pm 77$

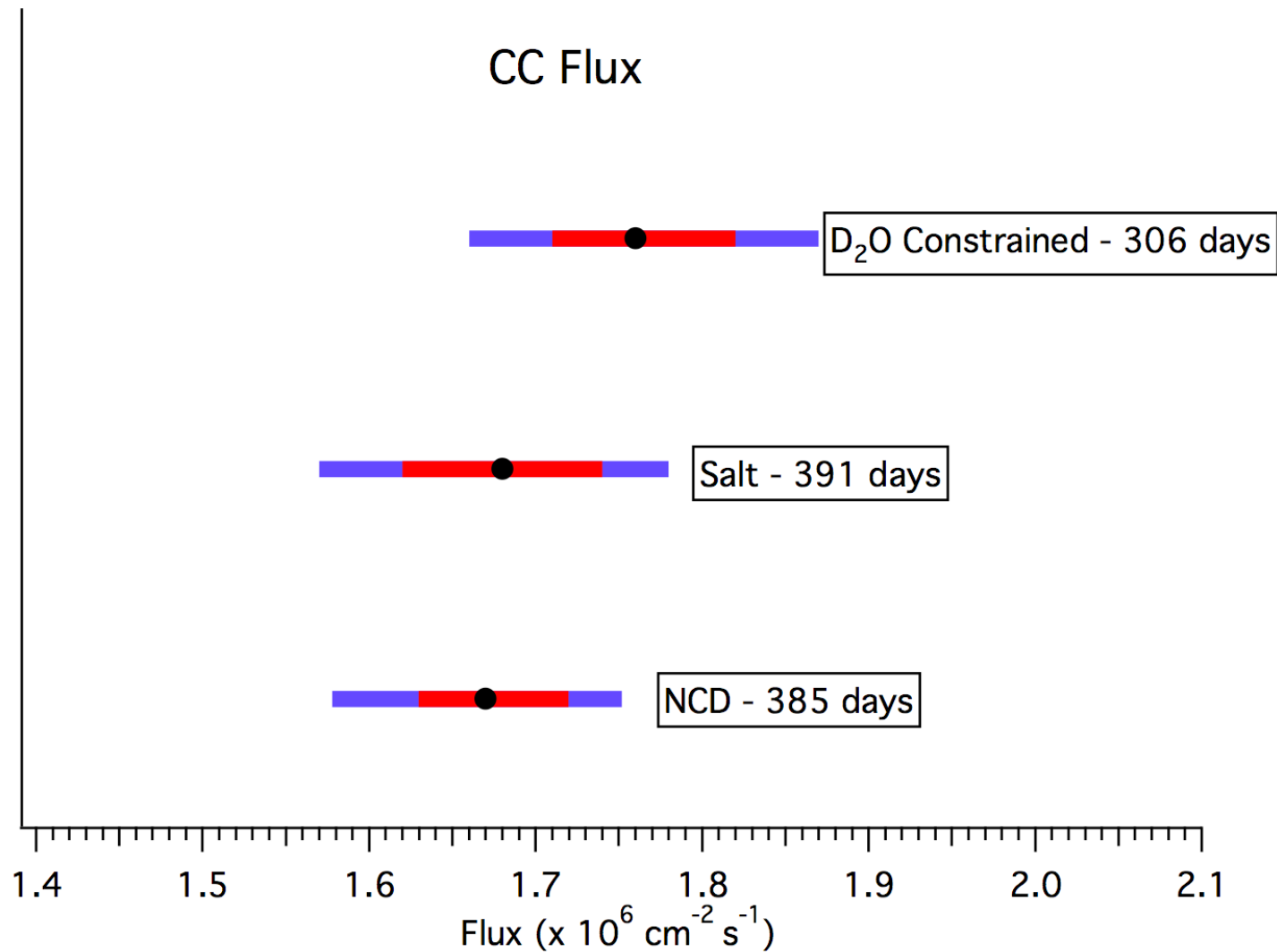
Neutron  
background:  
 $185 \pm 25$

Alphas and  
Instrumentals:  
 $6126 \pm 250$   
(0.4 to 1.4 MeV)

# SNO NC Flux: 3 Phases



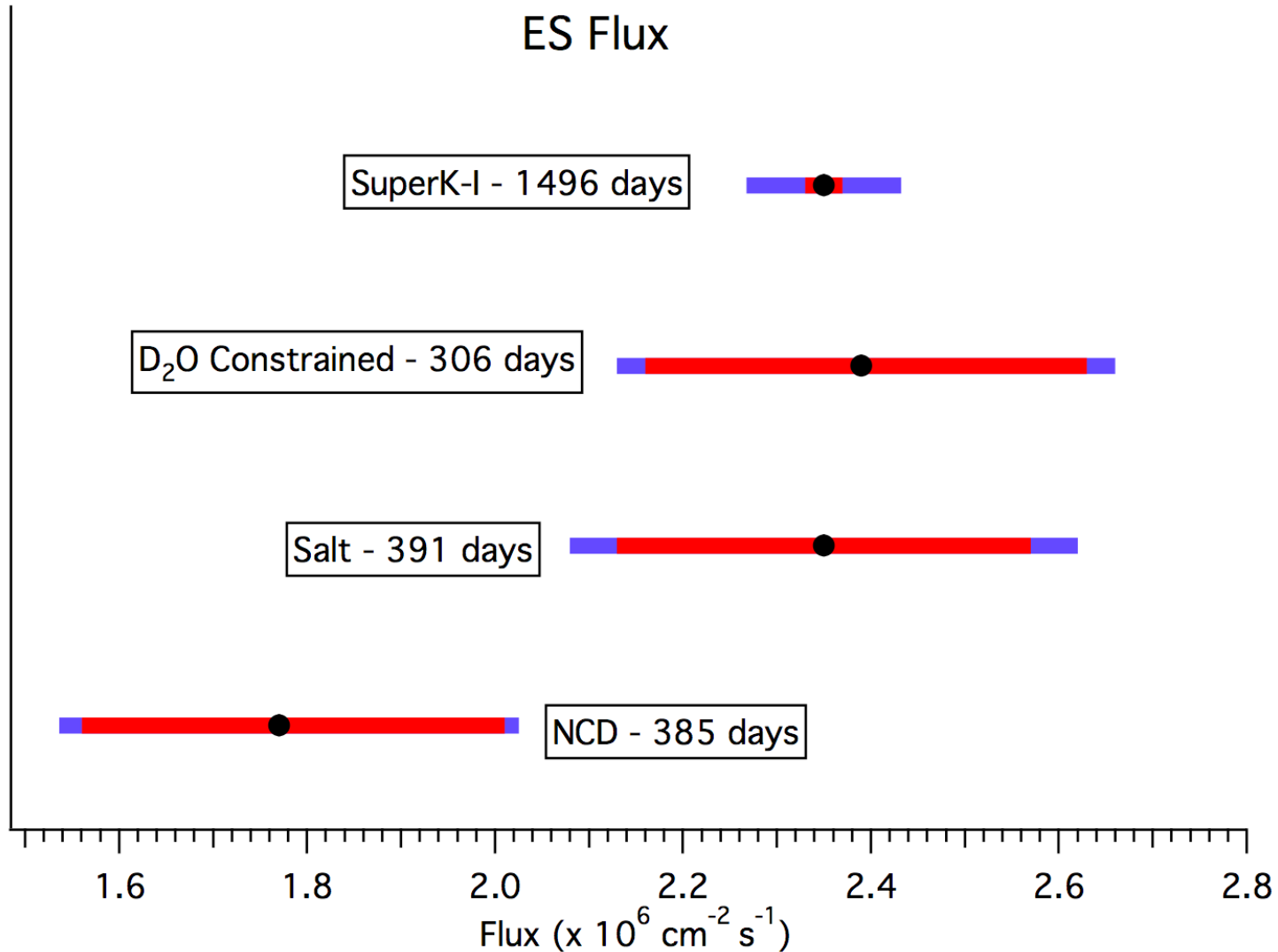
# SNO CC Flux: 3 Phases





# SNO, S-K ES Flux

p-value for consistency of NC/CC/ES  
in the salt & NCD phases + D<sub>2</sub>O  
NC(unconstr) is 32.8%



# Results for SNO NCD Phase & Super-K

Preliminary

Fluxes

( $10^4 \text{ cm}^{-2} \text{ s}^{-1}$ )

$\nu_e$ : 167(9)

$\nu_{ES}$ : 177(26)

