

# LBL neutrino beams and experiments

*See also arXiv:hep-ph/0106088*



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(ICARUS Collaboration)*

*Special thanks to A. Bueno, M. Campanelli & S. Navas-Concha*

**NO-VE: International Workshop on  
"Neutrino Oscillations in Venice"**

*24th-26th July, 2001*

# Three family oscillation phenomenology

*MNSP (Maki-Nagawa-Sakata-Pontecorvo) matrix:*

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{13}s_{23}e^{i\delta} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta} & c_{13}s_{23} \\ s_{12}s_{23} - c_{12}s_{13}c_{23}e^{i\delta} & -c_{12}s_{23} - s_{12}s_{13}c_{23}e^{i\delta} & c_{13}c_{23} \end{pmatrix}$$

Neutrino oscillations phenomenology determined by 6 parameters:

**3 angles  $\theta_{12}$ ,  $\theta_{13}$ ,  $\theta_{23}$**

**1 phase  $\delta$**

**2 independent  $\Delta m^2$ 's**

In addition, propagation through matter requires additional **density parameter  $\rho$**  of traversed medium (in fact, matter profile)

# The target of next generation LBL $\nu$ experiments



**Precise determination of  $\Delta m^2_{23}$  and  $\Theta_{23}$**



**Stringent limit/precise measurement of  $\Theta_{13}$**



**Determination of  $\Delta m^2_{23}$  sign**



**Study *matter effects***



**First detection of  $\nu_e \rightarrow \nu_\tau$  oscillations**



**Over-constrain the oscillation parameters (*matrix unitarity*)**



**Study the  $\delta$  phase (CP/T violation effects in the leptonic sector)**

## Looking at the $\theta_{13}$ term

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{13}s_{23}e^{i\delta} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta} & c_{13}s_{23} \\ s_{12}s_{23} - c_{12}s_{13}c_{23}e^{i\delta} & -c_{12}s_{23} - s_{12}s_{13}c_{23}e^{i\delta} & c_{13}c_{23} \end{pmatrix}$$

for  $\Delta m^2_{21} (L/4E_\nu) \ll 1$ :

$$P(\nu_e \rightarrow \nu_\mu) \approx \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2(\Delta m^2_{32} L/4E_\nu)$$

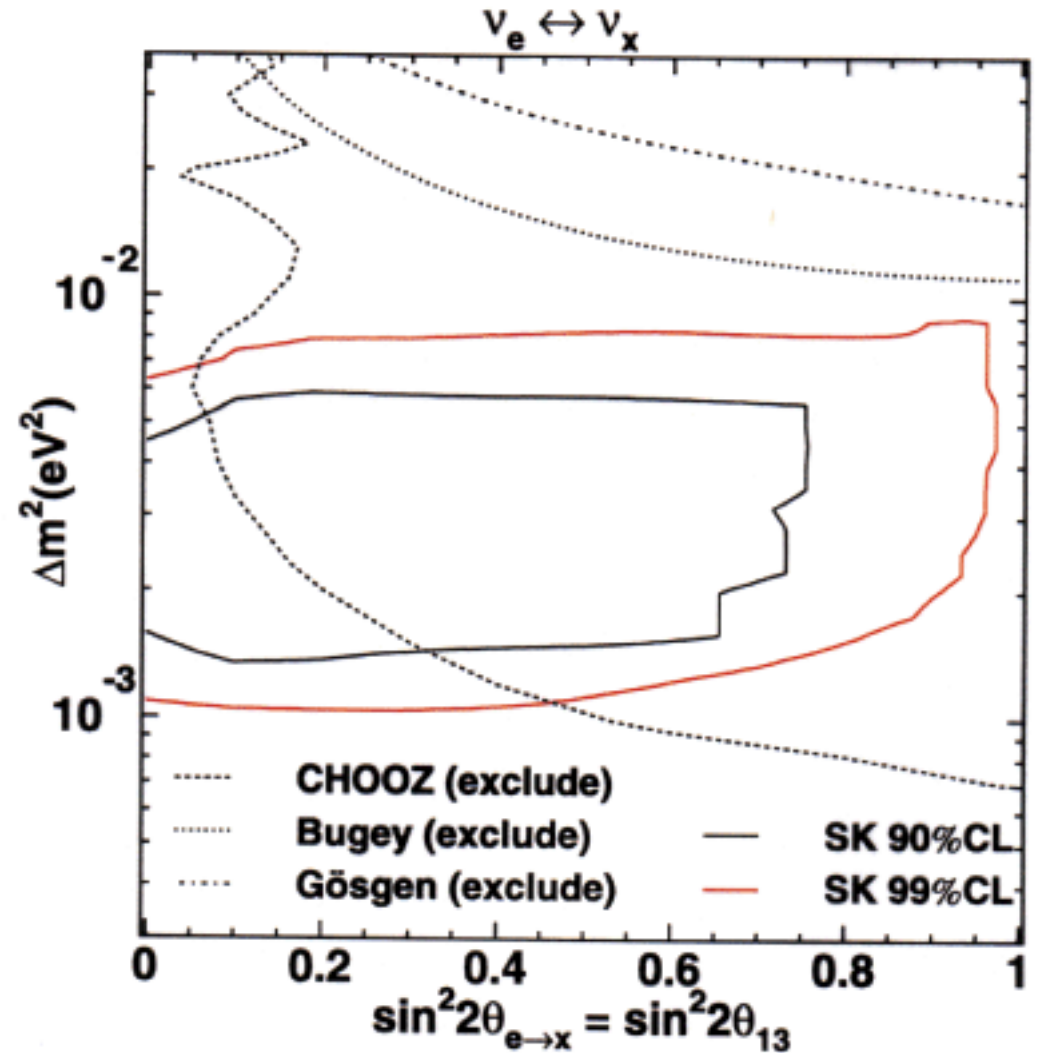
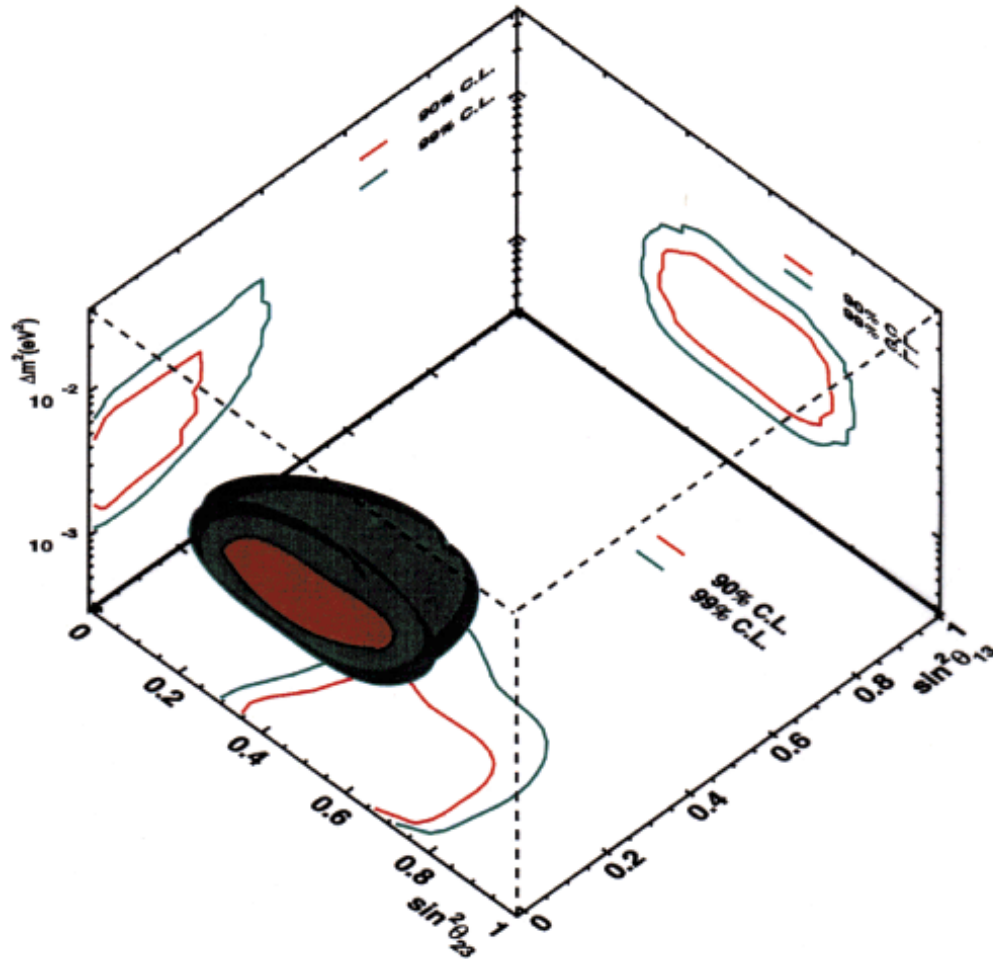
$$P(\nu_e \rightarrow \nu_\tau) \approx \sin^2 2\theta_{13} \cos^2 \theta_{23} \sin^2(\Delta m^2_{32} L/4E_\nu)$$

In contrast,

$$P(\nu_\mu \rightarrow \nu_\tau) = \cos^4 \theta_{13} \sin^2 2\theta_{23} \Delta^2_{32}$$

# 3 flavor mixing analysis of atmospheric

PRELIMINARY



**Atmospheric neutrinos  
analysis**

K. Nakamura, Nufact00, Monterey  
(USA), May 2000

# Running or approved LBL neutrino beams

	<b>K2K</b>	<b>MINOS</b>	<b>CNGS</b> <i>(shared)</i>
<b><i>E(GeV)</i></b>	<b>12</b>	<b>120</b>	<b>400</b>
<b><i>Pulse (10<sup>12</sup>ppp)</i></b>	6	40	92
<b><i>Rate (Hz)</i></b>	0.45	0.53	0.04
<b><i>Power (MW)</i></b>	<b>0.0052</b>	<b>0.41</b>	<b>0.22</b>
<b><i>Pot (/yr)</i></b>	<b>2×10<sup>19</sup></b>	<b>3.7×10<sup>20</sup></b>	<b>4.5×10<sup>19</sup></b> <i>(7.6×10<sup>19</sup> dedicated)</i>

# K2K (KEK-to-Kamioka)



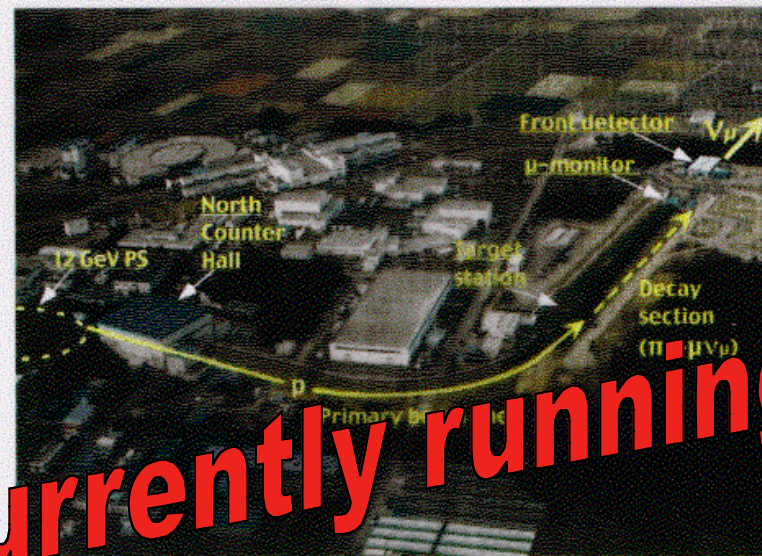
## Super Kamiokande

Water Cherenkov detector  
Total mass: 50 kton  
Inner mass: 32 kton  
Fiducial mass: 22.5 kton



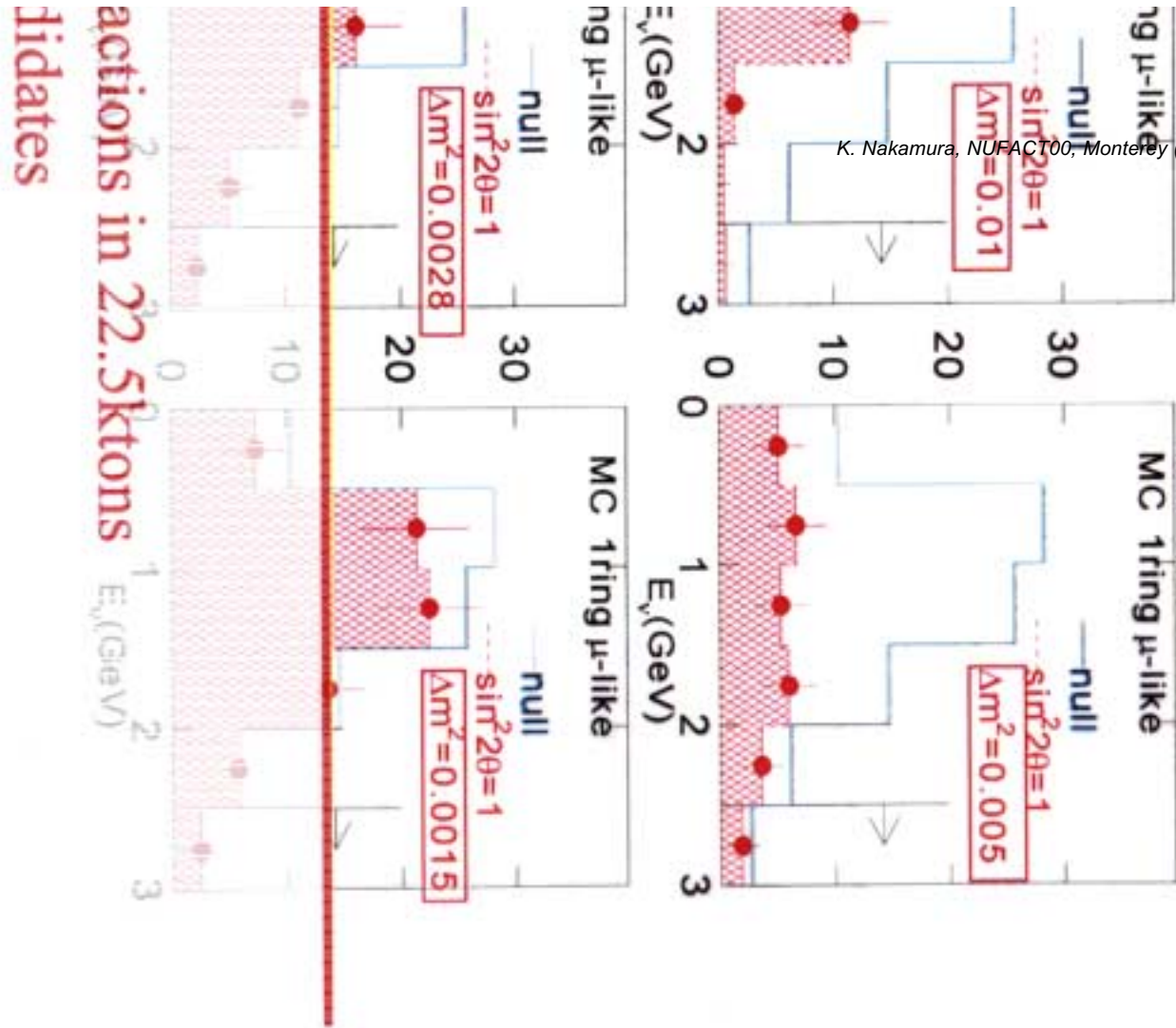
KEK

- Accelerator: 12 GeV proton synchrotron
  - Beam intensity:  $6 \times 10^{12}$  protons / pulse
  - Repetition: 1 pulse / 2.2 sec
  - Pulse width: 1.1  $\mu$ s (9 bunches)
- Horn-focused wide-band beam
  - Average neutrino energy: 1.4 GeV  $\rightarrow$   $\nu_{\mu} - \nu_{\tau}$  disappearance
- Near detector: 300 m from the target
- Far detector (Super-Kamiokande): 250 km from the target
- Goal:  $10^{20}$  protons on target



**Currently running!**

Naka-03



Reconstructed Neutrino Energy (MC)

Candidates

❖ *Results*  
*consistent* with  
*neutrino*  
*disappearance.*

❖ *More statistics*  
*needed.*

❖ *Final statistics:*  
*Expected  $10^{20}$*   
*pots*

❖ *Energy*  
*spectrum*

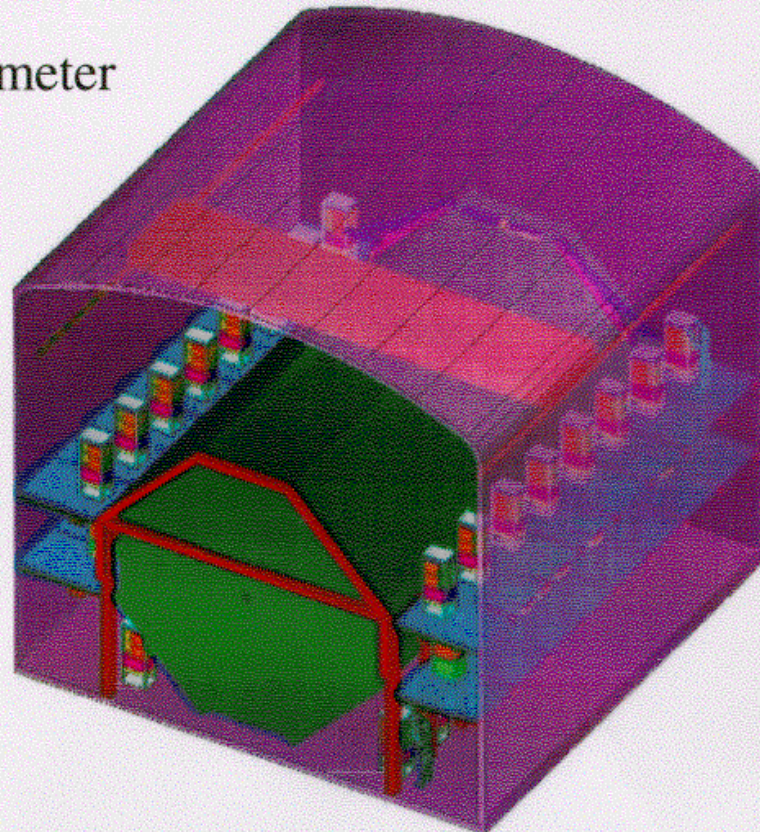
➔  $\Delta m_{32}^2, \theta_{23}$





# MINOS Far Detector

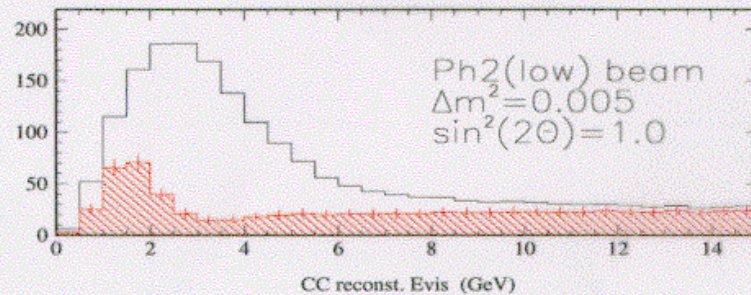
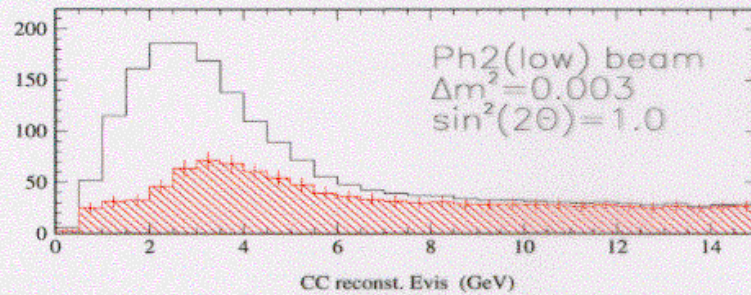
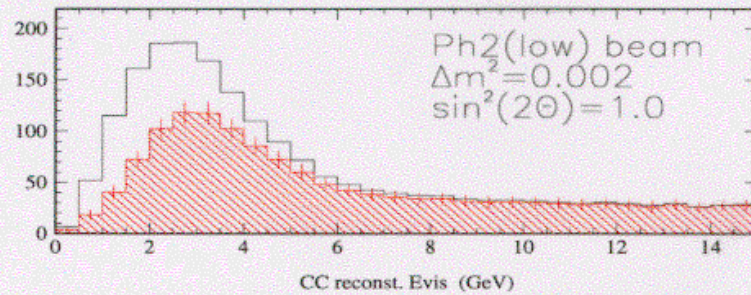
- 8m Octagonal Tracking Calorimeter
- 486 layers of 2.54cm Fe
- 2 sections, each 15m long
- 4.1cm wide solid scintillator strips with WLS fiber readout
- 25,800 m<sup>2</sup> active detector planes
- Magnet coil provides  $\langle B \rangle \approx 1.3\text{T}$
- 5.4kt total mass