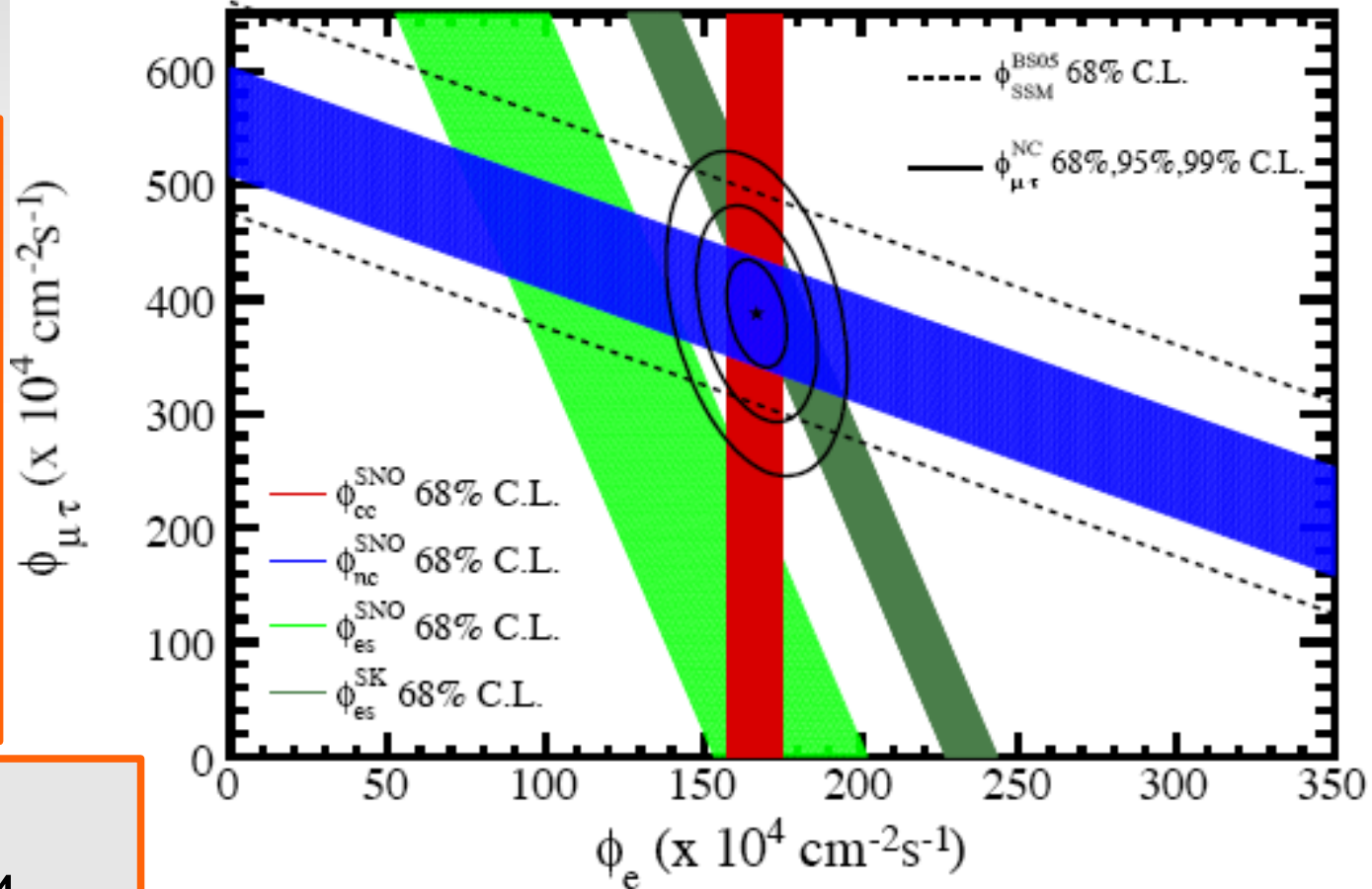
$\nu_{\text{total}}$ : 554(48)

$\nu_{SSM}$ : **569(91)**

$$\phi_{CC} = \nu_e$$

$$\phi_{ES} = \nu_e + 0.154 \nu_{\mu\tau}$$

$$\phi_{NC} = \nu_e + \nu_{\mu\tau}$$



$$\phi_{SSM} = 569(1 \pm 0.16) \times 10^4 \text{ cm}^{-2} \text{ s}^{-1}$$

(BSB05-OP: Bahcall, Serenelli, Basu  
Ap. J. 621, L85, 2005).

Super-K: PRD 73, 112001, 2006

# 2-Neutrino Oscillation Contours

2-neutrino mixing model.  
Marginalized 1- $\sigma$  unc.  
All SNO phases.

KamLAND: PRL 94, 081801 (2005).

$$\sin^2 \theta_{12} \sim \frac{\phi_{CC}}{\phi_{NC}} = 0.301 \pm 0.033 (tot)$$

$$\Delta m^2 = 7.94^{+0.42}_{-0.26} \times 10^{-5} \text{ eV}^2$$

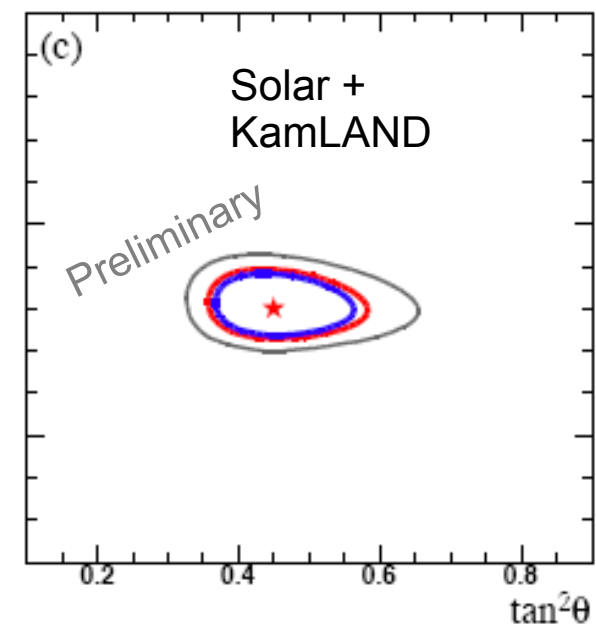
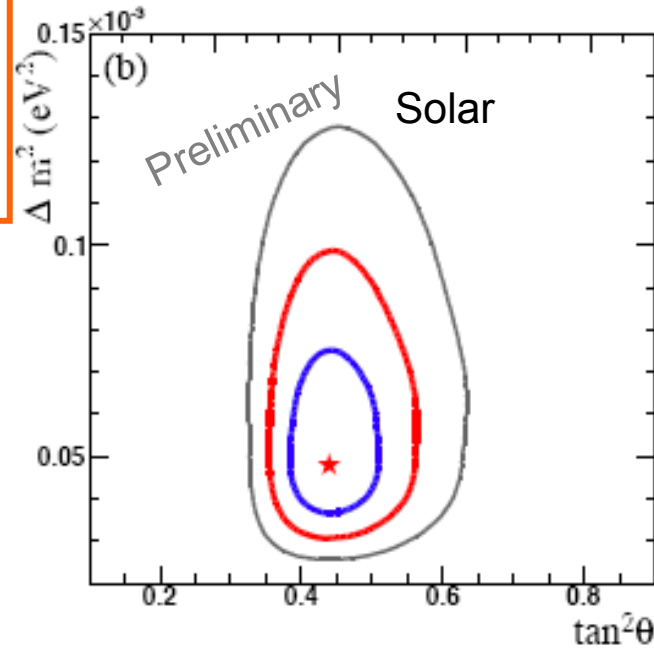
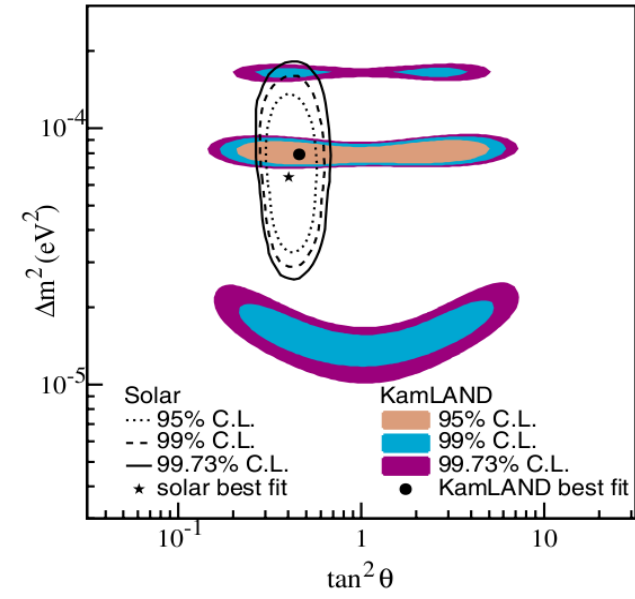
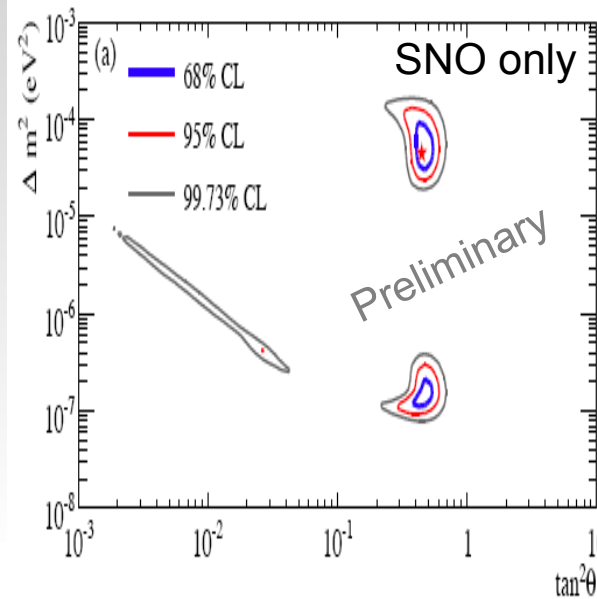
$$\tan^2 \theta = 0.447^{+0.047}_{-0.043}$$

$$\theta = 33.8^{+1.4}_{-1.3} \text{ degrees}$$

$$f_{8B} = 0.873 f_{8B(BSB05-OP)}$$

Cl-Ar  
Super-K  
SAGE  
Gallex  
GNO  
SNO  
Borexino

766 t-y KamLAND



# SNO Collaboration



# SNO gratefully acknowledges...

## Canada:

Natural Sciences and Engineering Research Council  
Industry Canada  
National Research Council  
Northern Ontario Heritage Fund  
Vale Inco  
Atomic Energy of Canada, Ltd.  
Ontario Power Generation  
High Performance Computing Virtual Laboratory  
Canada Foundation for Innovation  
Canada Research Chairs  
Westgrid

## US:

Department of Energy  
NERSC PDSF

## UK:

STFC (formerly Particle Physics and Astronomy Research Council)

## Portugal:

FCT



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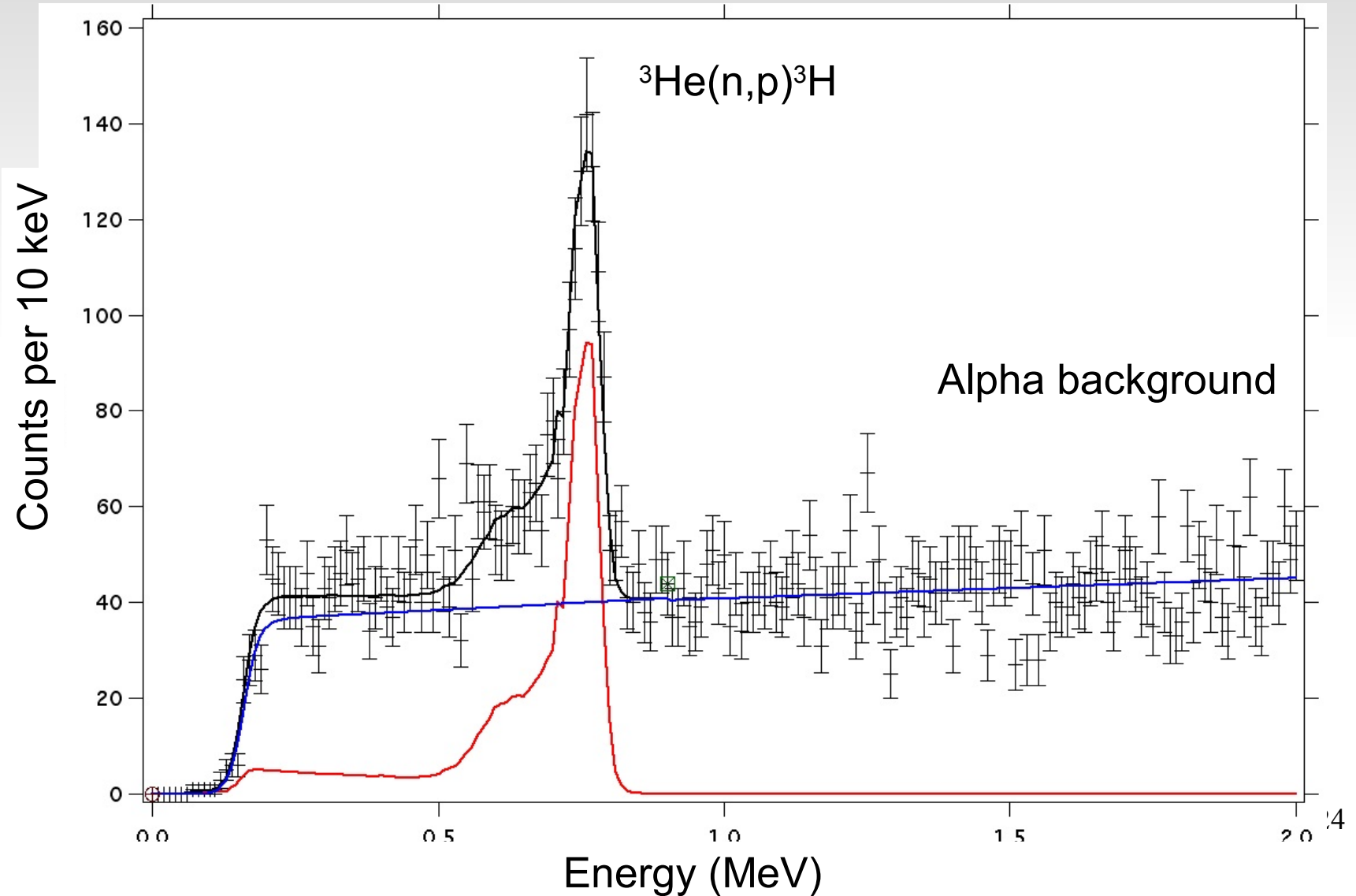
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M.W.E. Smith, T.D. Steiger, B.A. VanDevender,  
T. Van Wechel, B.L. Wall, J.E. Wilkerson



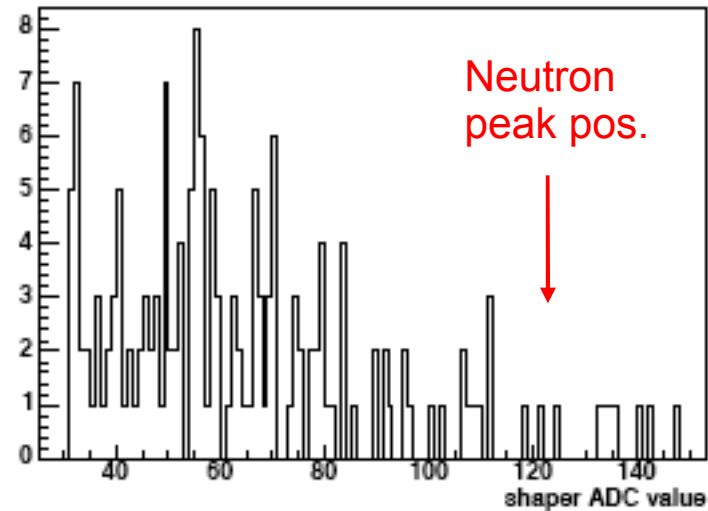
# Neutron-capture spectrum (blind data)





# Instrumental Events

Energy spectra of 2 strings showed instrumental events that could not be completely cut from neutron/alpha events.



These strings were dropped and PDFs were added in the analysis to allow for such events to be present on other strings.

# 391 - day salt results

$$\varphi_{CC} = 1.68^{+0.06}_{-0.06} (\text{stat.})^{+0.08}_{-0.09} (\text{syst.})$$

$$\varphi_{NC} = 4.94^{+0.21}_{-0.21} (\text{stat.})^{+0.38}_{-0.34} (\text{syst.})$$

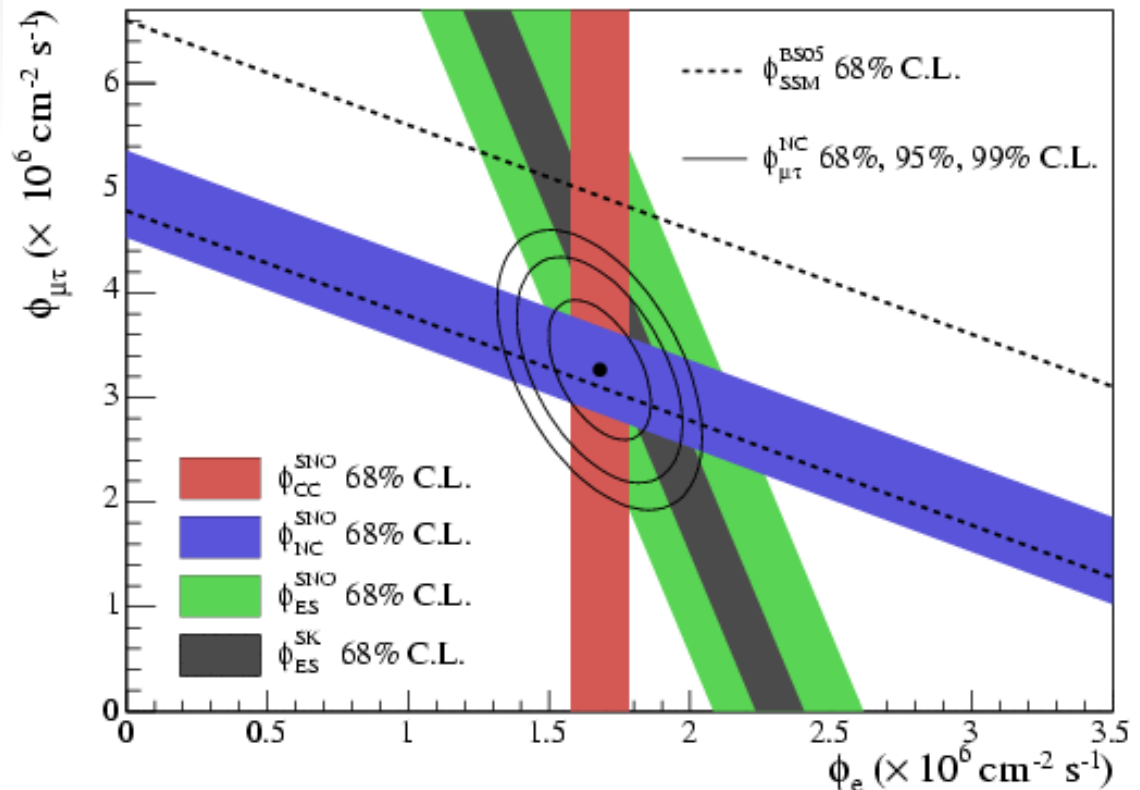
$$\varphi_{ES} = 2.35^{+0.22}_{-0.22} (\text{stat.})^{+0.15}_{-0.15} (\text{syst.})$$

$$\frac{\varphi_{CC}}{\varphi_{NC}} = 0.34 \pm 0.023 (\text{stat.})^{+0.029}_{-0.023}$$