Half of the MINOS Far Detector



# MINOS Energy Spectra



10 kt-yr Exposure

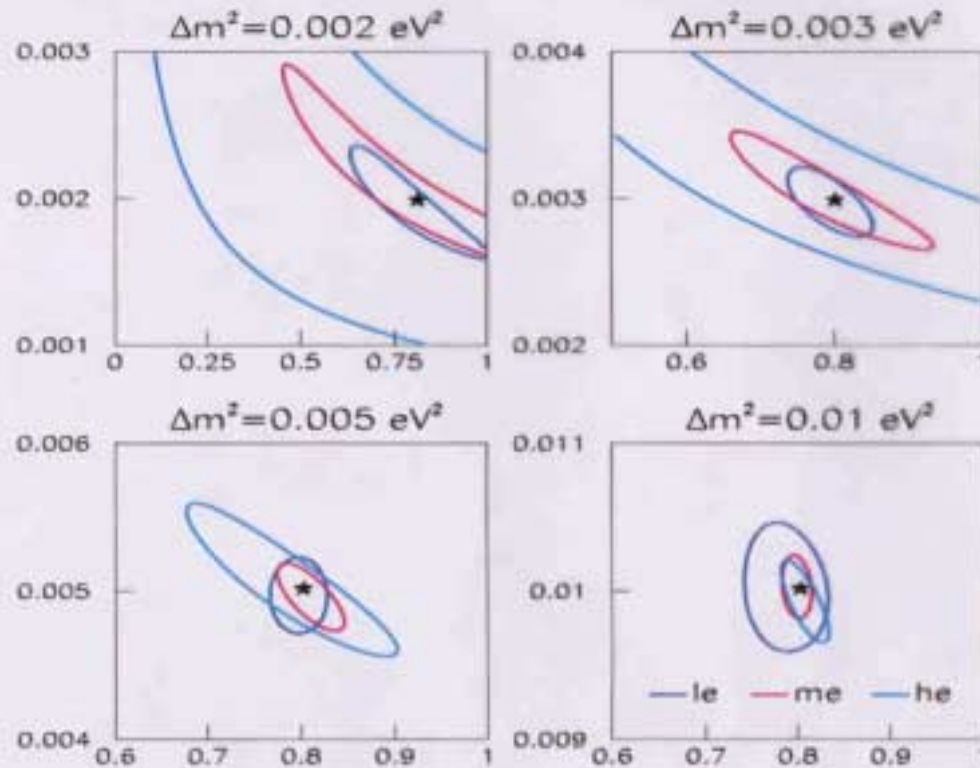
Solid lines - energy spectrum  
without oscillations

Dashed histogram - spectrum  
in presence of oscillations

→  $\Delta m_{32}^2, \theta_{23}$



# Comparison of Different Beams



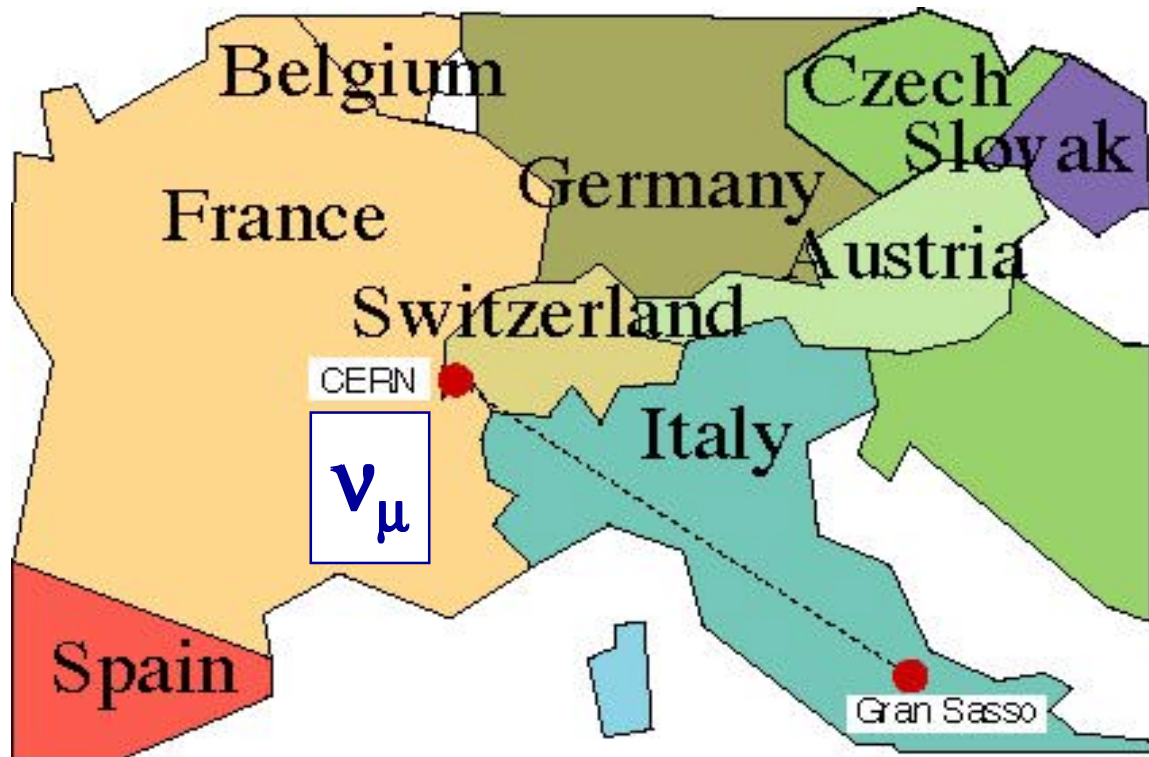
CC Energy Spectra  
68% Contours  
10kt-yr exposure

# CNGS neutrino beam

The expected  $\nu_e$  and  $\nu_\tau$  contamination of the CNGS beam are of the order of  $10^{-2}$  and  $10^{-7}$  respect to the dominant  $\nu_\mu$ .

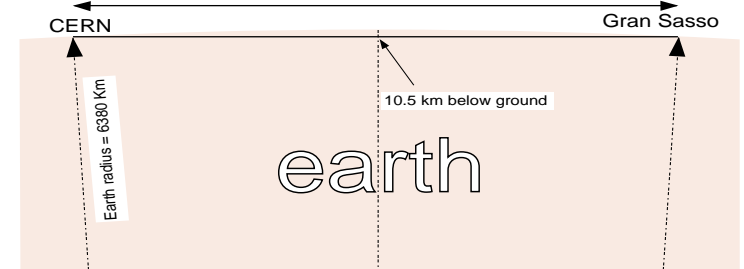
CERN 98-02 - INFN/AE/98-05

CERN-SL/99-034(DI) - INFN/AE-99/05



$\nu_\tau?$   $\nu_e?$

CERN Neutrino Beam in the Direction of Gran Sasso  
Distance = 732 Km



# CNGS beam characteristics

## Nominal $\nu$ beam

$\nu_{\mu}$ ( $\text{m}^{-2}$ / pot )	$7.78 \times 10^9$
$\nu_{\mu}$ CC / pot / kton	$5.85 \times 10^{-17}$
$\langle E \rangle_{\nu}$ ( GeV )	17
$(\nu_e + \bar{\nu}_e) / \nu_{\mu}$	0.87 %
$\bar{\nu}_{\mu} / \nu_{\mu}$	2.1 %
$\nu_{\tau}$ prompt	negligible

$\Rightarrow$  Interactions with 1.8 kton target x 5 years

$\sim 30000 \nu$  NC+CC

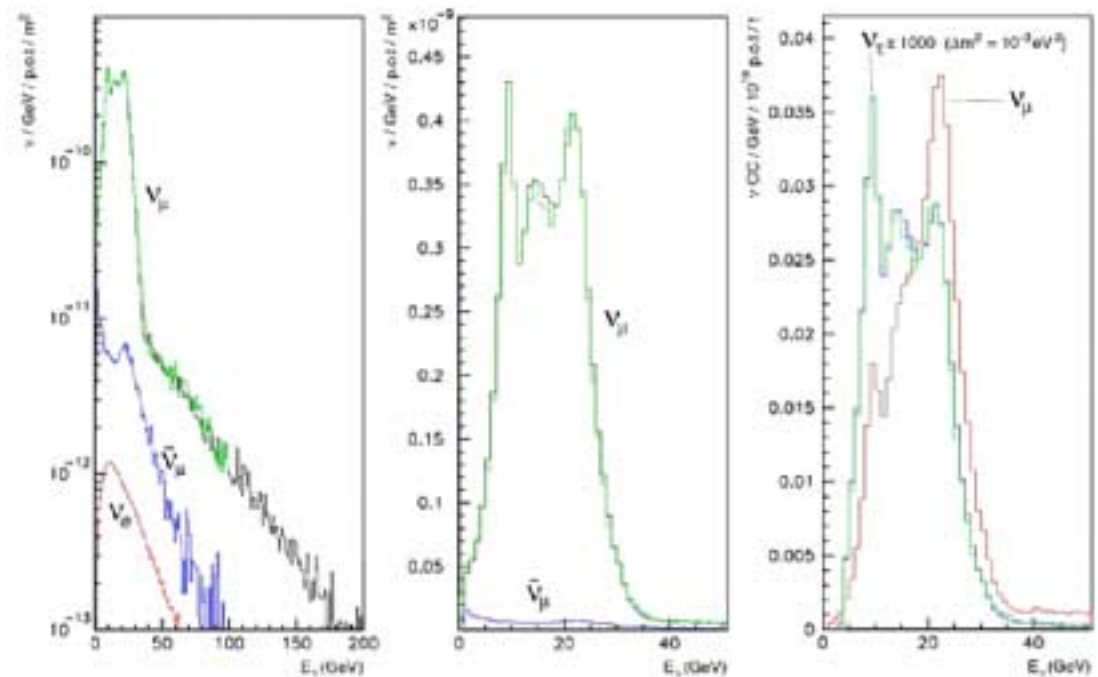
$\sim 140 \nu_{\tau}$  CC (@full mixing,  $\Delta m^2 = 2.5 \times 10^{-3} \text{ eV}^2$ )

400 GeV primary protons

**Shared SPS operation**

**200 days/year**

**$4.5 \times 10^{19}$  pot / year**



# CNGS event rates

- ★ Primary protons: **400 GeV;  $4 \times 2.3 \times 10^{13}$  p/cycle; 26.4 s/cycle**
- ★ Pots per year:  **$4.5 \times 10^{19}$  pots “shared”; 200x0.75 days/year**
- ★  **$7.6 \times 10^{19}$  pots/yr “dedicated”**

Process	Rates (events/kton/year)
$\nu_\mu$ CC	2450
$\bar{\nu}_\mu$ CC	49
$\nu_e$ CC	20
$\bar{\nu}_e$ CC	1.2
$\nu$ NC	823
$\bar{\nu}$ NC	17

No oscillations

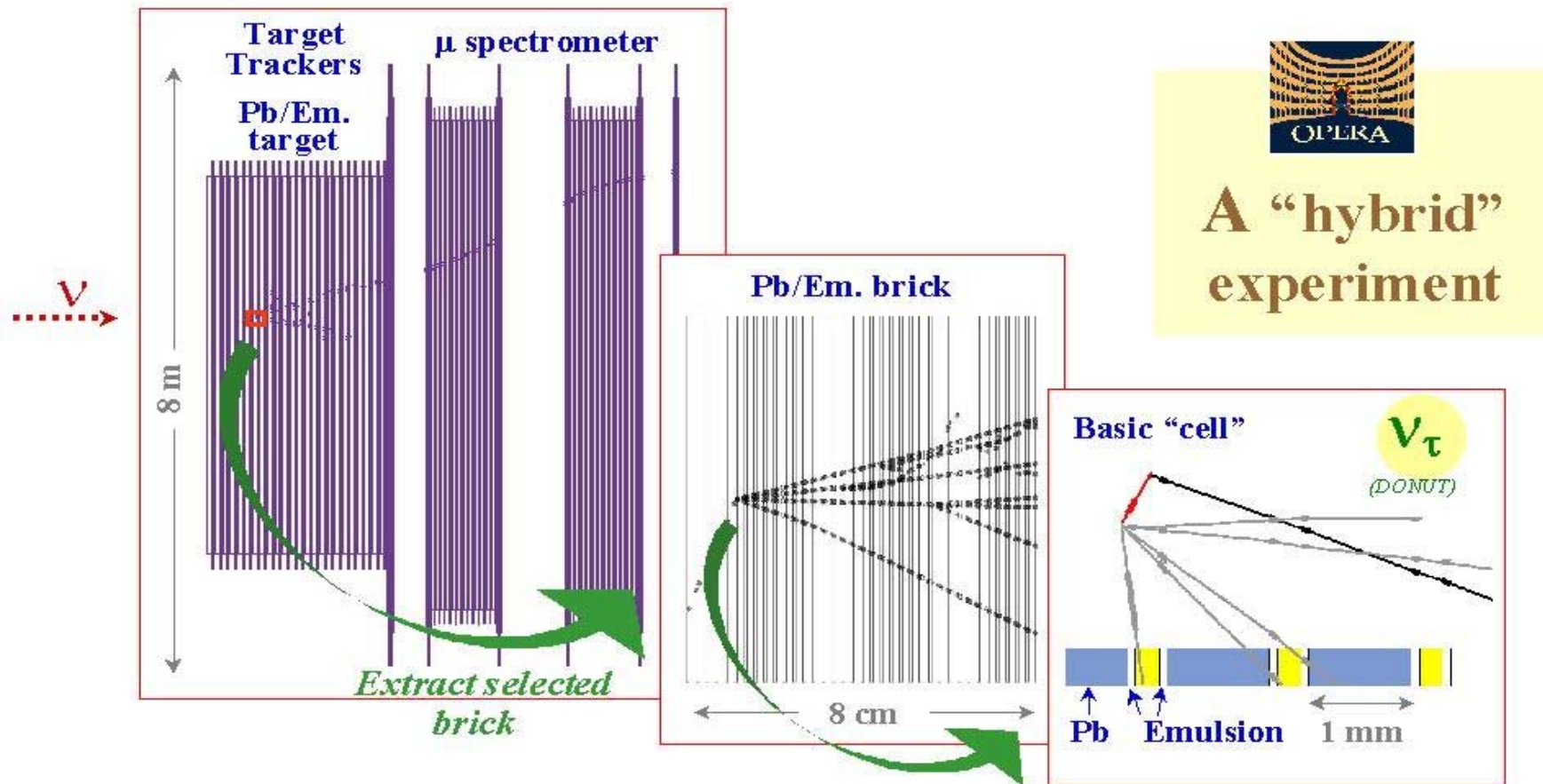
- ★ Optimized for  $N_\tau \propto \int \phi_{\nu_\mu}(E) \times \sigma_{\nu_\tau}^{CC}(E) E^{-2} dE$

$\Delta m^2$ (eV <sup>2</sup> )	Rates (events/kton/year)
$1 \times 10^{-3}$	2.4
$2.5 \times 10^{-3}$	15.1
$3.5 \times 10^{-3}$	29.4
$5 \times 10^{-3}$	58.6
$1 \times 10^{-2}$	209.0

ν<sub>τ</sub> CC event rates

CERN 98-02 - INFN-AE/98-05; CERN-SL/99-034(DI) - INFN/AE-99/05

# The OPERA experiment



**Electronic detectors**  
→ select  $\nu$  interaction brick  
→  $\mu$  ID, charge and  $p$

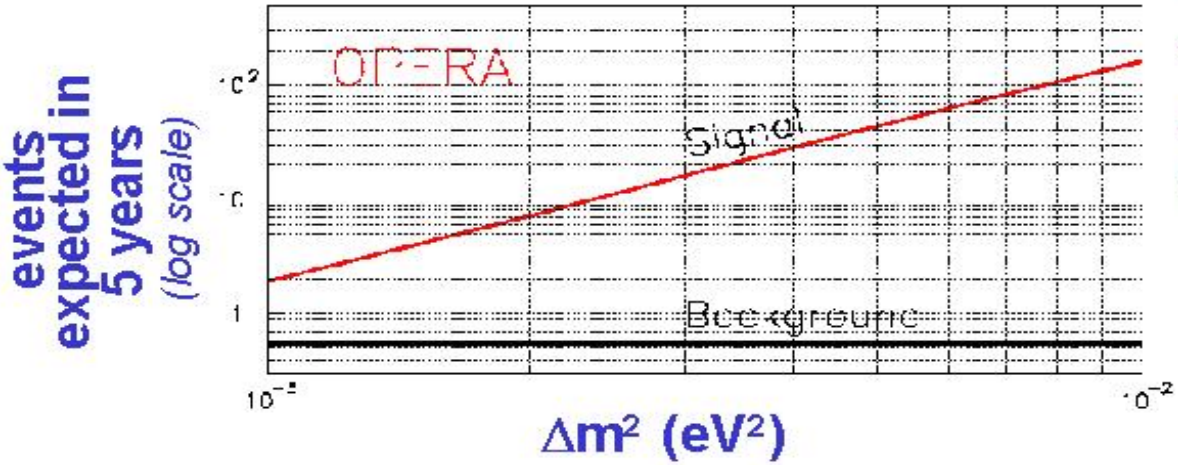
**Emulsion scanning**  
→ vertex search  
→ decay search  
→  $e/\gamma$  ID, kinematics



# Expected numbers of events

$\tau$ decay	$\nu_\tau$ events			b.g.
	$\Delta m^2$	$(10^3 \text{ eV}^2)$		
	1.5	3.2	5.0	
<b>e</b>	1.7	7.7	18.5	0.19
<b><math>\mu</math></b>	1.3	5.7	13.8	0.13
<b>h</b>	1.1	4.9	11.8	0.25
<b>Total</b>	<b>4.1</b>	<b>18.3</b>	<b>44.1</b>	<b>0.57</b>

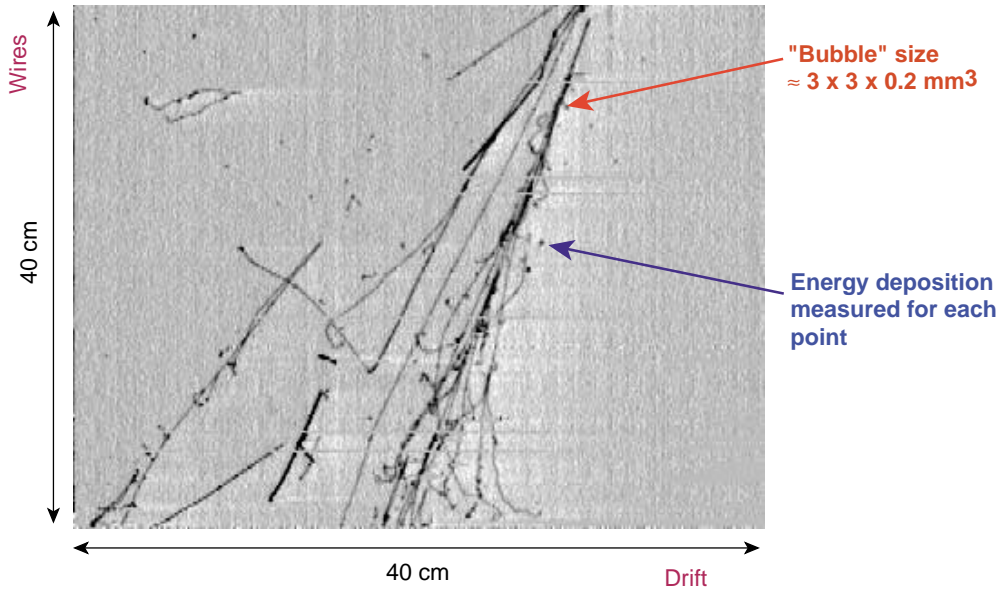
- Full mixing
- 5 years with shared SPS operation (2.25x10<sup>20</sup> pot)
- Average target mass = 1.8 kton  
(accounting for mass reduction with time, due to brick removal for analysis)
- Uncertainties on background and efficiencies accounted for in the following



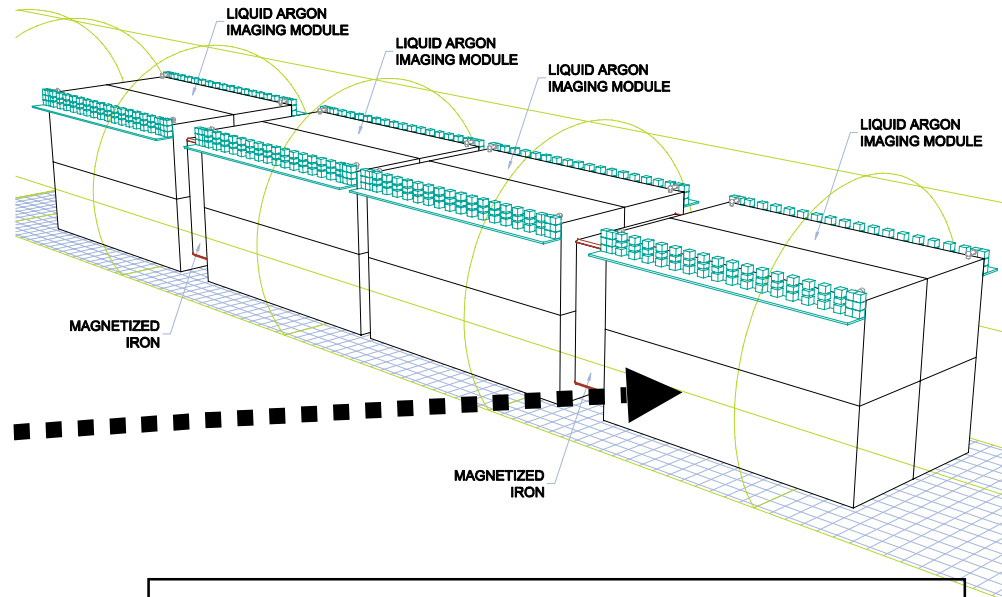
➔  $\Delta m_{32}^2 \times \theta_{23}$



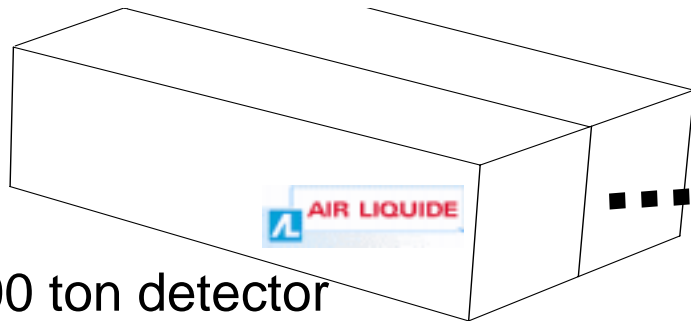
# The ICARUS experiment



## ICARUS multi-kton



## ICARUS T600 (approved)



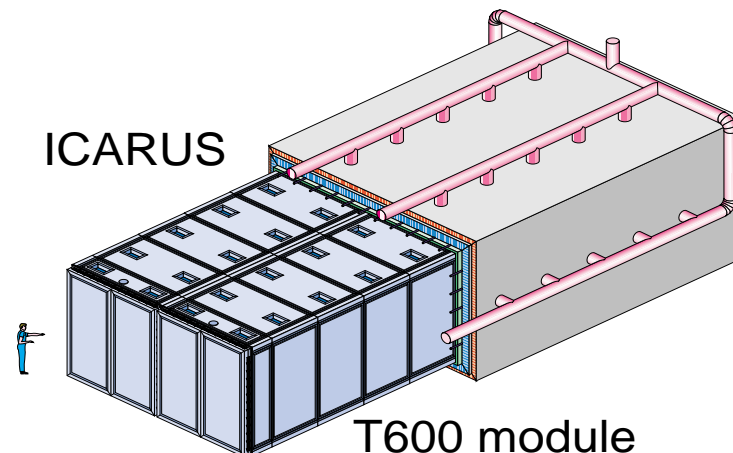
600 ton detector

*First test run in March 2001!  
In LNGS Tunnel in 2002*

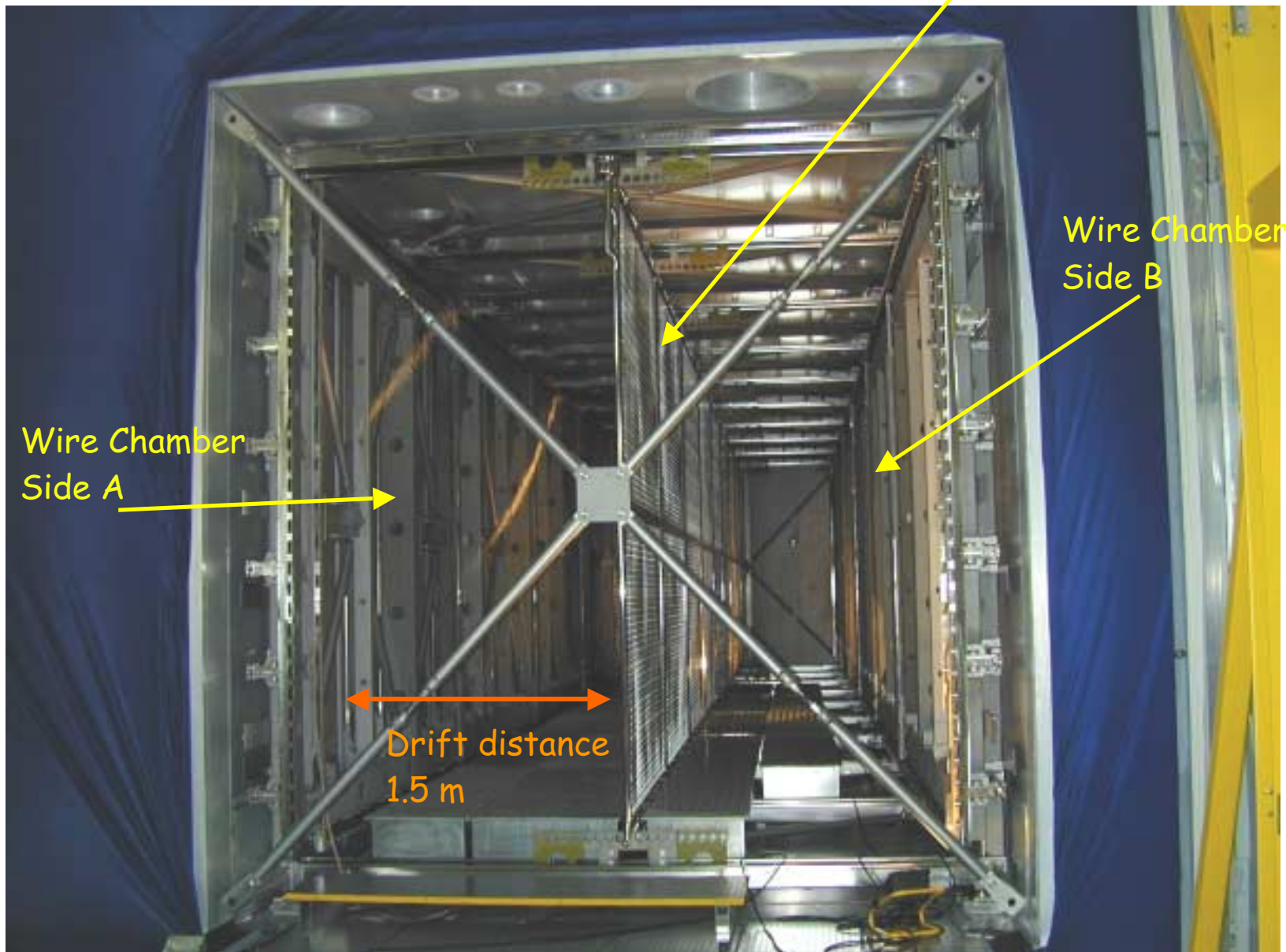
Two possible options:  
A) n x T600  
B) m x T1400 (better for physics)

# The first ICARUS T600 prototype

- ★ The T600 module is to be considered as a fundamental milestone on the road towards a total sensitive mass in the multi-kton range
  - First piece of the detector to be complemented by further modules of appropriate size and dimension ⇒ *Goal is to reach a multikton mass in LNGS tunnel in a most efficient and rapid way*
- ★ It has a physics program of its own, immediately relevant to neutrino physics, though limited by statistics (see hep-ex/0103008)



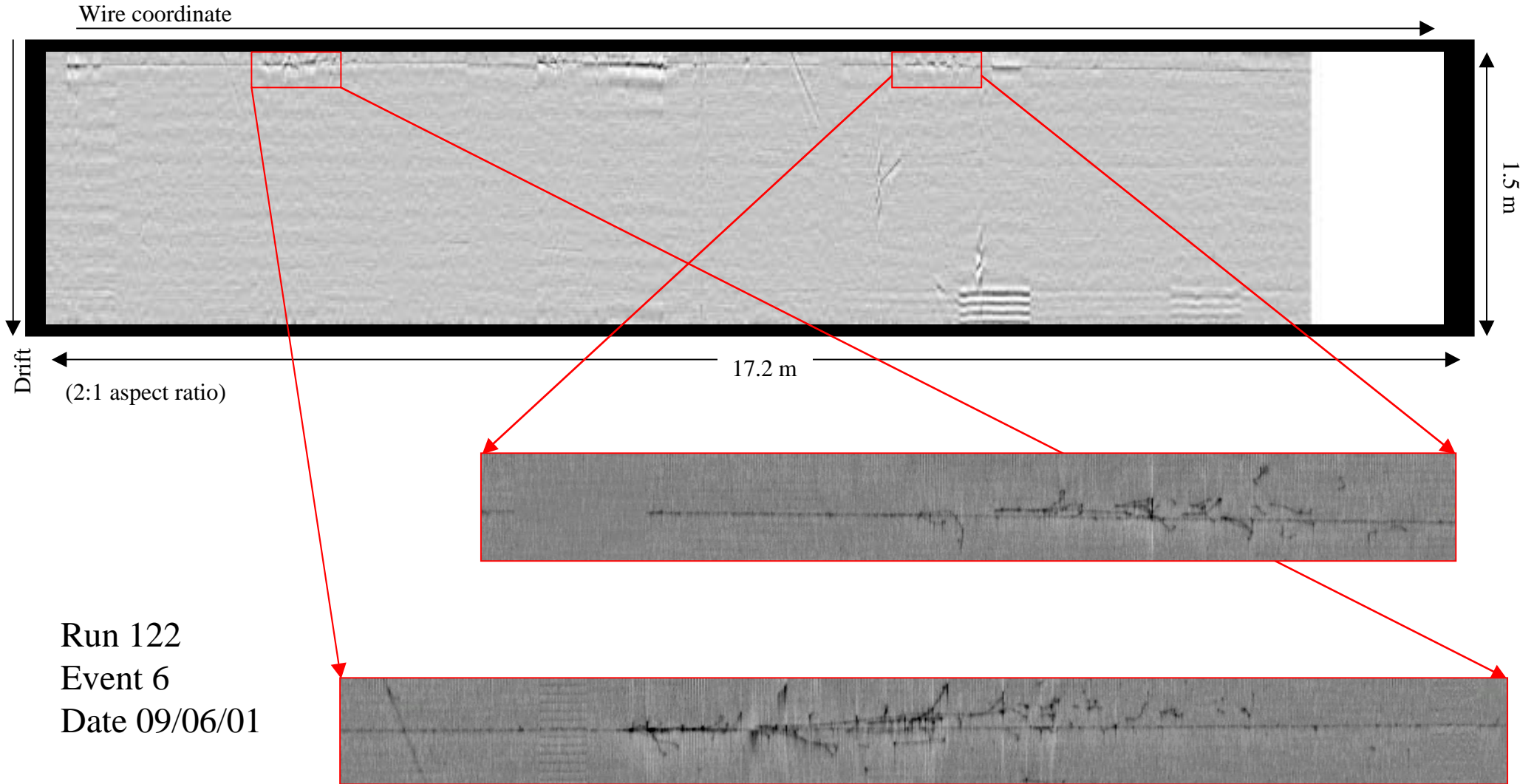
# *T600 - Completed Internal Half-Detector view*



# *ICARUS T600 semimodule horizontal muon*

***VERY PRELIMINARY***

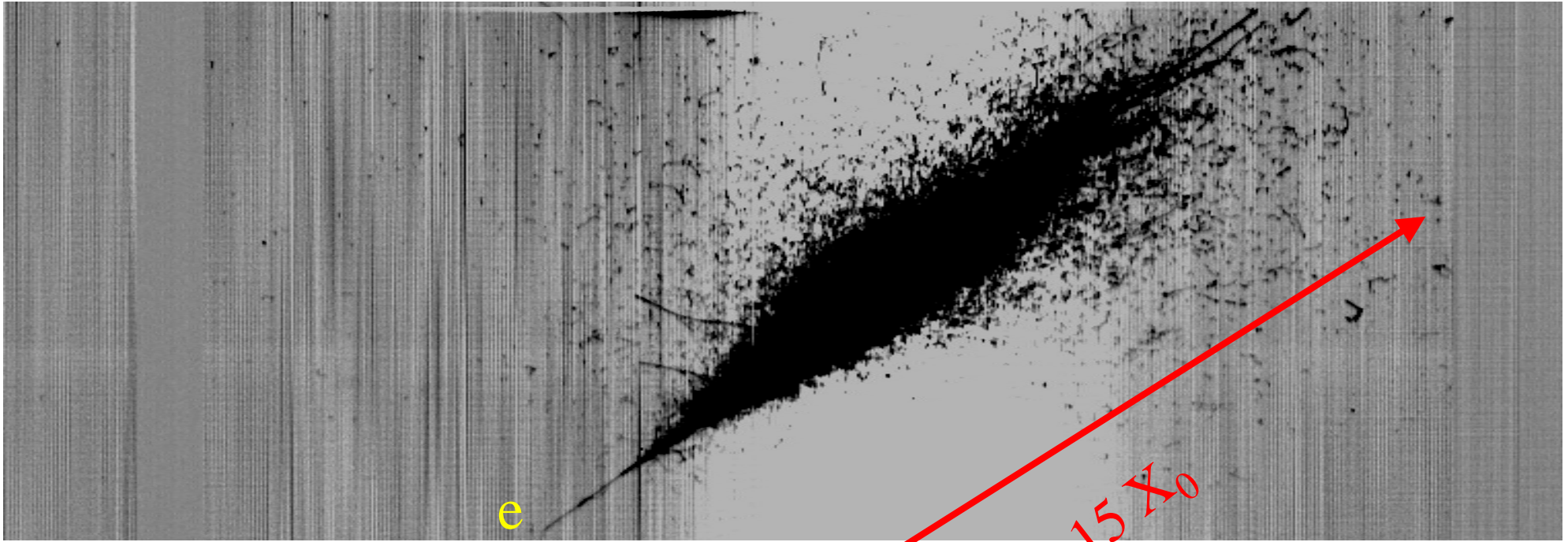
**60° Induction view**



# ICARUS T600 high energy electron candidate

The entering track is consistent with the  $dE/dx$  deposition of a single electron. An  $e^+e^-$  pair from a converted photon would deposit twice as much energy.