In units of  $10^{-6} \text{ cm}^{-2} \text{ s}^{-1}$

$$\Delta m^2 = 8.0^{+0.4}_{-0.3} \times 10^{-5} \text{ eV}^2$$

$$\theta = 33.9^{+1.6}_{-1.6} \text{ deg}$$

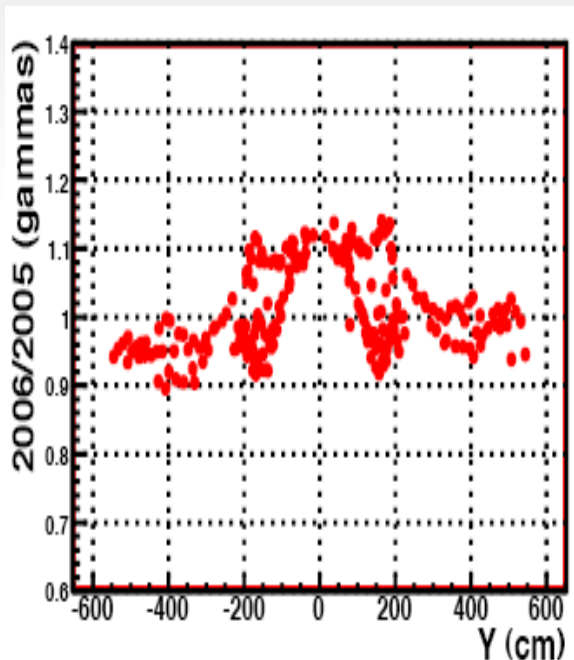


# Calibrating the Neutron Efficiency

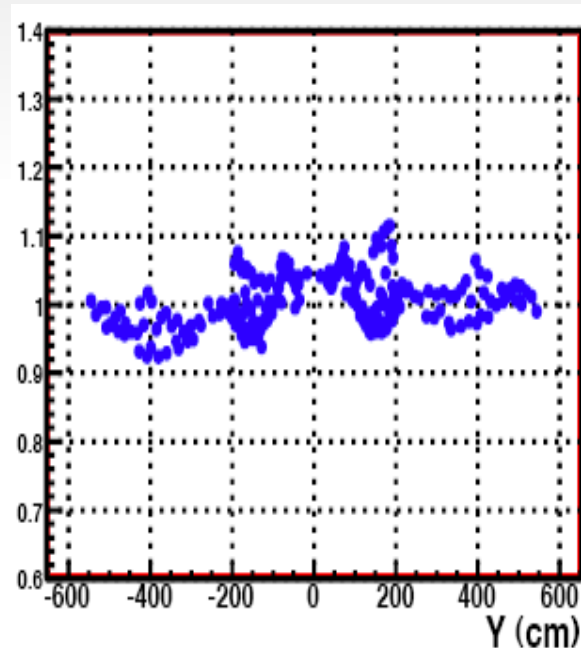
- Mixing  $^{24}\text{NaCl}$  with the  $\text{D}_2\text{O}$ .

Normalized ratio of Cherenkov light at many points in vessel: 2006 data/ 2005 data.  
Different brine injection methods. Equalized ratio indicates uniform mixing.

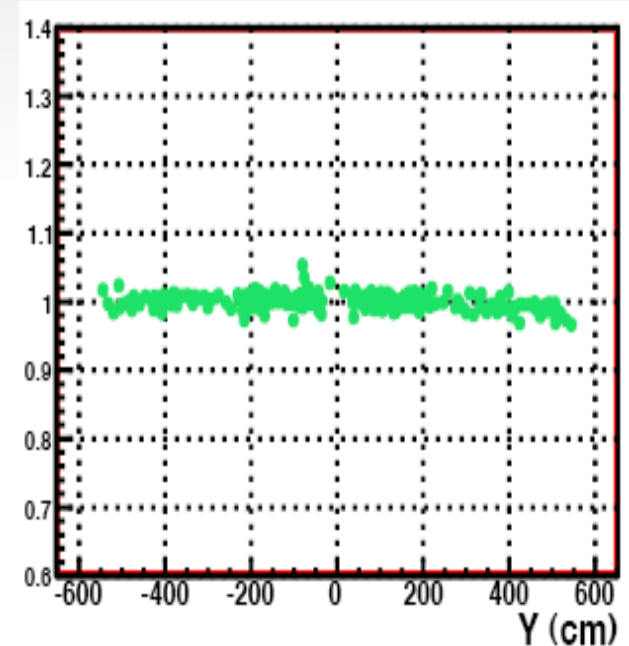
First day after injection



During mixing



Steady state



Neutron efficiency: 0.211(7) for NC signal.

Excellent agreement with Monte Carlo: 0.210(3)

# Signal Extraction - Extended

## Maximum Likelihood Fit for Fluxes

- maximize likelihood,  $N$  event measurements ( $x_1, \dots, x_n$ ), pars ( $a_1, \dots, a_k$ ):

$$L(\vec{x}|\vec{a}) = \frac{e^{-\nu} \nu^N}{N!} \prod_{i=1}^N P(\vec{x}_i|\vec{a}) \prod_{k=1}^K \text{Gaus}(a_k, \mu_k, \sigma_k)$$

Poisson probability of observing  $N$  events

Standard maximum likelihood

Constraints on systematics from calibration data

- minimize  $-\log L$ :  $\log L(\vec{x}|\vec{a}) = -\nu(\vec{a}) + \sum_{i=1}^N \log \nu(\vec{a}) P(\vec{x}_i|\vec{a}) - 0.5 \sum_{k=1}^K [(a_k - \mu_k)/\sigma_k]^2$
- $\nu$  = predicted # of event,  $P$  = probability density function (PDF)
- In SNO we have  $M$  event types ( $j=CC, ES, NC, \dots$ ) so:
  - $\log L(\vec{x}|\vec{a}) = -\sum_{j=1}^M f_j(\vec{a}) \phi_j(\vec{a}) + \sum_{i=1}^M \log \sum_{j=1}^N f_j(\vec{a}) \phi_j(\vec{a}) P_j(\vec{x}_i|\vec{a}) + \text{constraints}$
- where  $\phi$  is a flux and  $f$  is a conversion factor from flux to events

# Joint PMT + NCD fit

- For the NCD phase, NCD and PMT NC flux is common, as are neutron backgrounds
- Just add  $-\log L$  from the two measurements, using common flux parameter:

$$\begin{aligned} \log L(\vec{x}|\vec{a}) = & - \sum_{j=1}^{M^{PMT}} f_j^{PMT}(\vec{a}) \phi_j(\vec{a}) + \sum_{i=1}^{M^{PMT}} \log \sum_{j=1}^{N^{PMT}} f_j^{PMT}(\vec{a}) \phi_j(\vec{a}) P_j(\vec{x}_i^{PMT}|\vec{a}) \\ & - \sum_{j=1}^{M^{NCD}} f_j^{NCD}(\vec{a}) \phi_j(\vec{a}) + \sum_{i=1}^{M^{NCD}} \log \sum_{j=1}^{N^{NCD}} f_j^{NCD}(\vec{a}) \phi_j(\vec{a}) Q_j(\vec{x}_i^{NCD}|\vec{a}) \end{aligned}$$

- $f$  are conversion from flux to number of events, and  $\phi$  are fluxes

# Systematic Uncertainties

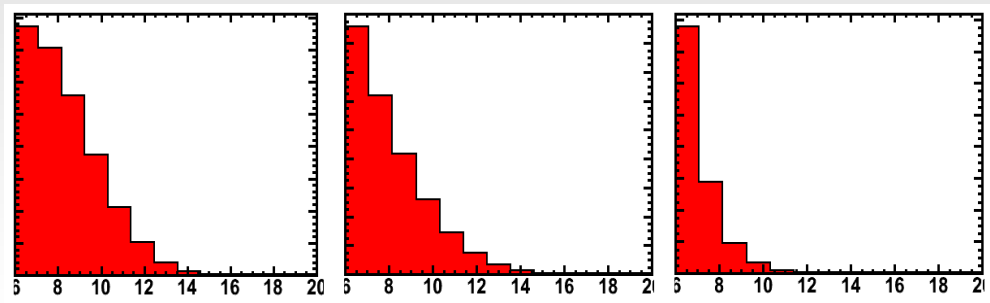
TABLE II: Sources of systematic uncertainties on NC, CC, and ES fluxes. The total error differs from the individual errors added in quadrature due to correlations.