**VERY PRELIMINARY**



Run 308  
Event 332  
Date 21/06/01

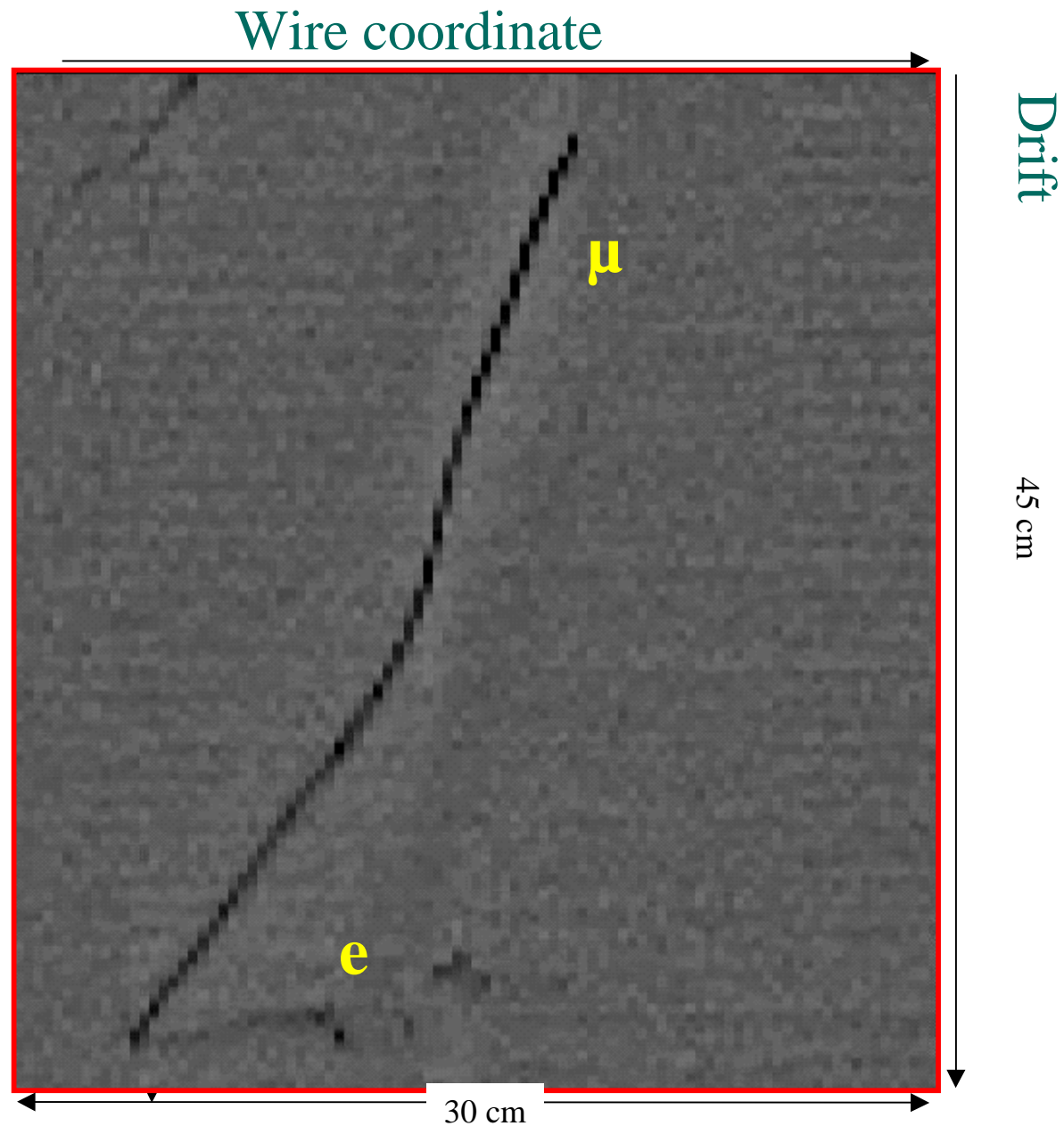
From the position of the shower maximum,  
we can estimate the electron energy  $E_e \approx$   
20 GeV

# ICARUS T600 semimodule stopping muon

**VERY  
PRELIMINARY**

**60° Collection view**

Run 118  
Event 11  
Date 08/06/01



# CNGS events in 4 kton, 5 years running

20 kton × year

$$\theta_{23} = 45^\circ, \theta_{13} = 7^\circ$$

	No osci	$\Delta m_{23}^2$ (eV <sup>2</sup> )		
		$1 \times 10^{-3}$	$3.5 \times 10^{-3}$	$5 \times 10^{-3}$
$\nu_\mu$ CC	54300	53820	49330	44910
$\bar{\nu}_\mu$ CC	1090	1088	1070	1057
$\nu_e$ CC	437	437	437	436
$\bar{\nu}_e$ CC	29	29	29	29
$\nu$ NC			17550	
$\bar{\nu}$ NC			410	
$\nu_\mu \rightarrow \nu_e$ CC	-	7	74	143
$\nu_\mu \rightarrow \nu_\tau$ CC	-	52	620	1250
$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ CC	-	< 1	< 1	1
$\bar{\nu}_\mu \rightarrow \bar{\nu}_\tau$ CC	-	< 1	6	13

# $\nu_\mu \rightarrow \nu_\tau$ oscillations in ICARUS 4 kton

## ★ Analysis of the electron sample

→ Exploit the small intrinsic  $\nu_e$  contamination of the beam

→ Exploit the unique  $e/\pi^0$  separation

## ★ Expected in 5 years @ CNGS and 4 ktons:

$$\nu_\mu \rightarrow \nu_\tau$$

$$\nu_\tau + N \rightarrow \tau + \text{jet}; \quad \tau \rightarrow e \nu \nu$$

Charged current (CC)

Br  $\approx$  18%

$$\Delta m^2 = 3.5 \times 10^{-3} eV^2 \Rightarrow 110 \text{ events}$$

**Background:**

$$\nu_e + N \rightarrow e + \text{jet}$$

Charged current (CC)

$$470 \nu_e \text{ CC}$$

*Statistical excess visible before cuts  $\Rightarrow$  this is the main reason for performing this experiment at long baseline !*

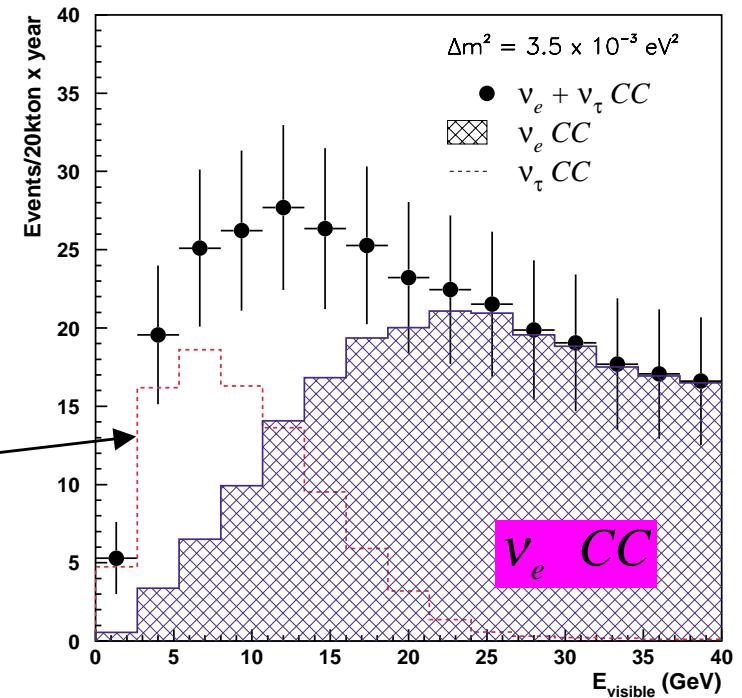


# $\nu_\mu \rightarrow \nu_\tau$ oscillations (II)

- ★ Reconstructed visible energy spectrum of electron events clearly evidences excess from oscillations into tau neutrino

$\Delta m_{32}^2 \times \theta_{23}$

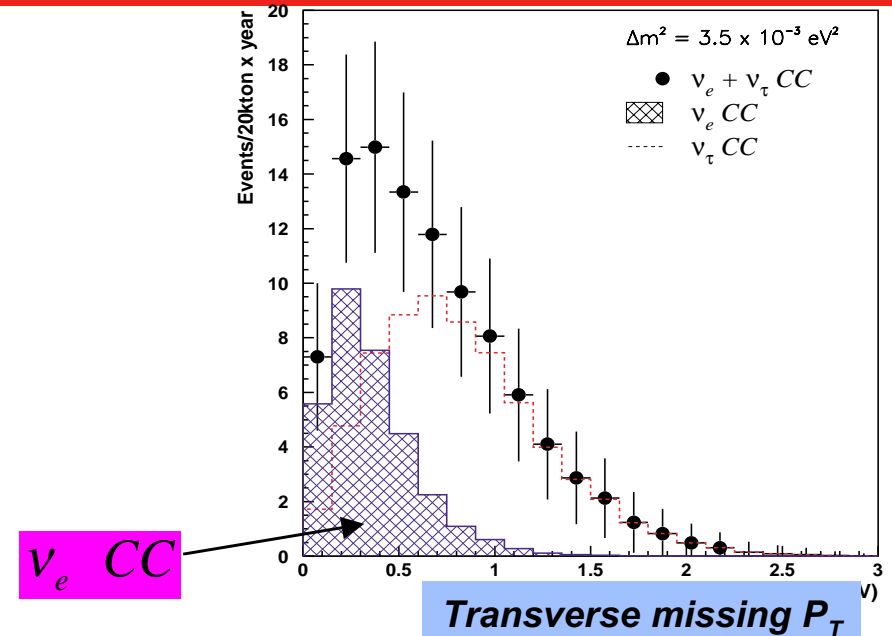
*signal*



Cuts	$\nu_\tau$ Eff. (%)	$\nu_e$ CC	$\bar{\nu}_e$ CC	$\nu_\tau$ CC $\Delta m^2 = 10^{-3} \text{ eV}^2$	$\nu_\tau$ CC $\Delta m^2 = 2.8 \times 10^{-3} \text{ eV}^2$	$\nu_\tau$ CC $\Delta m^2 = 3.5 \times 10^{-3} \text{ eV}^2$	$\nu_\tau$ CC $\Delta m^2 = 10^{-2} \text{ eV}^2$
Initial	100	437	29	9.3	71	111	779
Fiducial volume	88	383	25	8.2	64	97	686
One candidate with momentum > 1 GeV	72	365	25	6.7	50	80	561
$E_{vis} < 18 \text{ GeV}$	67	64	5	6.2	46	75	522

# $\nu_\mu \rightarrow \nu_\tau$ oscillations (III)

- ★ Kinematical selection in order to enhance S/B ratio
- ★ Can be tuned “a posteriori” depending on the actual  $\Delta m^2$
- ★ For example, with cuts listed below, reduction of background by factor 100 for a signal efficiency 33%



Cuts	$\nu_\tau$ Eff. (%)	$\nu_e$ CC	$\bar{\nu}_e$ CC	$\nu_\tau$ CC $\Delta m^2 = 10^{-3} \text{ eV}^2$	$\nu_\tau$ CC $\Delta m^2 = 2.8 \times 10^{-3} \text{ eV}^2$	$\nu_\tau$ CC $\Delta m^2 = 3.5 \times 10^{-3} \text{ eV}^2$	$\nu_\tau$ CC $\Delta m^2 = 10^{-2} \text{ eV}^2$
Initial	100	437	29	9.3	71	111	779
Fiducial volume	88	383	25	8.2	64	97	686
One candidate with momentum > 1 GeV	72	365	25	6.7	50	80	561
$E_{vis} < 18 \text{ GeV}$	67	64	5	6.2	46	75	522
$P_T^e < 0.9 \text{ GeV}$	54	31	3	5.0	38	60	421
$P_T^{lep} > 0.3 \text{ GeV}$	51	29	2	4.7	35	56	397
$P_T^{miss} > 0.6 \text{ GeV}$	33	4	0.4	3.1	23	37	257

# Search for $\theta_{13} > 0$

$$\Delta m_{32}^2 = 3.5 \times 10^{-3} \text{ eV}^2; \sin^2 2\theta_{23} = 1$$

**ICARUS 4kton**  
5 years @ CNGS

Cuts: Fiducial,  $E_e > 1 \text{ GeV}$ ,  $E_{vis} < 20 \text{ GeV}$

$$\Delta m_{23}^2 = 3.5 \times 10^{-3} \text{ eV}^2, \theta_{23} = 45^\circ$$

$\theta_{13}$ (degrees)	$\sin^2 2\theta_{13}$	$\nu_e \text{ CC}$	$\nu_\mu \rightarrow \nu_\tau$ $\tau \rightarrow e$	$\nu_\mu \rightarrow \nu_e$	Total	Statistical significance
9	0.095	79	74	84	237	$6.8\sigma$
8	0.076	79	75	67	221	$5.4\sigma$
7	0.058	79	76	51	206	$4.1\sigma$
5	0.030	79	77	26	182	$2.1\sigma$
3	0.011	79	77	10	166	$0.8\sigma$

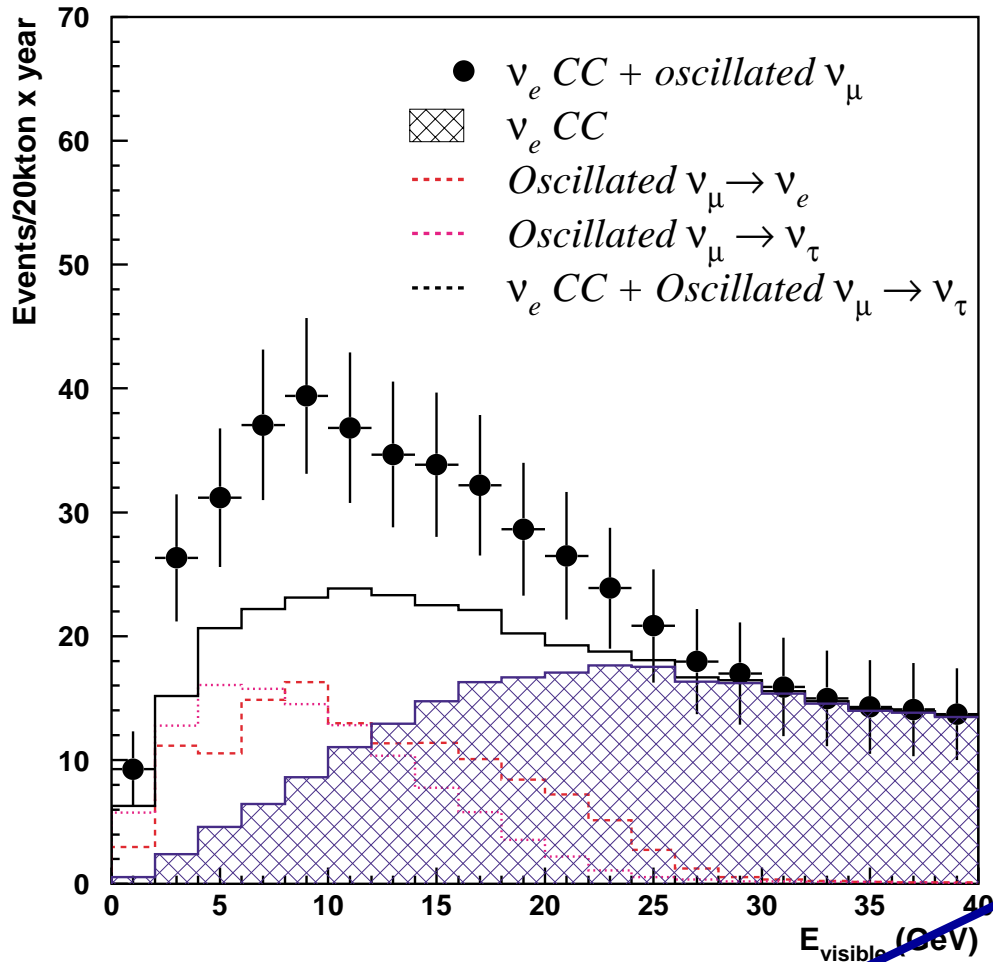
$$P(\nu_\mu \rightarrow \nu_\tau) = \cos^4 \theta_{13} \sin^2 2\theta_{23} \Delta_{32}^2$$

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta_{13} \sin^2 \theta_{23} \Delta_{32}^2$$

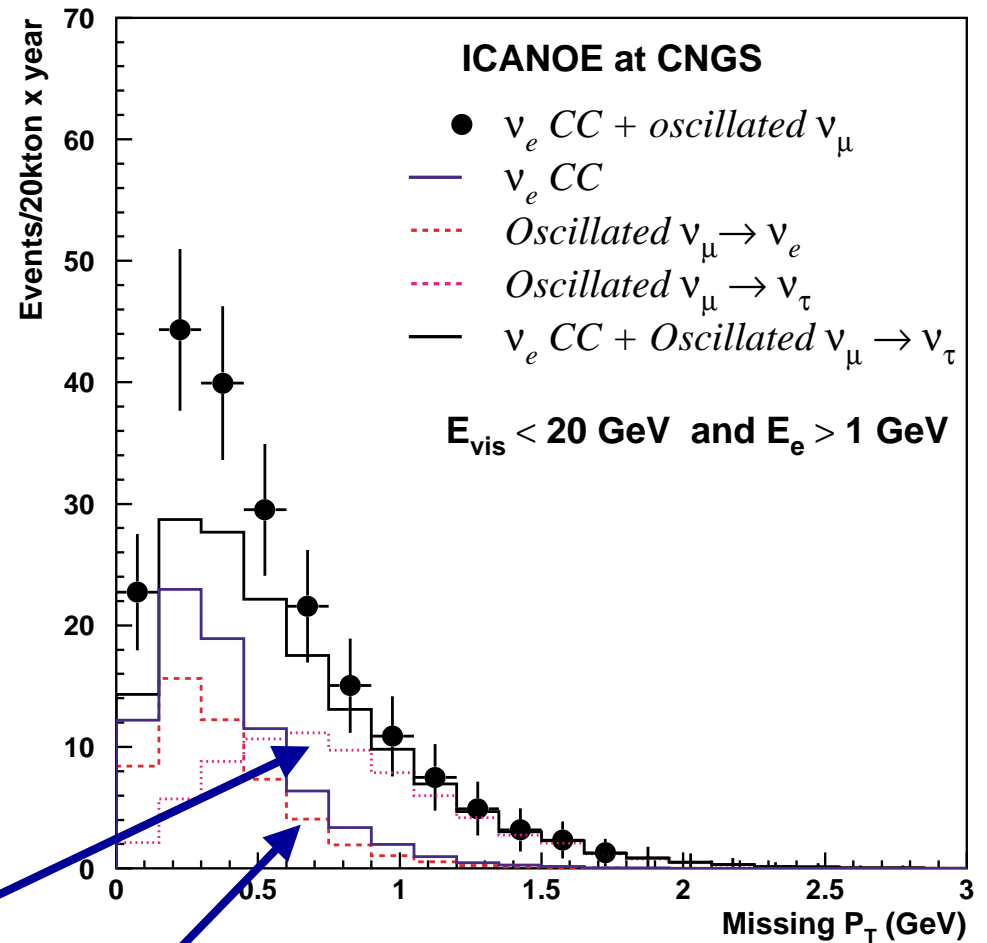
$$\Delta m_{32}^2, \theta_{23}, \theta_{13}$$

$$\Delta m_{32}^2 = 3.5 \times 10^{-3} \text{ eV}^2; \sin^2 2\theta_{23} = 1; \sin^2 2\theta_{13} = 0.05$$