Nuisance Parameter	NC uncert. (%)	CC uncert. (%)	ES uncert. (%)
PMT energy scale	$\pm 0.6$	$\pm 2.7$	$\pm 3.6$
PMT energy resolution	$\pm 0.1$	$\pm 0.1$	$\pm 0.3$
PMT radial scaling	$\pm 0.1$	$\pm 2.7$	$\pm 2.7$
PMT angular resolution	$\pm 0.0$	$\pm 0.2$	$\pm 2.2$
PMT radial energy dep.	$\pm 0.0$	$\pm 0.9$	$\pm 0.9$
Background neutrons	$\pm 2.3$	$\pm 0.6$	$\pm 0.7$
Neutron capture	$\pm 3.3$	$\pm 0.4$	$\pm 0.5$
Cherenkov/AV backgrounds	$\pm 0.0$	$\pm 0.3$	$\pm 0.3$
NCD instrumentals	$\pm 1.6$	$\pm 0.2$	$\pm 0.2$
NCD energy scale	$\pm 0.5$	$\pm 0.1$	$\pm 0.1$
NCD energy resolution	$\pm 2.7$	$\pm 0.3$	$\pm 0.3$
NCD alpha systematics	$\pm 2.7$	$\pm 0.3$	$\pm 0.4$
PMT data cleaning	$\pm 0.0$	$\pm 0.3$	$\pm 0.3$
Total experimental uncertainty	$\pm 6.5$	$\pm 4.0$	$\pm 4.9$
Cross section <a href="#">[16]</a>	$\pm 1.1$	$\pm 1.2$	$\pm 0.5$

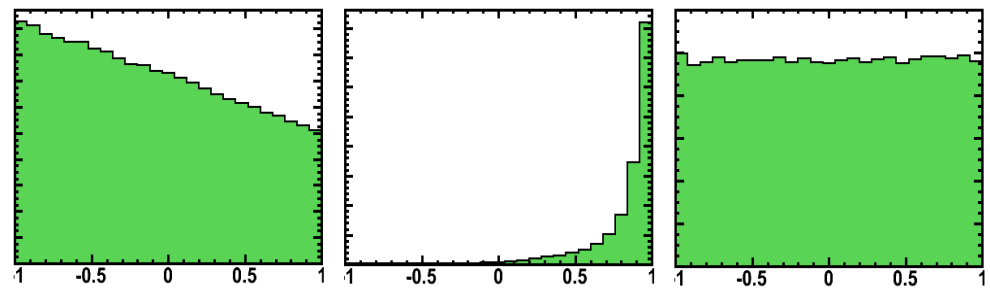
# PMT PDFs are 3D

$P_{CC}(E, R, \theta | \vec{a})$      $P_{ES}(E, R, \theta | \vec{a})$      $P_{NC}(E, R, \theta | \vec{a})$   
 CC                      ES                      NC

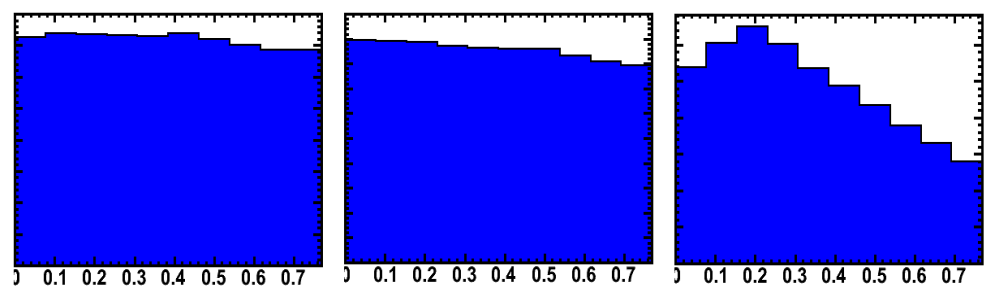
Energy



Angle

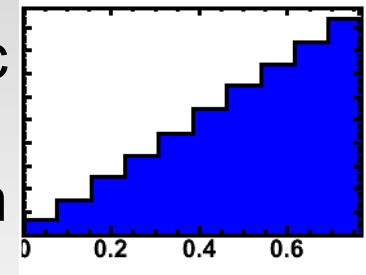


Radius

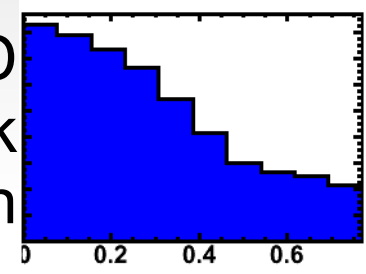


Radius

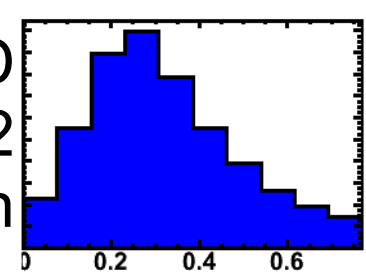
acrylic  
vessel  
neutron



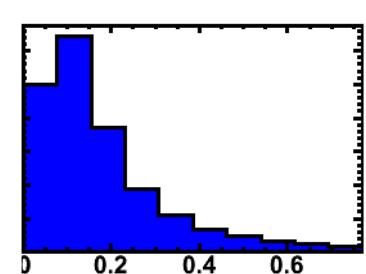
NCD  
bulk  
neutron



NCD  
K2  
neutron

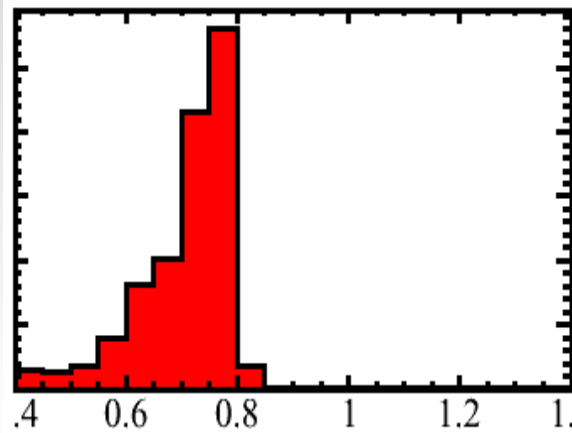


NCD  
K5  
neutron

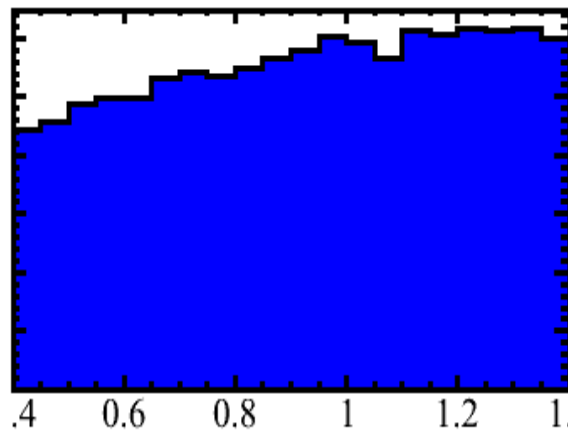


# NCD PDFs are 1D

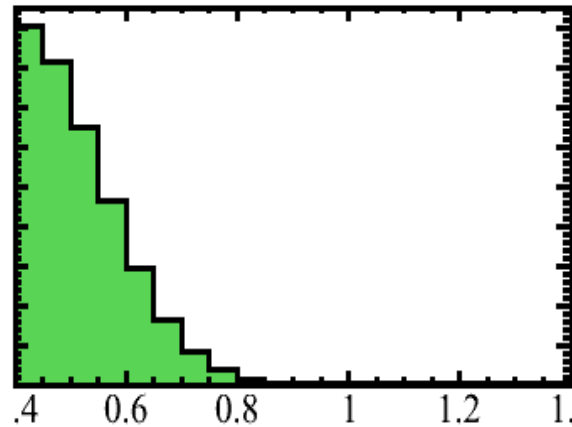
neutron  
 $Q_{NC}(E_{NCD}|\vec{a})$



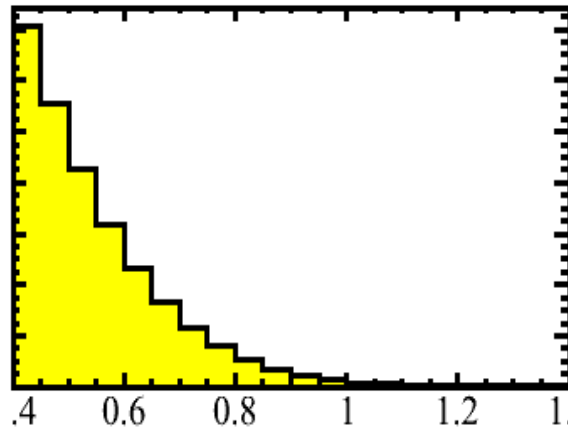
NCD  
alphas  
 $Q_{\alpha}(E_{NCD}|\vec{a})$



J3  
Instrumental  
 $Q_{J3}(E_{NCD}|\vec{a})$



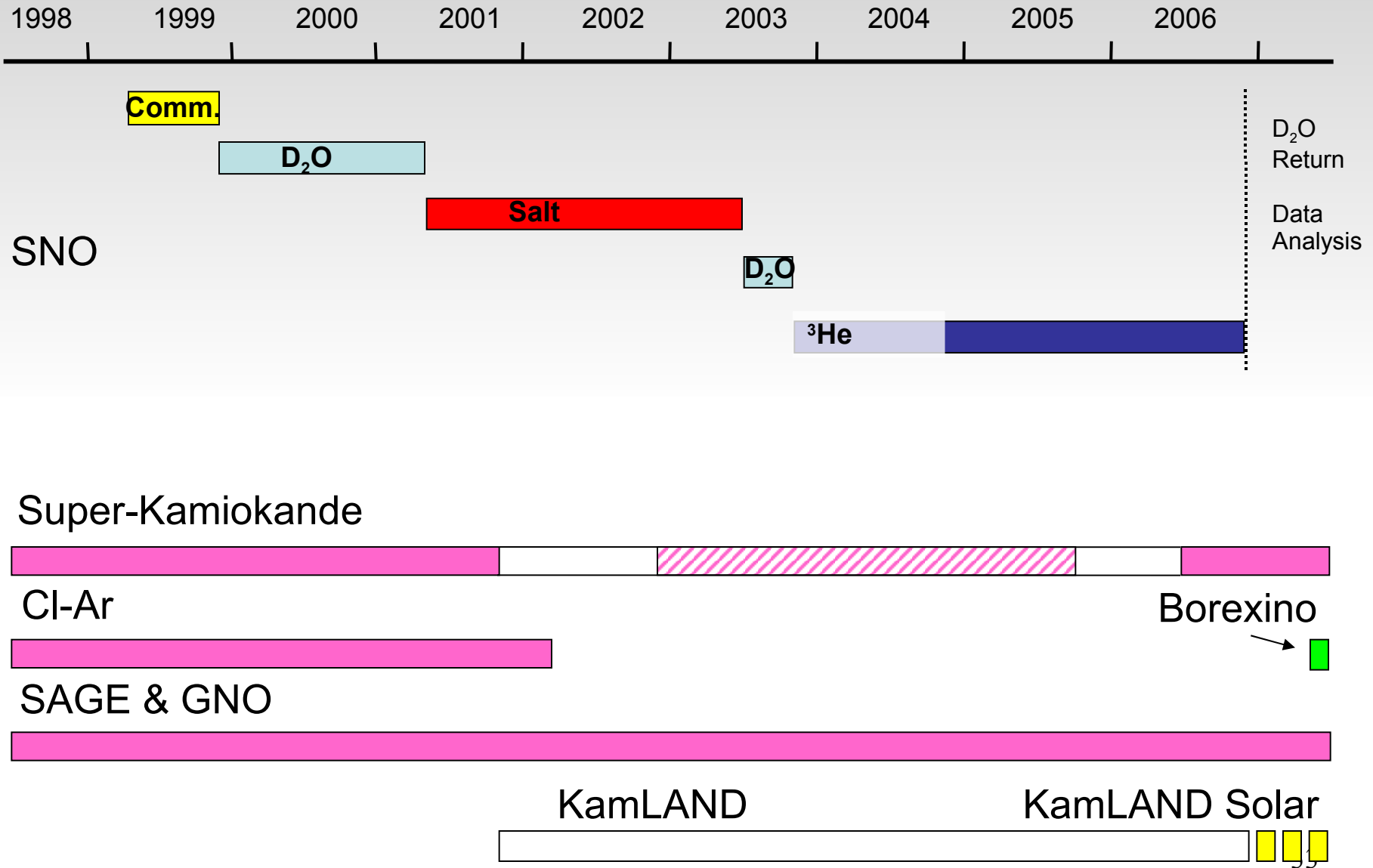
N4  
Instrumental  
 $Q_{N4}(E_{NCD}|\vec{a})$



NCD Energy (MeV)



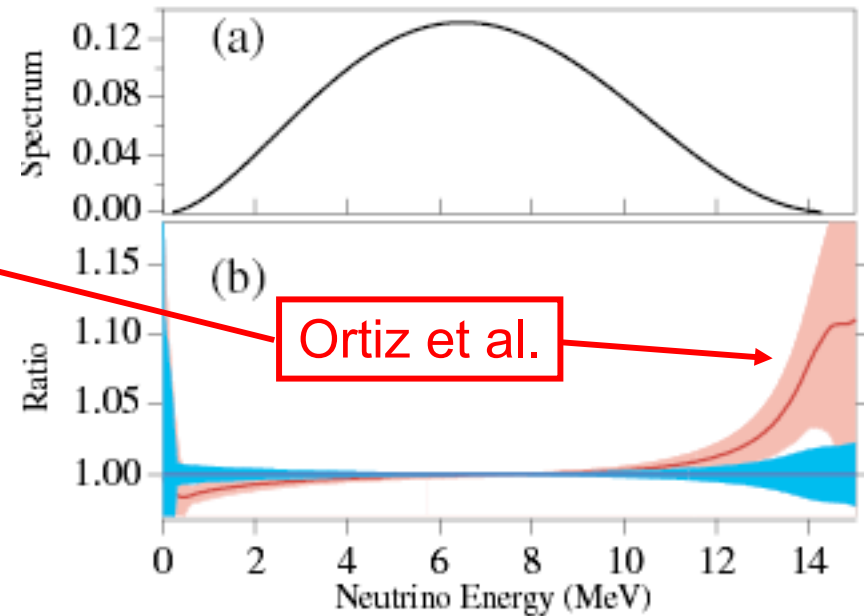
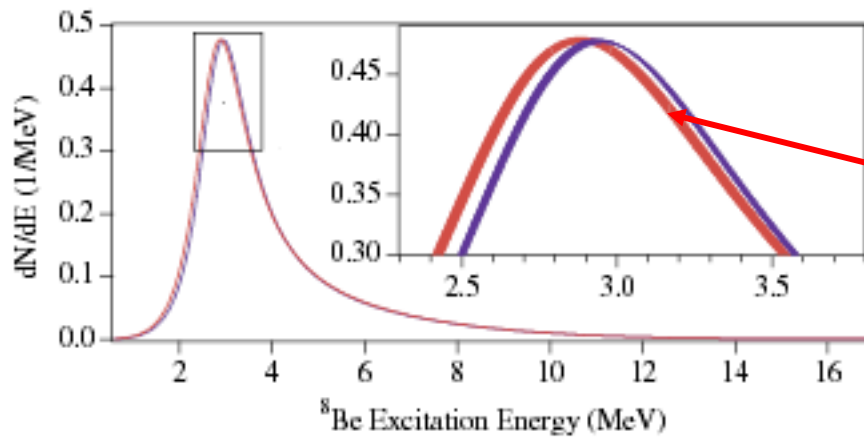
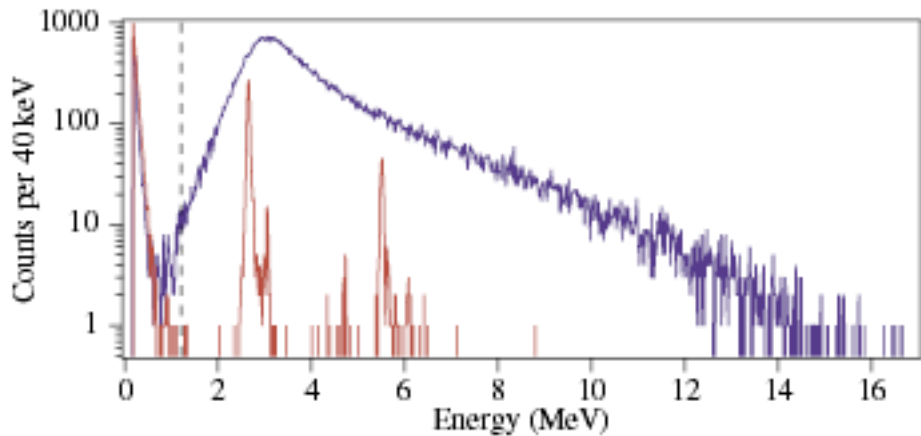
# Recent Solar Neutrino Program



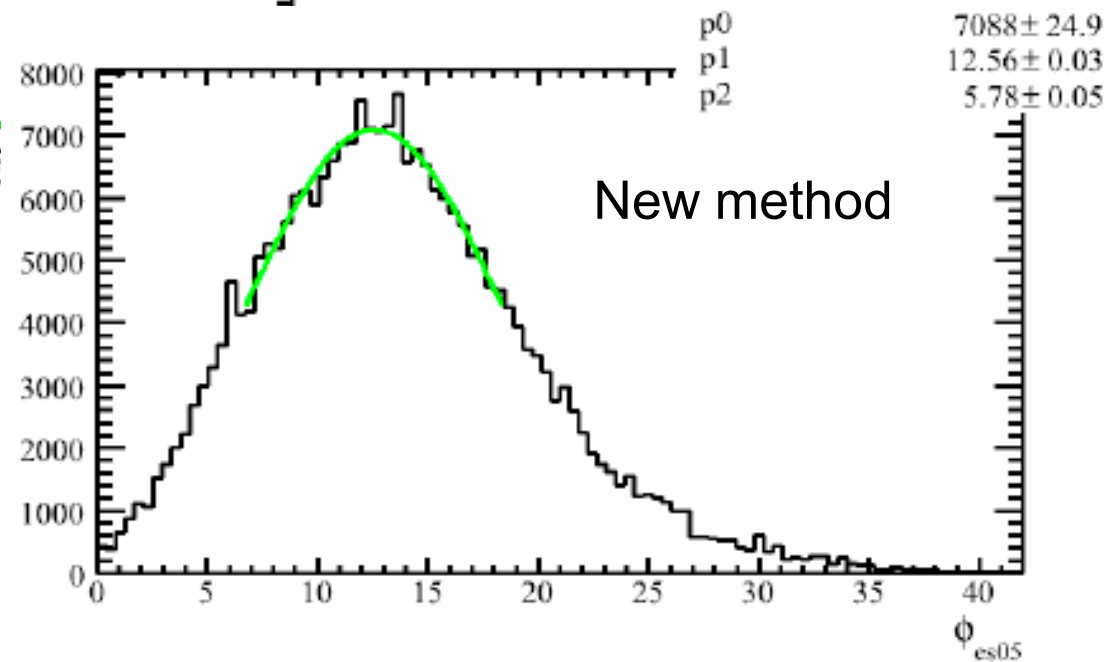
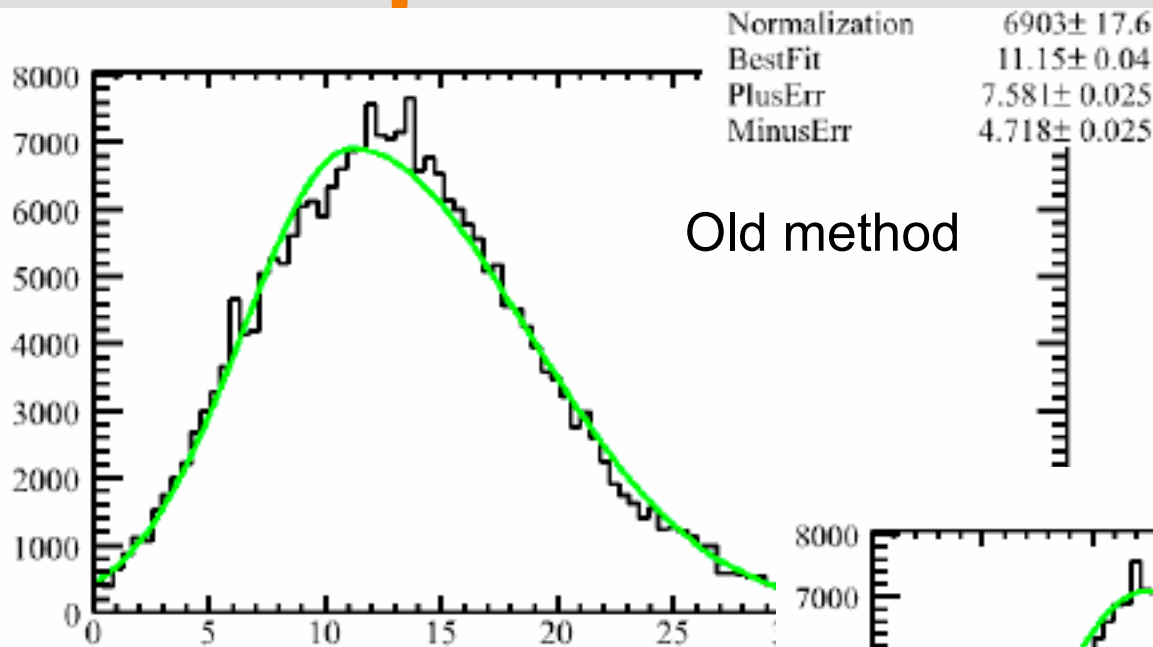
# New Measurements of ${}^8\text{B}$ $\nu$ Spectrum