### Total visible energy



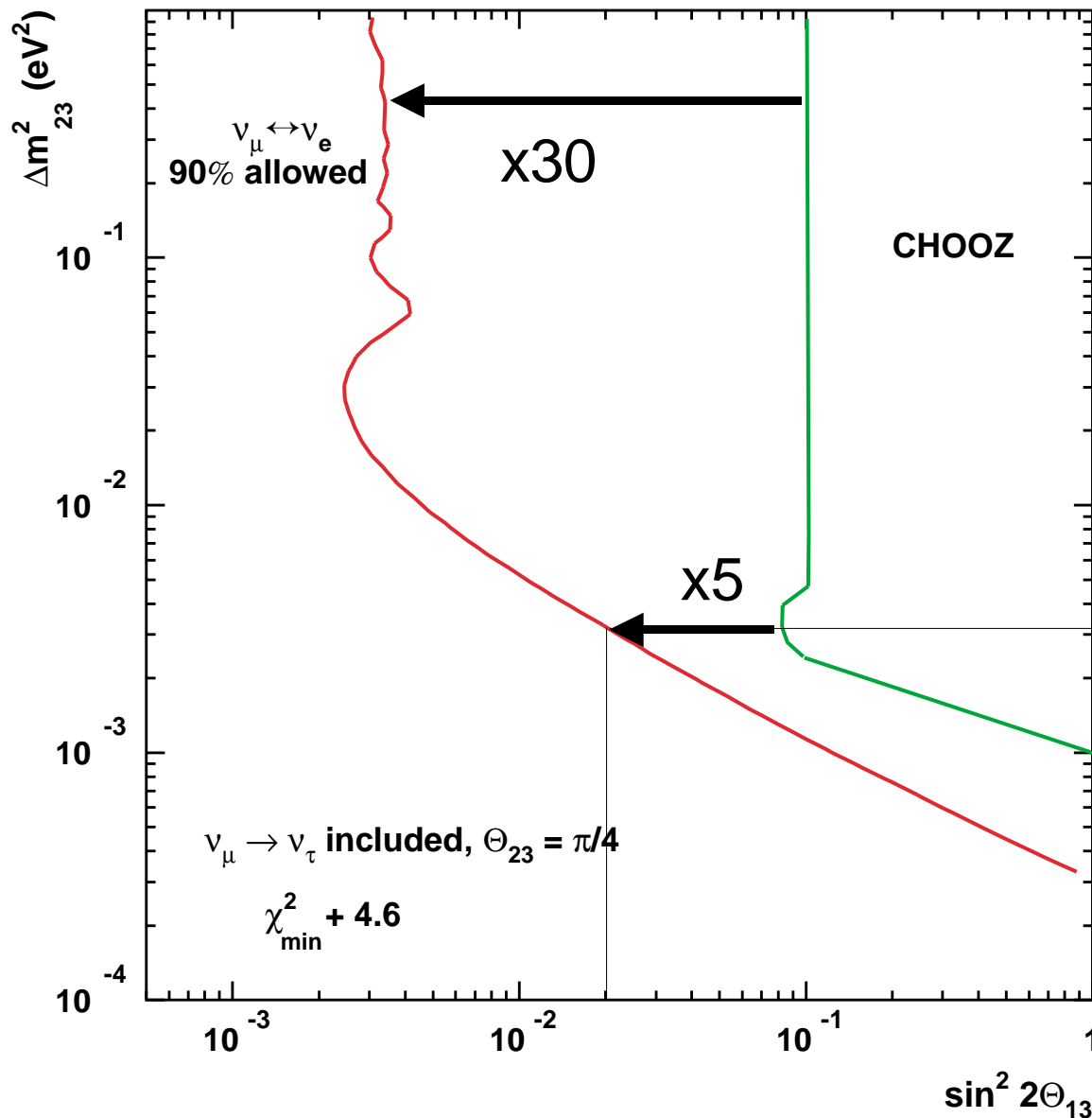
### Transverse missing $P_T$



$$P(\nu_\mu \rightarrow \nu_\tau) = \cos^4 \theta_{13} \sin^2 2\theta_{23} \Delta_{32}^2$$

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta_{13} \sin^2 \theta_{23} \Delta_{32}^2$$

# Sensitivity to $\theta_{13}$ in three family-mixing



**ICARUS 4kton**  
5 years @ CNGS

Sensitivity assuming both  $\nu_{\mu} \rightarrow \nu_{\tau}$  and  $\nu_{\mu} \rightarrow \nu_e$  at the same  $\Delta m^2$  (i.e. three family mixing)

$$\sin^2 2\theta_{13} > 2 \times 10^{-2}$$

$$\text{for } \Delta m^2_{32} = 3 \times 10^{-3} \text{ eV}^2$$

Study led by US working group:

# Oscillation Measurements with Upgraded Conventional Neutrino Beams

April 20, 2001

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***arXiv:hep-ph/0103052***

# The oscillation physics program at the Superbeams

Mostly  $\pi^+ \rightarrow \mu^+ \nu_\mu$

$\nu_\mu \rightarrow \nu_e$

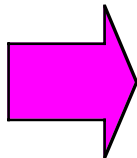
appearance

$\nu_\mu$

disappearance

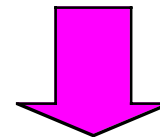
$\nu_\mu \rightarrow \nu_\tau$

appearance (high energy)



Backgrounds for  $\nu_\mu \rightarrow \nu_e$ :

1. Irreducible beam  $\nu_e$  content (K and  $\mu$  decays)
2. Electron misidentification



1. *Particle ID: electron identification and measurement*
2. *Near detector : can help predict flux accurately*

# Superbeams

	<b>K2K</b>	<b>MINOS</b>	<b>CNGS (shared)</b>	<b>JHF</b>	<b>JHF Phase II</b>	<b>Upgraded Booster</b>	<b>Super- NUMI</b>	<b>Super- NGS</b>
<b>E(GeV)</b>	<b>12</b>	<b>120</b>	<b>400</b>	<b>50</b>	<b>50</b>	<b>16</b>	<b>120</b>	<b>360</b>
<b>Pulse (<math>10^{13}</math>ppp)</b>	0.6	4	9.2	33		3		4
<b>Rate (Hz)</b>	0.45	0.53	0.04	0.29		15		<b>1</b>
<b>Power (MW)</b>	<b>0.0052</b>	<b>0.41</b>	<b>0.22</b>	<b>0.77</b>	<b>4</b>	<b>1</b>	<b>1.6</b>	<b>2.3</b>
<b>Pot (/yr)</b>	<b><math>2 \times 10^{19}</math></b>	<b><math>3.7 \times 10^{20}</math></b>	<b><math>4.5 \times 10^{19}</math></b>	<b><math>10^{21}</math></b>	<b><math>5 \times 10^{21}</math></b>		<b><math>1.4 \times 10^{21}</math></b>	<b><math>7 \times 10^{20}</math></b>

*2000  $\Rightarrow$  2010*

*2008 and beyond*



# Comparison event rates Superbeams vs Nufactory

Table 1: Neutrino event rates assuming no oscillations, compared with intrinsic beam backgrounds for conventional and muon-derived beams of comparable energies. The calculations assume a 1.6 MW proton source is used for the MINOS-type beam, the neutrino factories provide  $2 \times 10^{20}$  muon decays per year in the beam-forming straight section, and the detector is 732 km downstream of the neutrino source.

hep-ph/0103052

Super-NUMI  
1.6MW

Beam (Signal: $\nu_\mu \rightarrow \nu_e$ )	$\langle E_\nu \rangle$ (GeV)	$\nu_\mu$ CC Events (per kton-year)	$\nu_e/\nu_\mu$ Fraction
MINOS-LE	3.5	1800	0.012
MINOS-ME	7	5760	0.009
MINOS-HE	15	12800	0.006

$L=732 \text{ km}$

Neutrino  
Factory  
 $2 \times 10^{20}$   
decays

Beam (Signal: $\nu_e \rightarrow \nu_\mu$ )	$\langle E_\nu \rangle$ (GeV)	$\nu_e$ CC Events (per kton-year)	$\nu_\mu/\nu_e$ Fraction
4.5 GeV $\mu$ Ring	3.5	400	0
9.1 GeV $\mu$ Ring	7	3700	0
18.2 GeV $\mu$ Ring	15	31400	0
30 GeV $\mu$ Ring	20	72600	0

## *Intrinsic beam background*

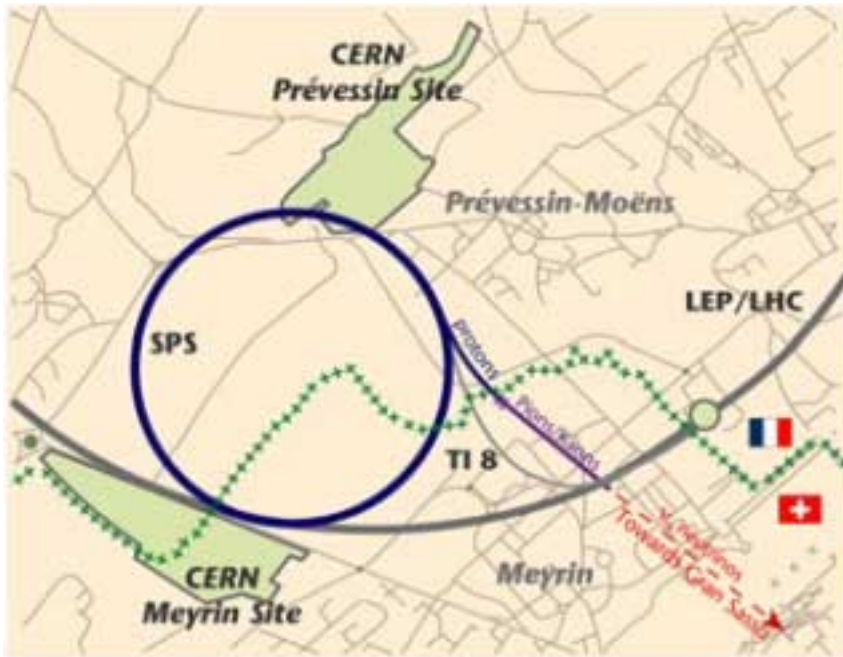
Table 2: Electron neutrino fractions and the fractional energy spreads for a selection of current (or next) generation conventional neutrino beams. Note that most beamlines produce a beam with a fractional energy spread between 30% and 50%, and a  $\nu_e$  contamination that ranges from 0.2% to 1.2%, for beams at or above 1 GeV.

hep-ph/0103052

Beamline	Proton Energy (GeV)	Peak $\nu_\mu$ Energy (GeV)	$\nu_e/\nu_\mu$ ratio	$\sigma_{E_\nu}/E_\nu$
K2K	12	1.4	0.7%	1.0
MINOS LE	120	3.5	1.2%	0.28
MINOS ME	120	7	0.9%	0.43
MINOS HE	120	15	0.6%	0.47
CNGS	400	18	0.8%	0.33
JHF wide	50	1	0.7%	1.0
JHF HE	50	5	0.9%	0.40
MiniBooNE	8	0.5	0.2%	0.50
ORLaND	1.3	0.0528	0.05%	0.38

*Typ. at the level of 1% for multiGeV beams, assuming 5% error  $\Rightarrow$   
natural limit  $\approx 5 \times 10^{-4}$*

# Super-CNGS



	CNGS (shared)	Super-NGS
<b>E(GeV)</b>	<b>400</b>	<b>360</b>
<b>Pulse (<math>10^{13}</math>ppp)</b>	9.2	4
<b>Rate (Hz)</b>	0.04	<b>1</b>
<b>Power (MW)</b>	<b>0.22</b>	<b>2.3</b>
<b>Pot (/yr)</b>	<b><math>4.5 \times 10^{19}</math></b>	<b><math>7 \times 10^{20}</math></b>

⇒ Assume for simplicity, **Super-CNGS = 20xCNGS with same beam optics**

**→**  $\approx 300$  (48)  $\nu_\tau$  CC/kt/year @  $\Delta m^2 = 2.5(1.0) \times 10^{-3} \text{ eV}^2$ , full mixing

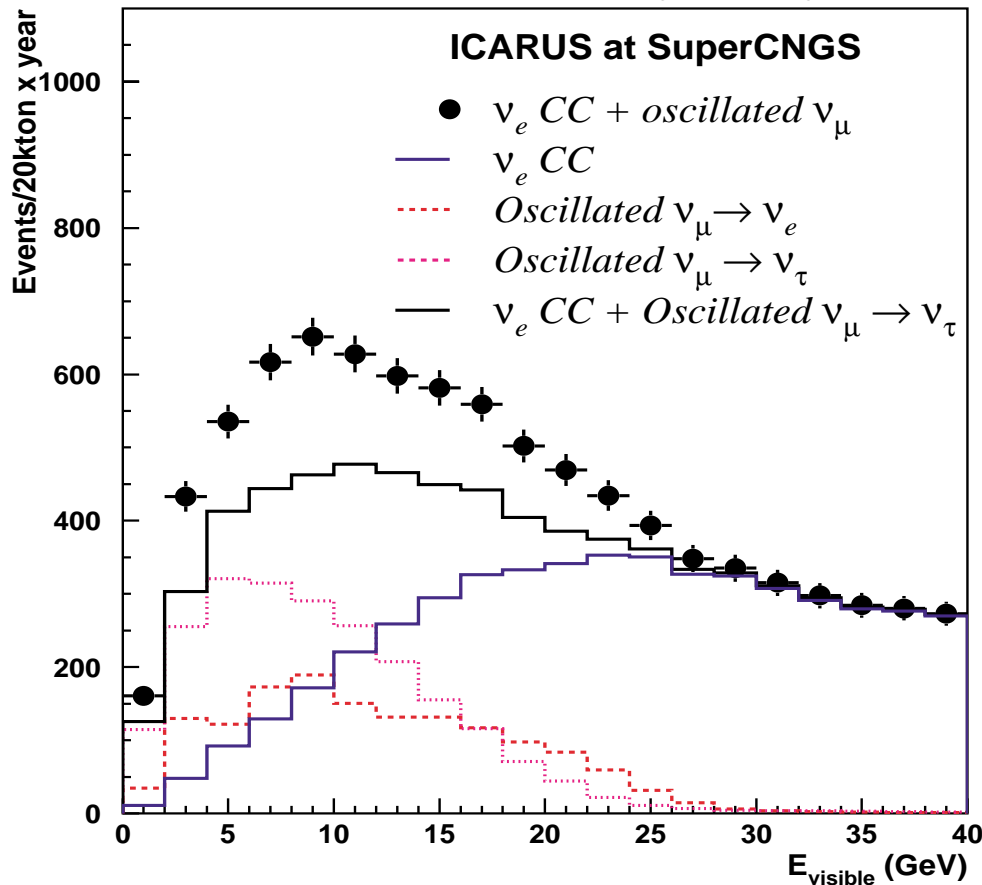
Also, with **high proton yield**, **low energy beam** optics optimizations become viable!