Winter, Freedman, et al.  
PRL **91** 252501, NP A746,  
311 (2004).

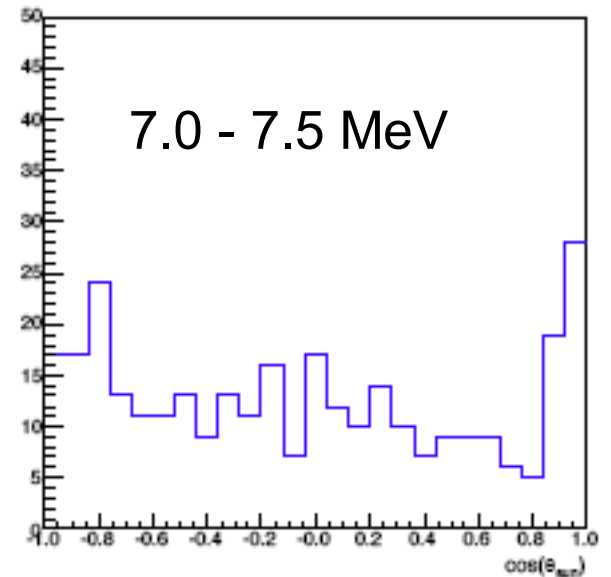
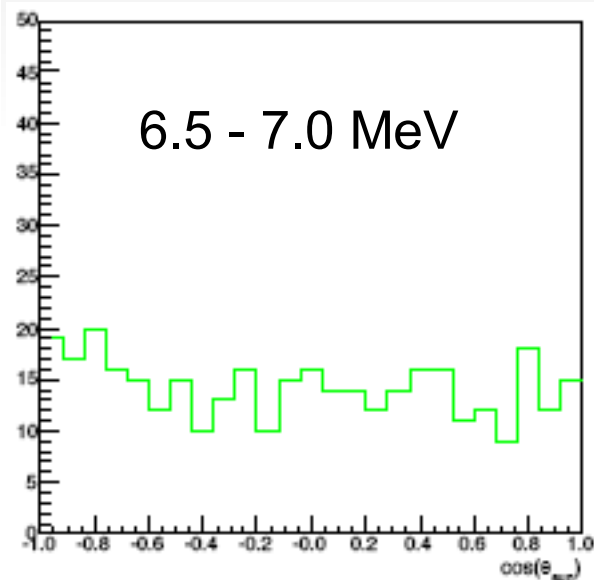
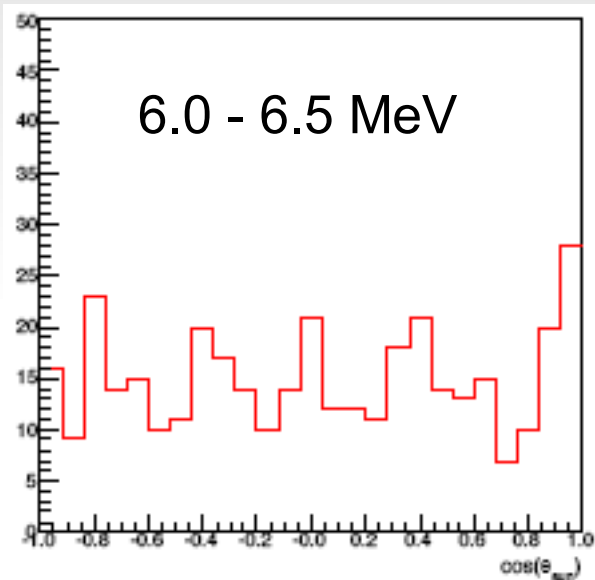
Bhattacharya et al. PRC  
**73**:055802,2006

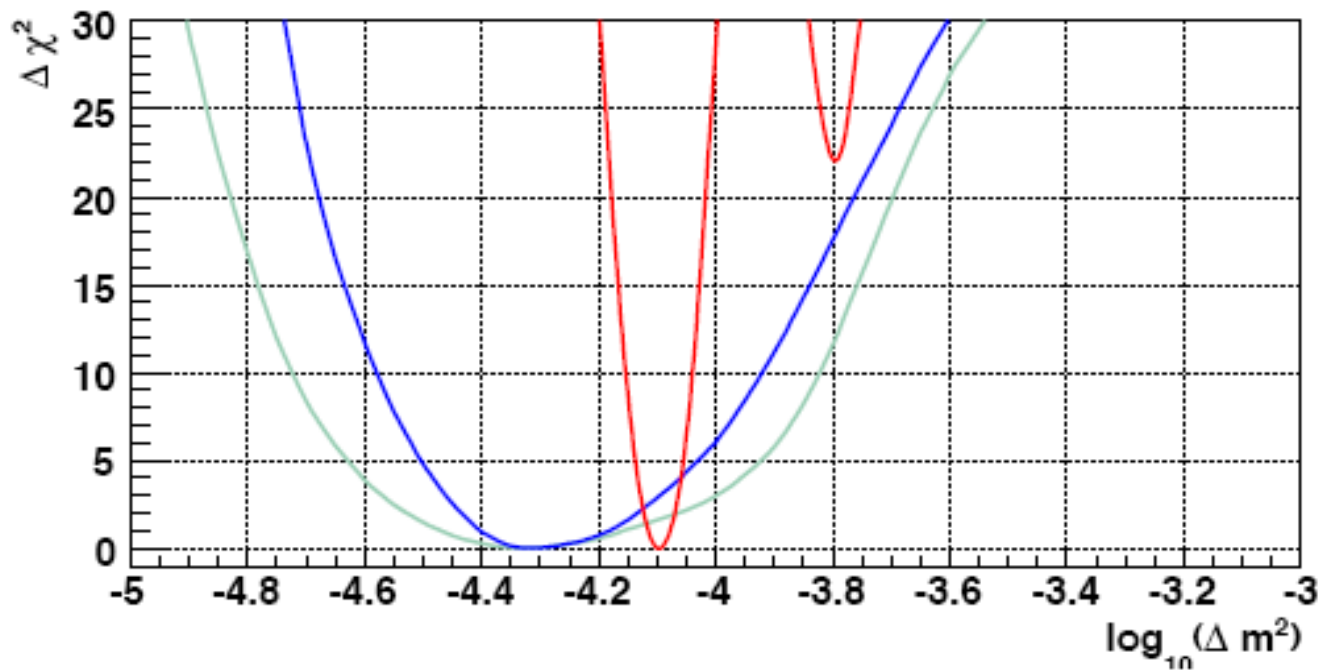
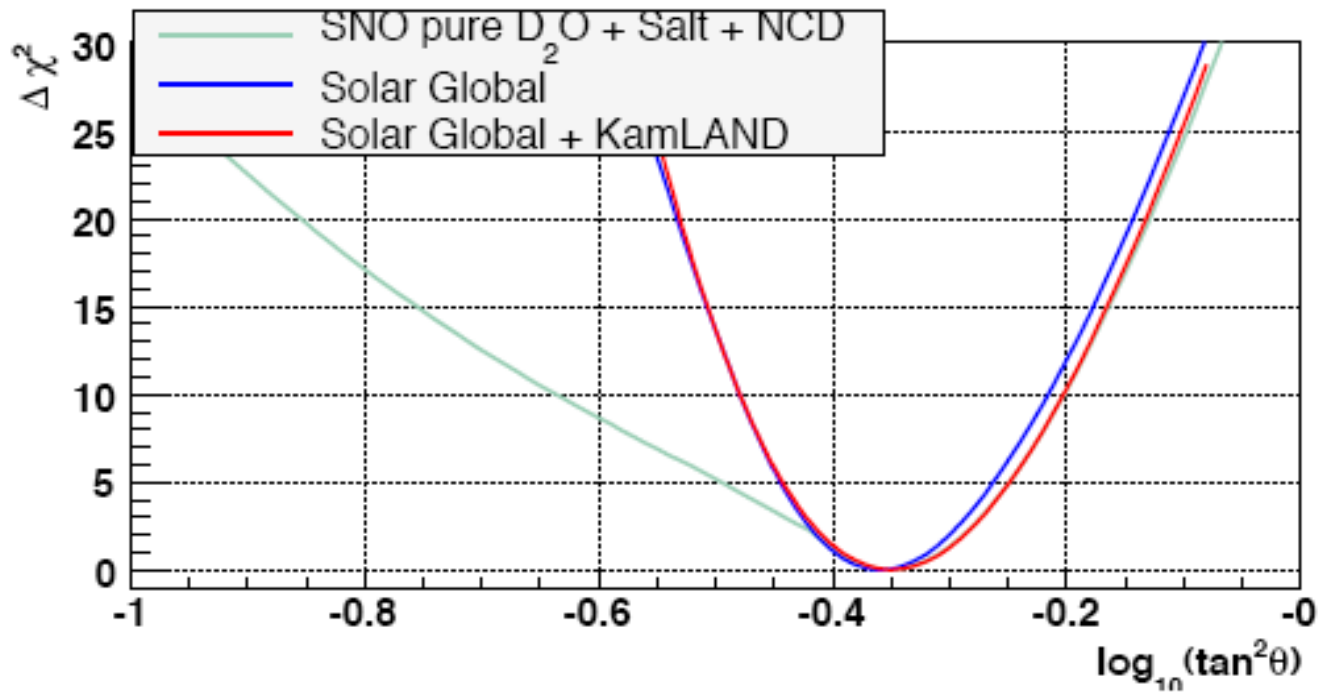


# Change in estimate of best-fit to posterior distributions

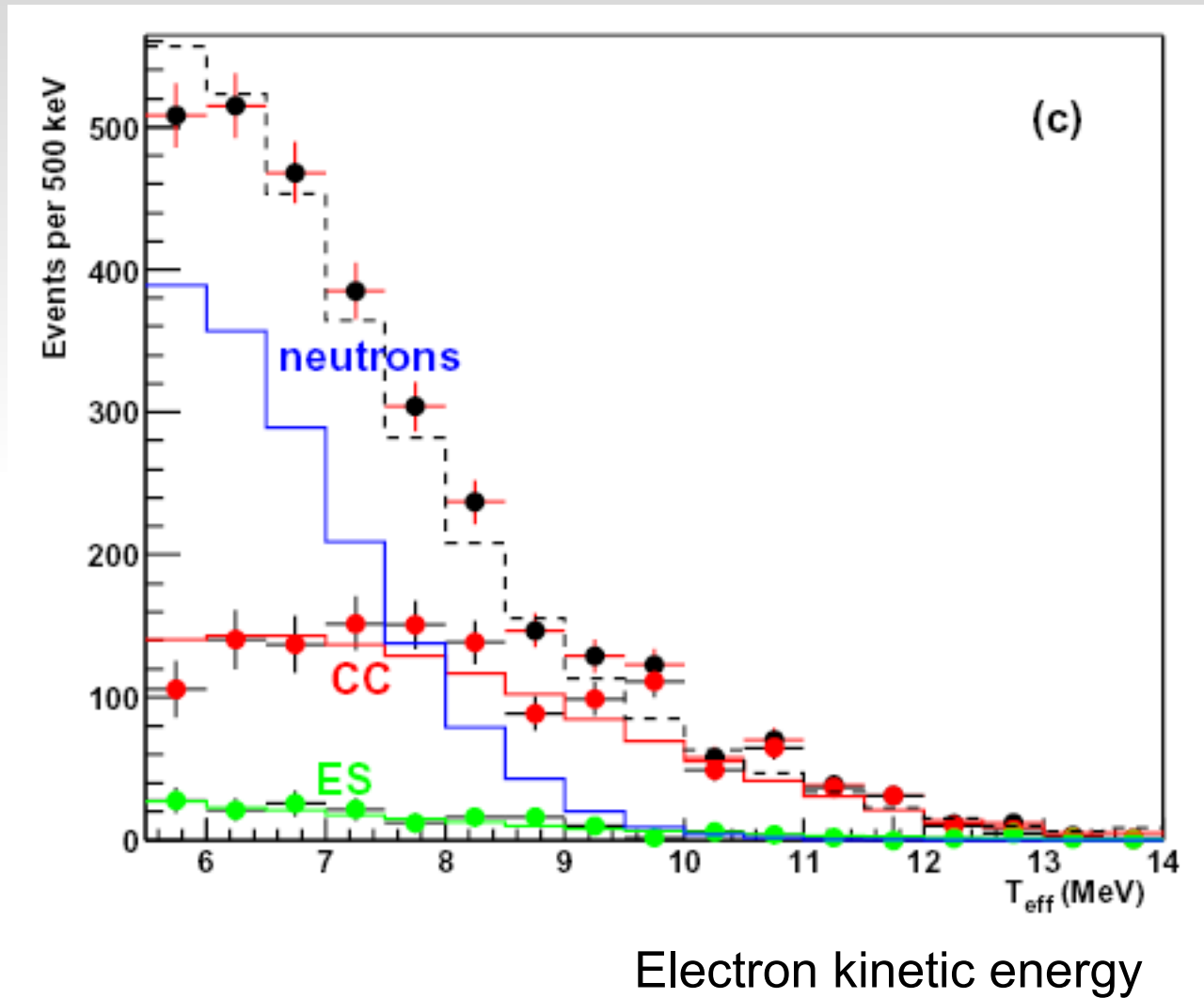


# Angular distributions for ES in 3 Energy bins

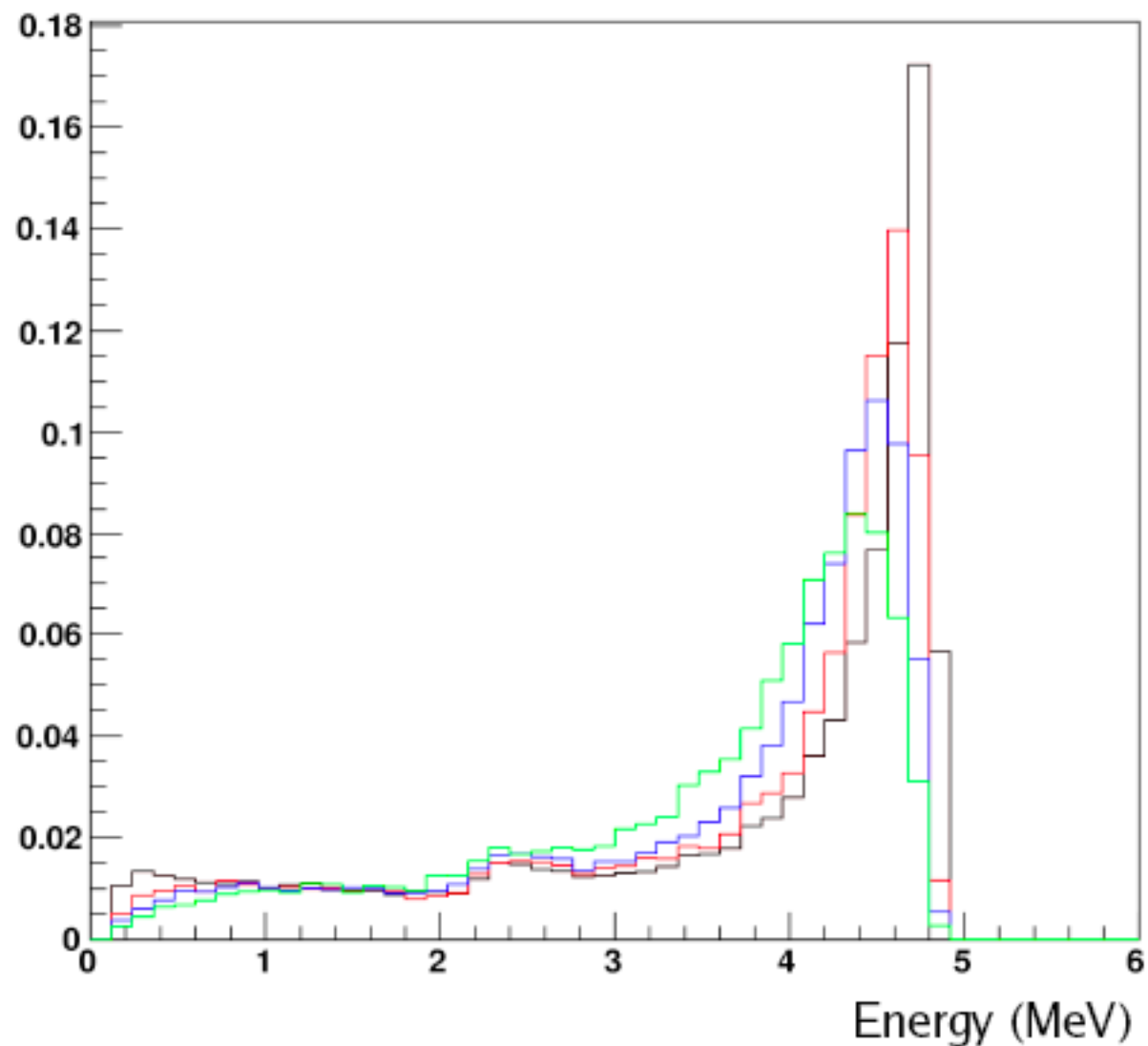




# Energy spectra, salt phase



## Energy distribution assuming an embedded Po profile



Assume exponentially decreasing  $^{210}\text{Po}$  concentration inside nickel

Black: Surface Po  
Red: 0.1 microns  
Blue: 0.25 microns  
Green: 0.5 microns

# Cutting instrumental events