# $\nu_\mu \leftrightarrow \nu_e$ oscillations (CNGS superbeam)

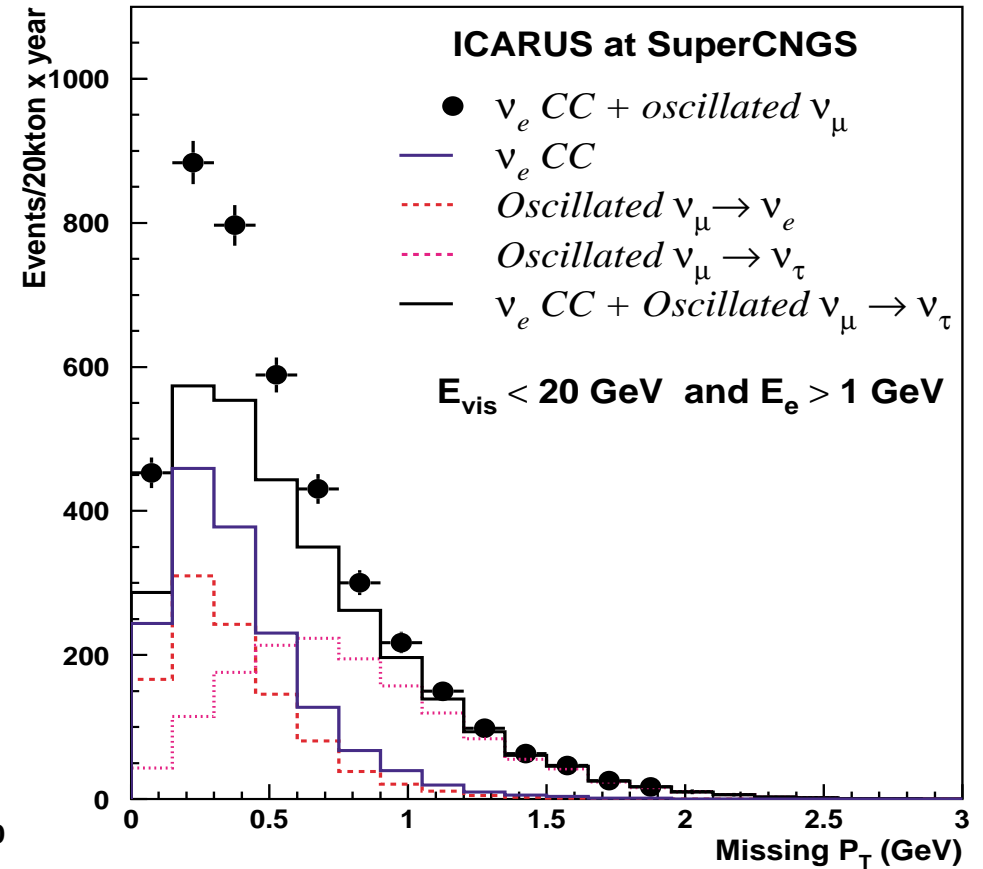
$\Delta m^2_{32} = 3 \times 10^{-3} \text{ eV}^2; \sin^2 2\theta_{23} = 1; \sin^2 2\theta_{13} = 0.05$

**ICARUS 4kton @ LNGS**  
5 years @ super-CNGS

$L = 732 \text{ Km } \Delta m^2 = 3 \times 10^{-3} \text{ eV}^2 \Theta_{23} = 45^\circ \Theta_{13} = 7^\circ$



$L = 732 \text{ Km } \Delta m^2 = 3 \times 10^{-3} \text{ eV}^2 \Theta_{23} = 45^\circ \Theta_{13} = 7^\circ$



*Fully exploit liquid Argon electron reconstruction capabilities!*

# $\Theta_{13}$ sensitivity (CNGS superbeam)

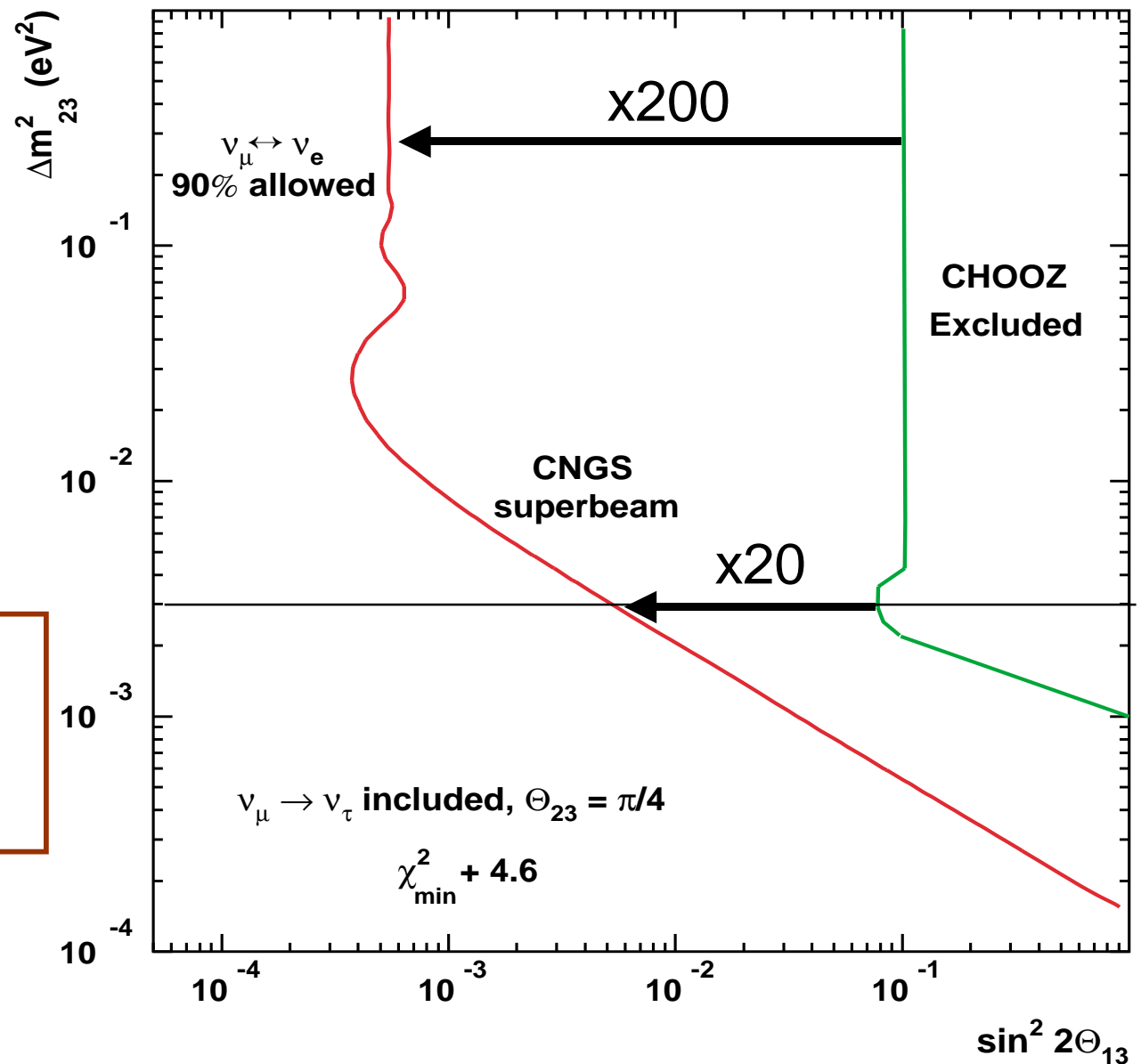
**ICARUS 4kton**

5 years @ super-CNGS

Sensitivity assuming both  $\nu_{\mu} \rightarrow \nu_{\tau}$  and  $\nu_{\mu} \rightarrow \nu_e$  at the same  $\Delta m^2$  (i.e. three family mixing)

**For  $\Delta m^2_{23} = 3 \times 10^{-3} \text{ eV}^2$**

**$\sin^2 2\Theta_{13} < 5 \times 10^{-3}$**



# To parameterize different types of detectors

Exposure (statistical error of signal):

$$D \equiv M_{\text{fiducial}} \times \mathcal{E}_{\text{signal}} \times t_{\text{data-taking}} \left[ \text{kt} \times \text{years} \right]$$

Background (statistical error of signal):

$$f_B \equiv \text{background fraction (relative to CC)}$$

Background (systematic error of background):

$$\sigma(f_B) / f_B \equiv \text{fractional uncertainty}$$

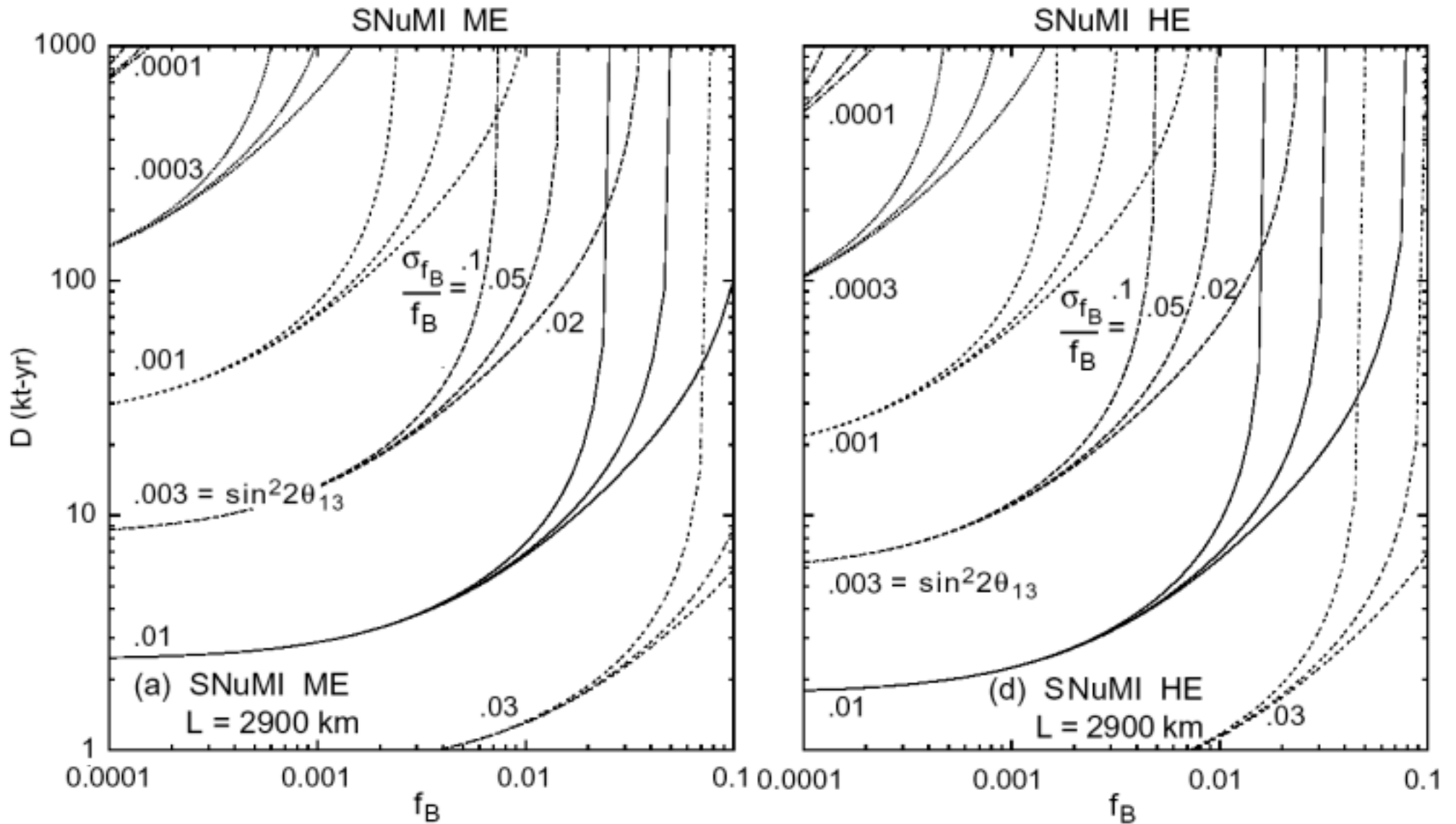
# A detector comparison

Table 4: Detector background rates ( $f_B$ ), signal efficiencies, and unit costs. Water cerenkov backgrounds and efficiencies are neutrino energy dependent: numbers left of the arrows for a 1 GeV beam, numbers right of the arrows for a multi-GeV beam requiring  $y < 0.5$ .

	Water Cerenkov (UNO)	Liquid Argon (ICARUS)	Steel+readout (MINOS)	(THESEUS)	Liquid <sup>f</sup> Scintillator
Signal Efficiency	0.7 → 0.5	0.90	0.33	0.6 <sup>b, g</sup>	0.76
$f_B(\text{NC})$	0.02 → 0.04	0.001	0.01	0.01	< 0.006
$f_B(\text{beam})$	0.002	0.002	0.002	0.002	0.002
$f_B(\tau)$	0 → 0.01	~ 0.005 <sup>c</sup>	0.02 <sup>c</sup>	0 <sup>b</sup>	~ 0.005 <sup>c</sup>
$f_B$	0.02 → 0.05	~ 0.008	0.03	0.01	~ 0.01
Electron cut	$> 0.5 \times E_\nu$	none <sup>d</sup>	1-6 GeV	$> 0.5 E_{\text{vis}}$	$E_{\text{vis}} > 2 \text{ GeV}$
Unit cost (M\$/kt) <sup>a</sup>	2.4	23	10.4	78	59
Mass (kt) / 500 M\$	745	37	85	6.4	260
$D$ (kt-yrs) <sup>e</sup>	2600 → 1860	170	140	19	990

hep-ph/0103052

1.6MW Super-NUMI



*3 $\sigma$  above-background reach contours*



# JHF-Kamioka neutrino project

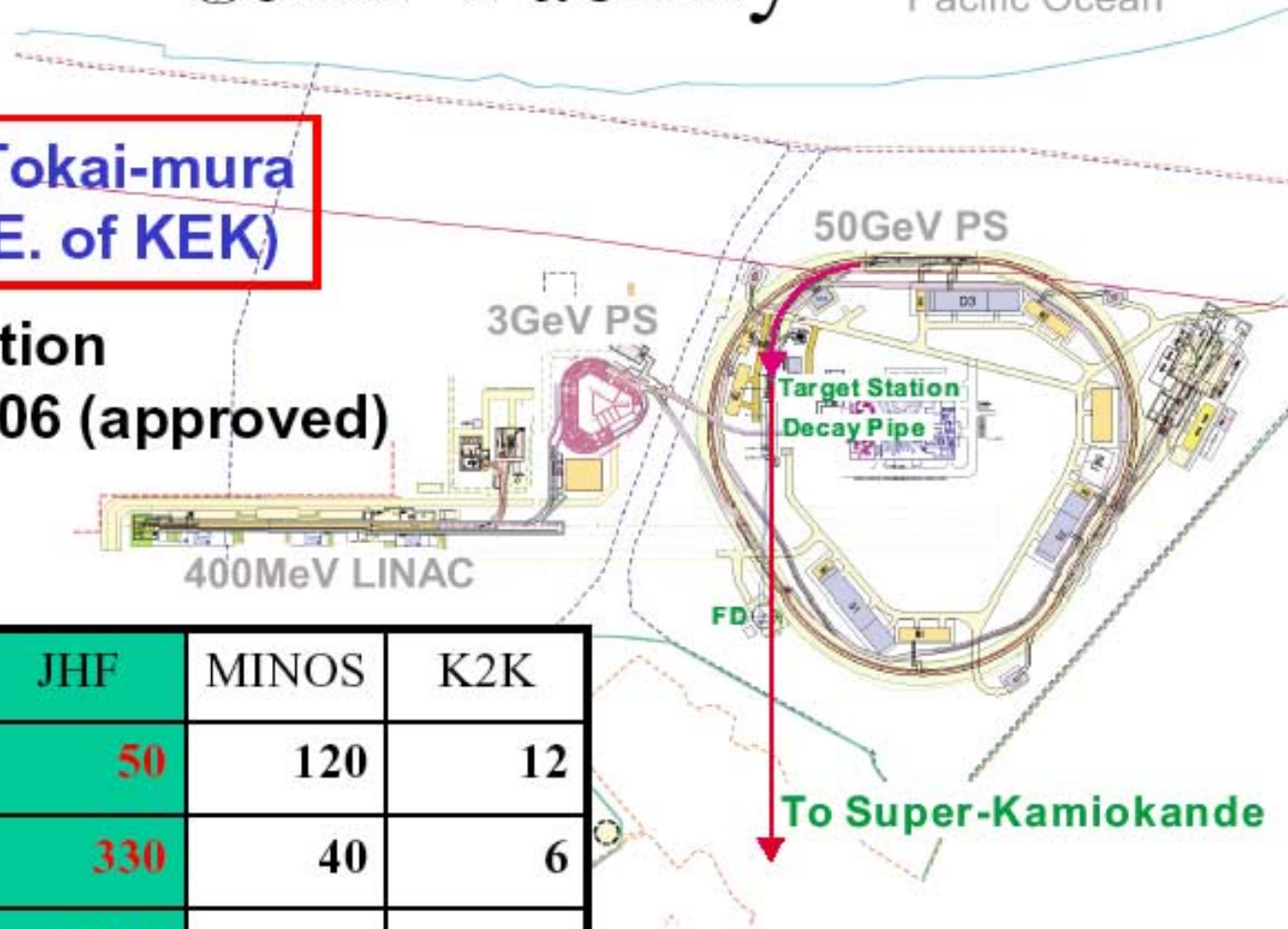
- $L=295\text{km}$ ,  $E_\nu=0.5\sim 2\text{ GeV}$ 
  - match to a Water Cherenkov detector (SK exists)
    - generally easy to build a larger detector
    - less NC  $\pi^0$  background to  $\nu_\mu \rightarrow \nu_e$
    - good  $\nu$  energy reconstruction by QE interaction
    - good particle ID capability
  - small matter effect (difficult to see the sign of  $\Delta m_{23}^2$ , but easier to look for CP violation.)
  - match to a size of Japan with the existing facilities

# JHF Facility

Pacific Ocean

**JAERI@Tokai-mura  
(60km N.E. of KEK)**

**Construction  
2001 ~ 2006 (approved)**



	JHF	MINOS	K2K
E(GeV)	<b>50</b>	120	12
Int.( $10^{12}$ ppp)	<b>330</b>	40	6
Rate(Hz)	<b>0.29</b>	0.53	0.45
Power(MW)	<b>0.77</b>	0.41	0.0052

$10^{21}$ POT(130day)  $\equiv$  "1 year"  
8

*Nakaya, NUFACT01*

Neutrino beam and detectors:



**Phase-I (0.77MW + Super-K)**

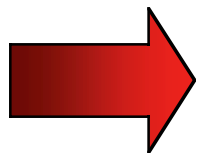
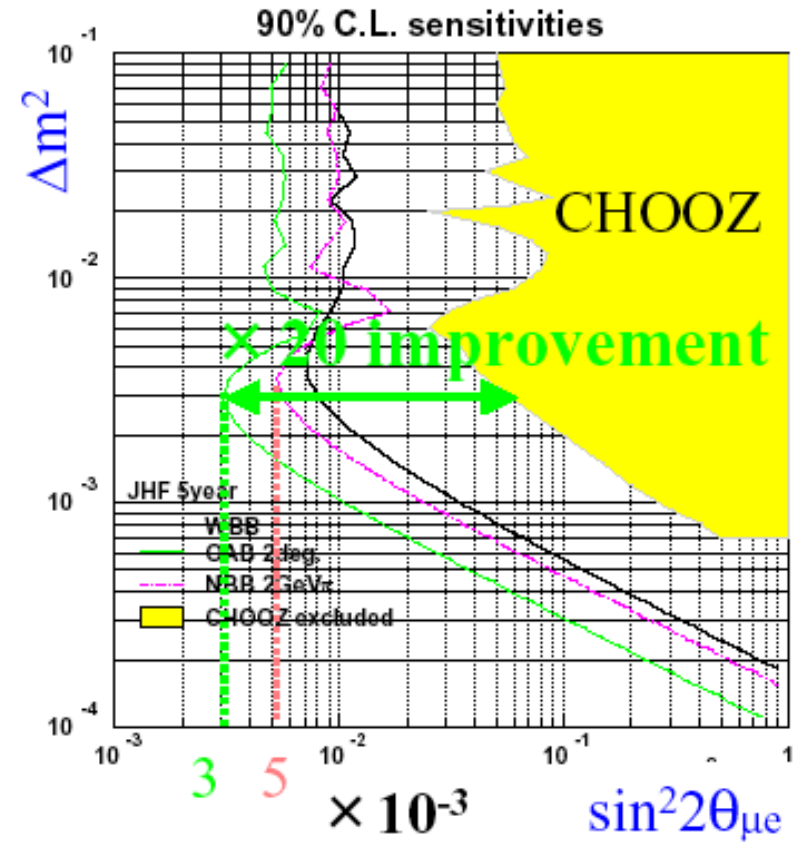
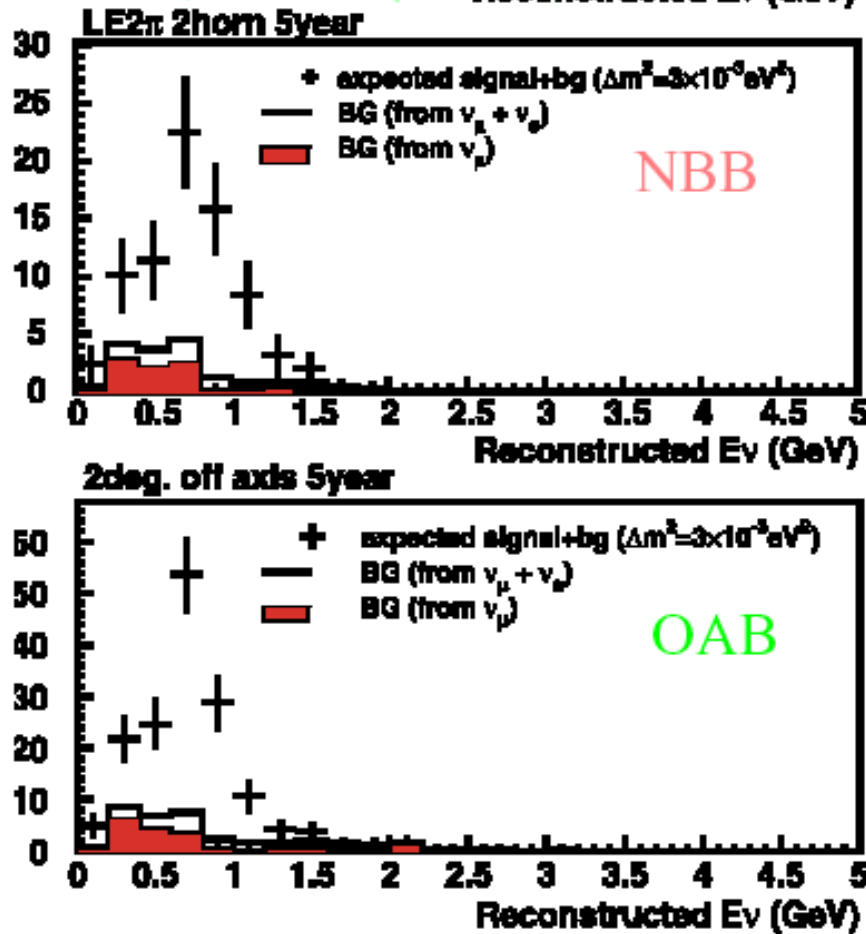
**Phase-II (4MW+Hyper-K)  $\sim$  Phase-I  $\times$  200**

*Nakaya, NUFACT01*

# $\nu_e$ appearance

Background rejection against NC  $\pi^0$  is improved.

$\sin^2 2\theta_{\mu e} = 0.05$  ( $\sin^2 2\theta_{\mu e} \equiv 0.5 \sin^2 2\theta_{13}$ )



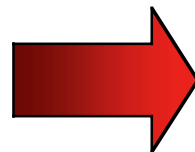
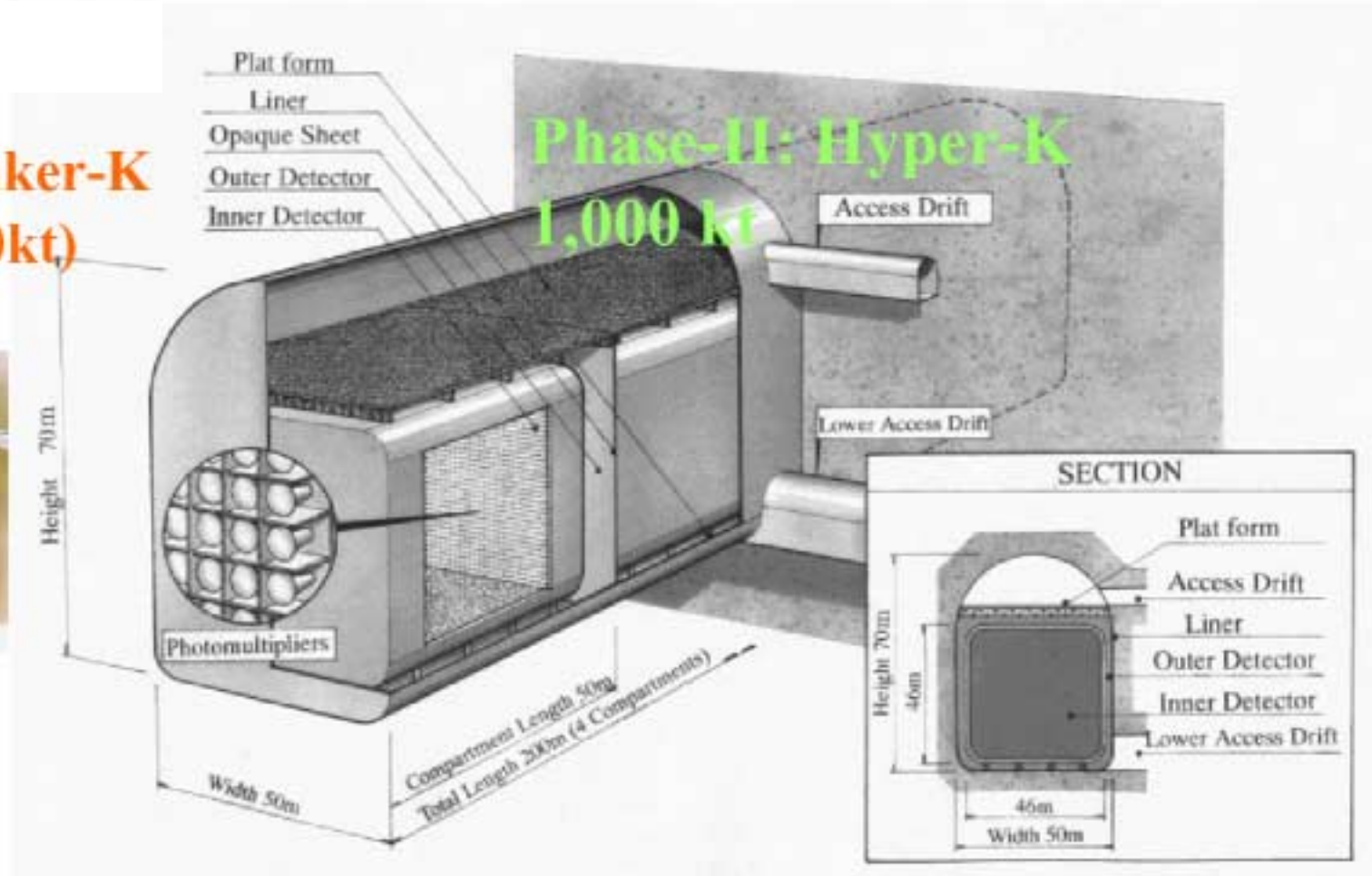
$\sin^2 2\theta_{13} > 6 \times 10^{-3}$

Ph2me, Ph2he<sup>17</sup>  
 A.Para, hep-ph/0005012)

*Nakaya, NUFACT01*

Phase II: *upgraded 4MW machine coupled to Mton Water detector*

**Phase-I: Suker-K**  
**22.5kt (50kt)**



$$\sin^2 2\theta_{13} > 10^{-3}$$

*Nakaya, NUFACT01*

# CP Violation Study

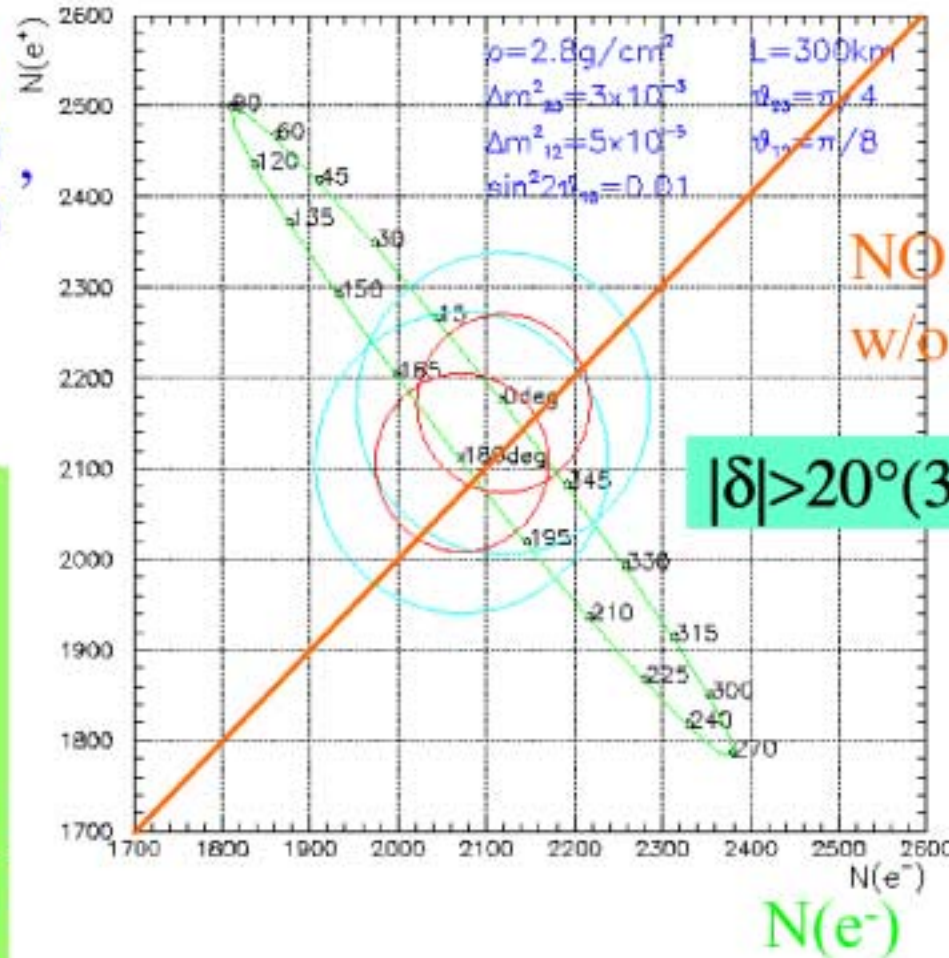
4 MW machine + 1000 kt Water  
2 years  $\nu$  and 6 years  $\bar{\nu}$

- Compare  $\nu_{\mu} \rightarrow \nu_e$  with  $\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$

$$\Delta m_{12}^2 = 5 \times 10^{-5} \text{eV}^2, \\ \Delta m_{23}^2 = 3 \times 10^{-3} \text{eV}^2, \\ \sin^2 2\theta_{13} = 0.01 \\ \theta_{23} = \pi/4, \theta_{12} = \pi/8$$

Asymmetry

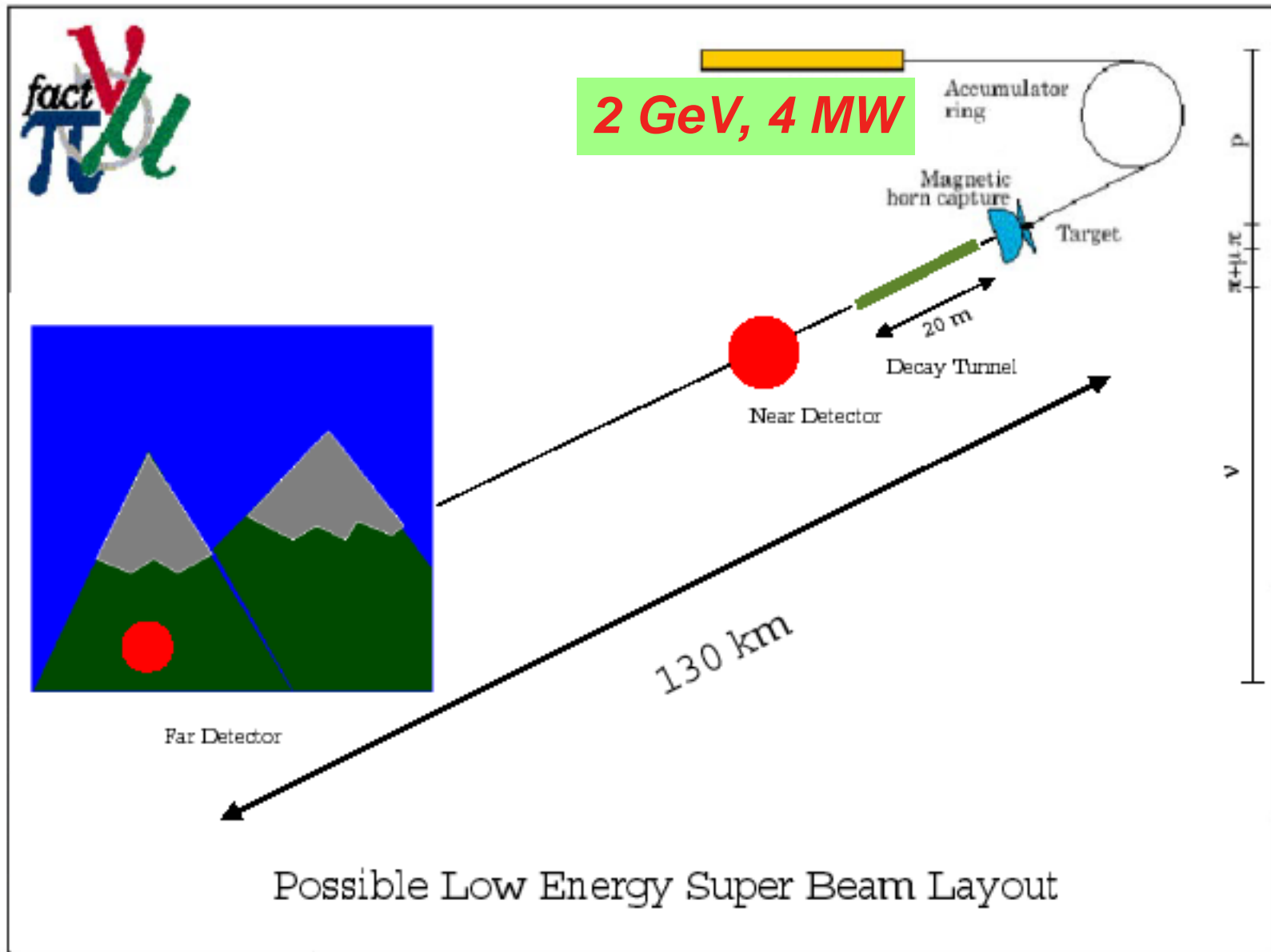
$$\equiv \frac{N(e^+) - N(e^-)}{N(e^+) + N(e^-)} \\ \approx \frac{\sim 2000 - \sim 2000}{\sim 2000 + \sim 2000} \\ \approx 0.02$$



NO CP violation  
w/o matter effect.

$|\delta| > 20^\circ$  (3 $\sigma$  discovery)

CERN superbeam option: Requires the SPL (Superconducting Proton Linac)



*Mezzetto, NUFACT01*

## Three detectors scenario

### Water Čerenkov detector á la SuperK (40% PMT coverage) with 40 kton fiducial mass

- $\epsilon_s \sim 70\%$  (from a full simulation + analysis)
- $f_B(\pi^0/e) \sim 0.002$  (full simulation + analysis using energy flow fitter to identify  $\pi^0$ )
- $f_B(\mu/e) \sim 0.001$  (full simulation)
- $f_B(\text{Beam}) \sim 0.003$  (full simulation of beam)

$f_B$  are normalized to the  $\nu_\mu$  CC rate

### Liquid scintillator á la MiniBoone (10% PMT coverage) with 40 kton fiducial mass

- $\epsilon_s \sim 50\%$  (using MiniBoone numbers)
- $f_B(\pi^0/e) \sim 0.001$  (using MiniBoone numbers)
- $f_B(\mu/e) \sim 0.001$  (using MiniBoone numbers)
- $f_B(\text{Beam}) \sim 0.003$  (full simulation of beam)

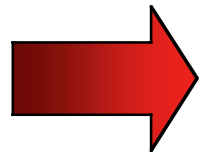
### Water Čerenkov detector á la SuperK with 400 kton fiducial mass

- Extrapolated from the 40 kton detector

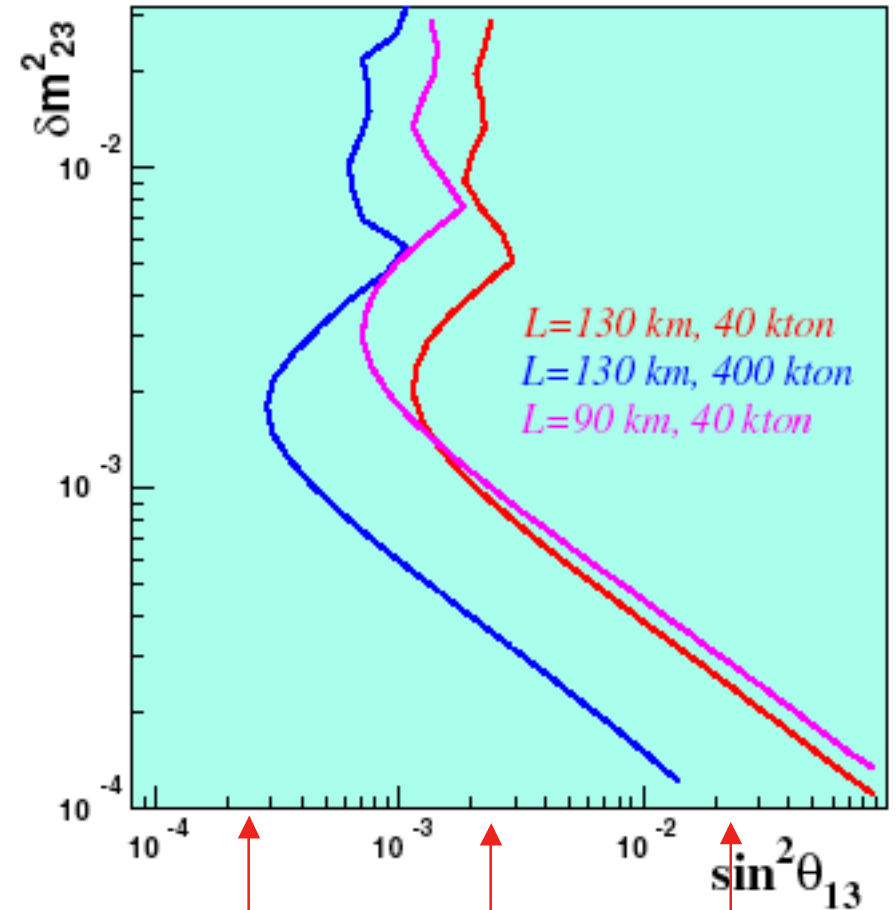
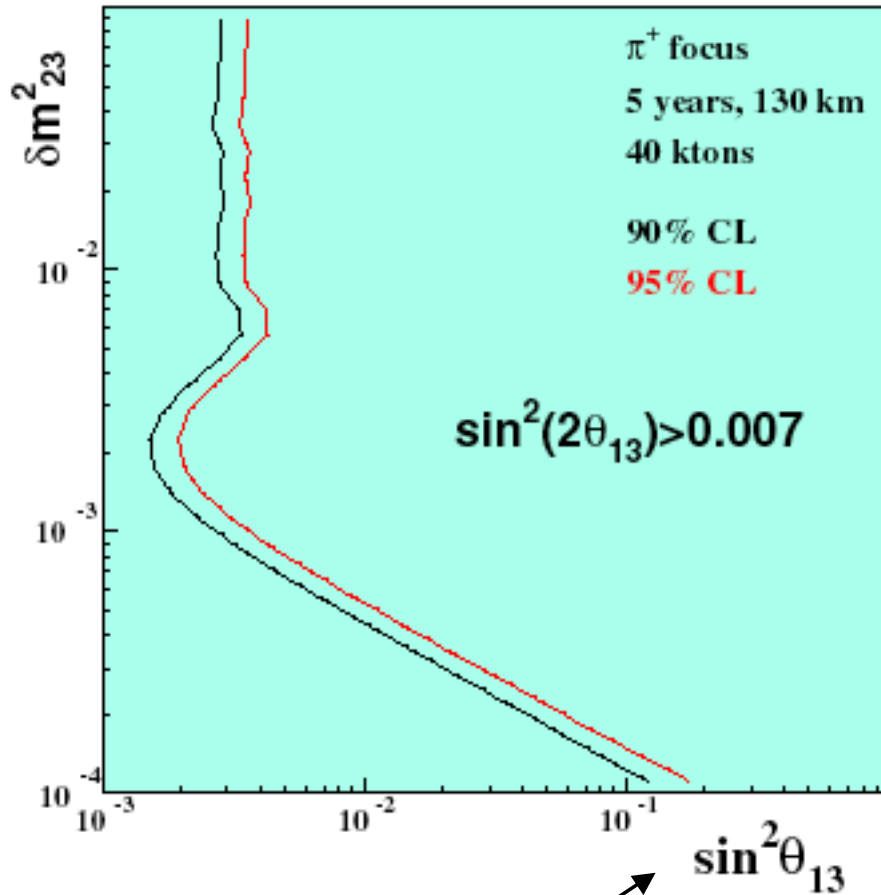


Expected event rate for 200 kt x year exposure:

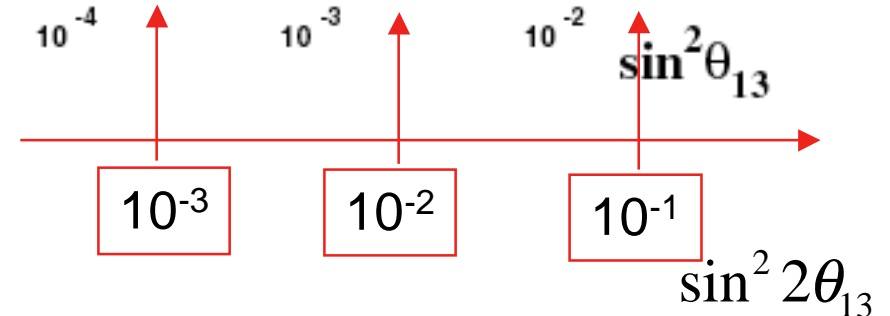
Water Čerenkov, $\pi^+$ focused beam						
Channel	Initial sample	Visible events	Single-ring $100 - 450 \text{ MeV}$	Tight PID	No $\mu \rightarrow e$	$m_{\gamma\gamma} < 45$ ( $\text{MeV}/c^2$ )
$\nu_{\mu}$ CC	3250	887	578	5.5	2.5	1.5
$\nu_e$ CC	18	12	8.2	8.0	8.0	7.8
NC	2887	37	8.7	7.7	7.7	7.5
$\nu_{\mu} \rightarrow \nu_e$		82.4%	77.2%	76.5%	70.7%	70.5%
Water Čerenkov, $\pi^-$ focused beam						
$\bar{\nu}_{\mu}$ CC	539	186	123	2.3	0.7	0.7
$\bar{\nu}_e$ CC	4	3.3	3.	2.7	2.7	2.7
NC	687	11.7	3.3	3.	3.	0.3
$\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e$		79.3%	74.1%	74.0%	67.1%	67.1%



$$\sin^2 2\theta_{13} > 6 \times 10^{-3} \quad (40kt)$$



Beware:  $\sin^2 2\theta_{13} \approx 4 \sin^2 \theta_{13}$



# The oscillation physics program at the NF

$$\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu$$

$$\nu_\mu \rightarrow \nu_e$$

appearance

$$\nu_\mu$$

disappearance

$$\nu_\mu \rightarrow \nu_\tau$$

appearance

$$\bar{\nu}_e$$

disappearance

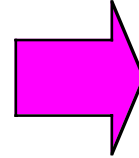
$$\bar{\nu}_e \rightarrow \bar{\nu}_\mu$$

appearance

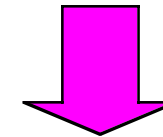
$$\bar{\nu}_e \rightarrow \bar{\nu}_\tau$$

appearance

Plus their charge conjugates with  $\mu^+$  beam



Ideal detector should be able to measure **12 different processes as a function of  $L$  and  $E_\nu$**



$$\begin{cases} \nu_\ell N \rightarrow \ell^- + \text{hadrons} \\ \bar{\nu}_\ell N \rightarrow \ell^+ + \text{hadrons} \end{cases}$$

$$\begin{cases} \nu_\ell N \rightarrow \nu_\ell + \text{hadrons} \\ \bar{\nu}_\ell N \rightarrow \bar{\nu}_\ell + \text{hadrons} \end{cases}$$

1. **Particle ID**: charged lepton tags **incoming neutrino flavor**

2. **Charge ID**: sign of lepton charge tags **helicity** of incoming neutrino

3. **Energy resolution**: Reconstructed event energy is  **$E_\nu = E_\ell + E_{had}$**

4. **Various baselines  $L$**  could help for detector systematics

# The Neutrino Factory



Roughly as many  $\nu_e$ 's as  $\nu_\mu$ 's

P. Lipari, hep-ph/0102046

Flux scales as  $E_\mu^2/L^2$

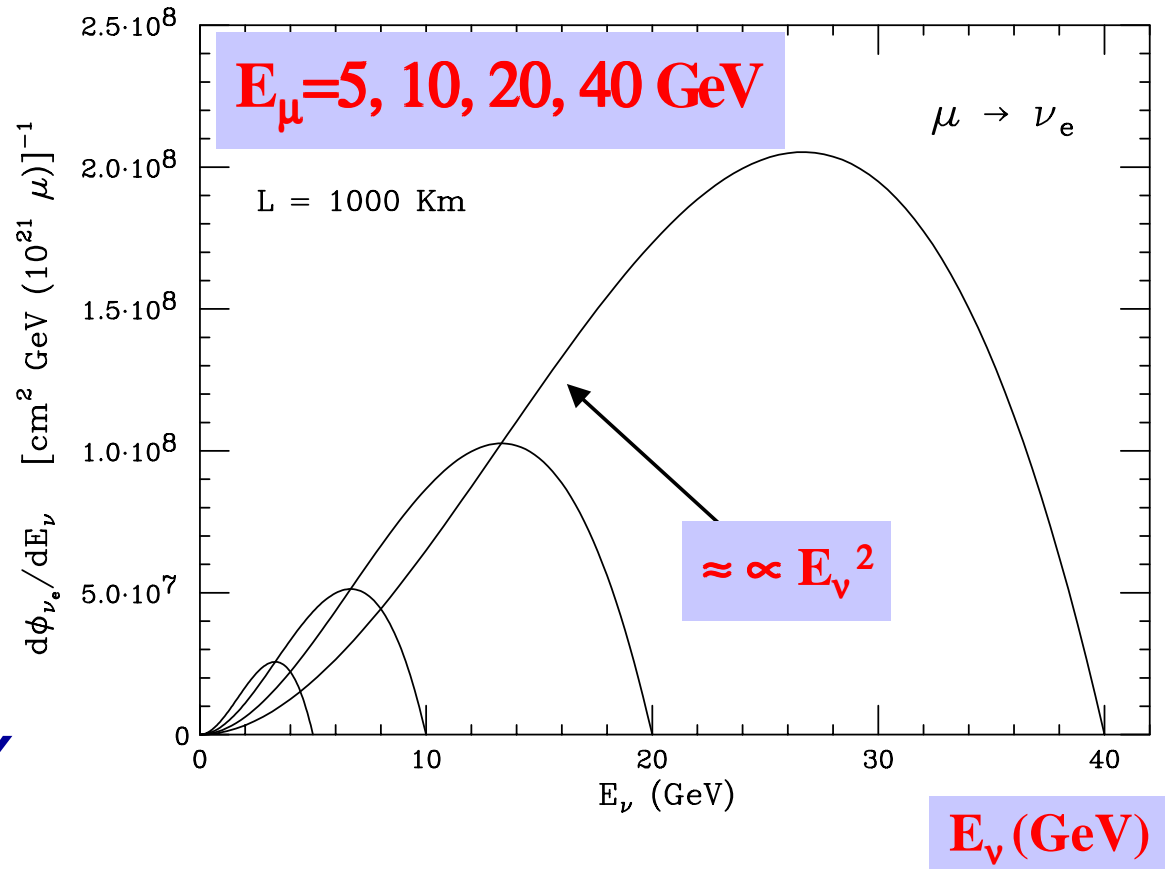
Total event rate scales as  $\approx E_\mu^3/L^2$

A very important feature!

The generally adopted consensus (see later)  $\Rightarrow$

*high energy  $\nu$ -factory*

$E_\mu = O(30 \text{ GeV})$



$$\frac{dN}{dx} \propto x^2(1-x)$$

$$x \equiv E_\nu / E_\mu$$

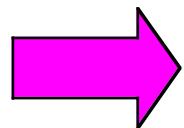
# Predicted event rates at a Neutrino Factory

FNAL-FN-692, Apr 2000

$10^{20}$   $\mu^-$  decays

No oscillations assumed

Experiment		Baseline (km)	$\langle E_{\nu_\mu} \rangle$ (GeV)	$\langle E_{\bar{\nu}_e} \rangle$ (GeV)	$N(\nu_\mu \text{ CC})$ (per kt-yr)	$N(\bar{\nu}_e \text{ CC})$ (per kt-yr)
NuMI	Low energy	732	3	—	458	1.3
	Medium energy	732	6	—	1439	0.9
	High energy	732	12	—	3207	0.9
CNGS		732	17	—	2714	1.4
Muon ring	$E_\mu$ (GeV)					
	10	732	7.5	6.6	1400	620
	20	732	15	13	12000	5000
	50	732	38	33	$1.8 \times 10^5$	$7.7 \times 10^4$
Muon ring	$E_\mu$ (GeV)					
	10	2900	7.6	6.5	91	41
	20	2900	15	13	740	330
	50	2900	38	33	11000	4900
Muon ring	$E_\mu$ (GeV)					
	10	7300	7.5	6.4	14	6
	20	7300	15	13	110	51
	50	7300	38	33	1900	770



However, in addition to the increased neutrino flux, ambitious oscillation physics program requires detectors in the **10's kton** range to perform experiment with baselines  **$L \approx 1000$ 's km**

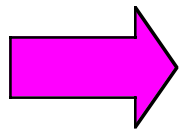
# The goal: detect $\mu^+$ , $\mu^-$ , $e^+$ , $e^-$ , $\tau^+$ , $\tau^-$ and NC !

★ Particle ID:  $\Rightarrow$  *via CC interactions*

- **Muons:** *straight-forward*, look for penetrating particles, but beware  $\pi^\pm, K^\pm$  and charm decays
- **Electrons:** *harder*, look for large & “short” energy deposition, need good granularity for  $e/\pi^0$  separation
- **Taus:** *hardest*, “kink” or kinematical methods (statistical separation),  $\tau \rightarrow \text{hadrons} + \nu$  (Br $\approx$ 60%) look like “NC”

★ Charge ID:  $\Rightarrow$  *via magnetic analysis*

- **Muons:** *easy*, muon spectrometer downstream or fully magnetized target
- **Electrons:** *hardest*, need to measure significantly precisely the bending in B-field before start of e.m. shower
- **Taus:** easy for  $\tau \rightarrow \mu\nu\nu$  (Br $\approx$ 18%), otherwise *difficult*

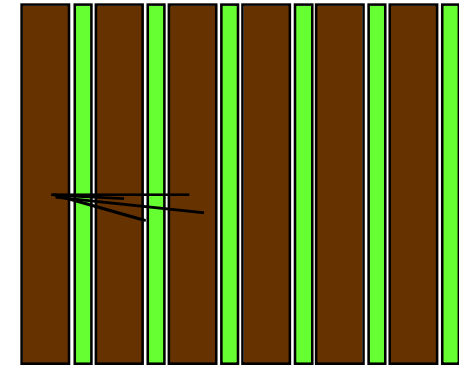


*This has to be implemented on multi-kton detectors... various choices & optimizations considered.*

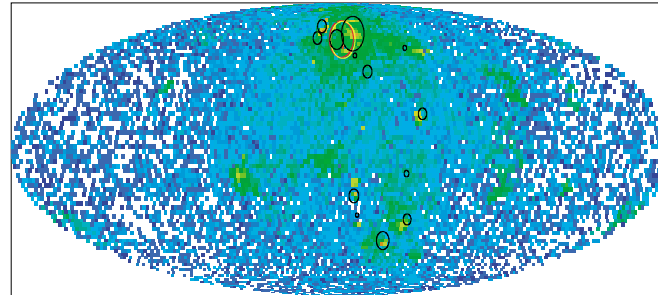
# The typical detectors

★ See also [arXiv:hep-ph/0106088](https://arxiv.org/abs/hep-ph/0106088)

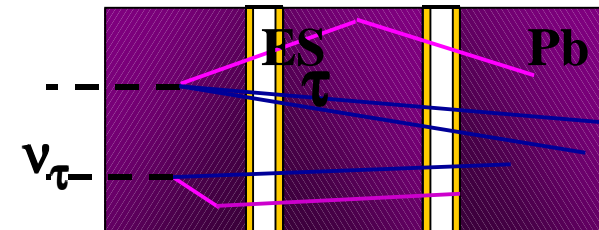
1. Magnetized iron-scintillator sandwich



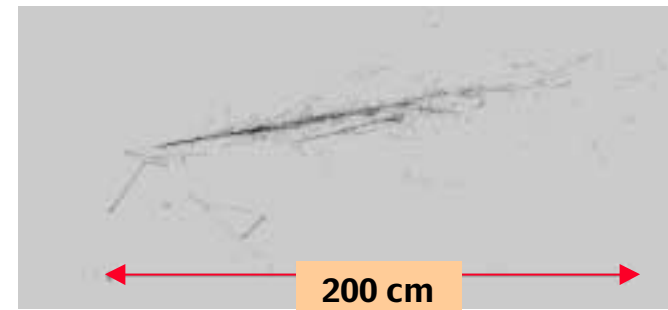
2. Large water Cerenkov



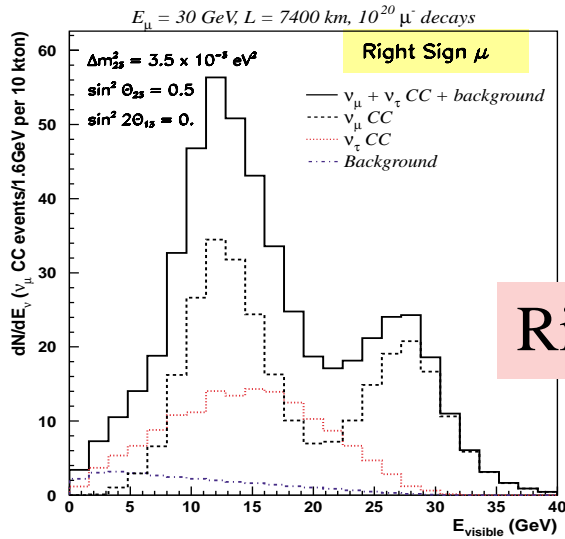
3. Emulsion/target sandwich



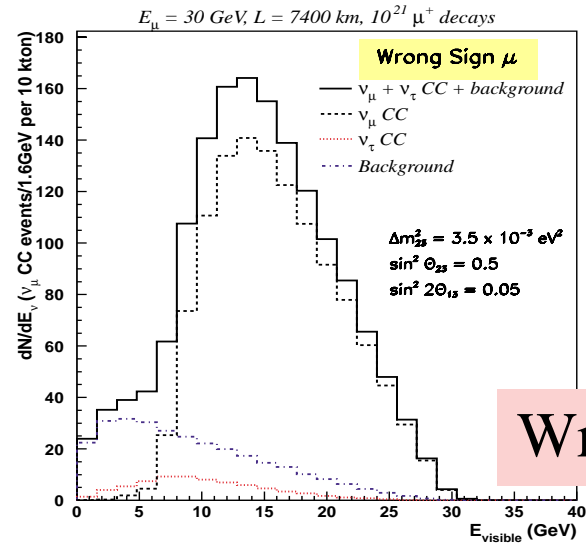
4. Liquid argon imaging TPC



# Over-constraining the parameters (I)

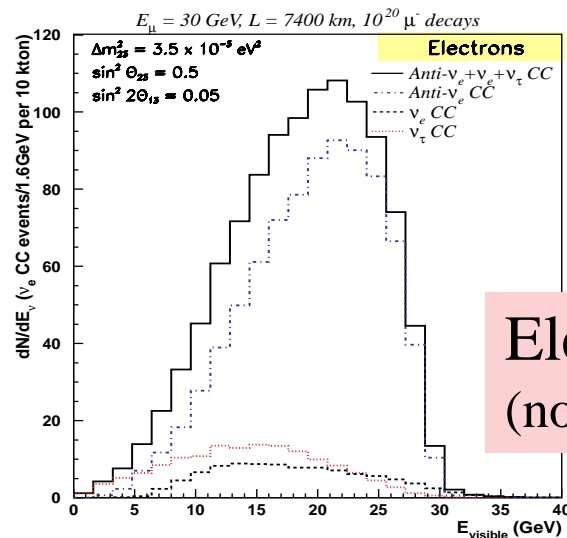


Right sign  $\mu$

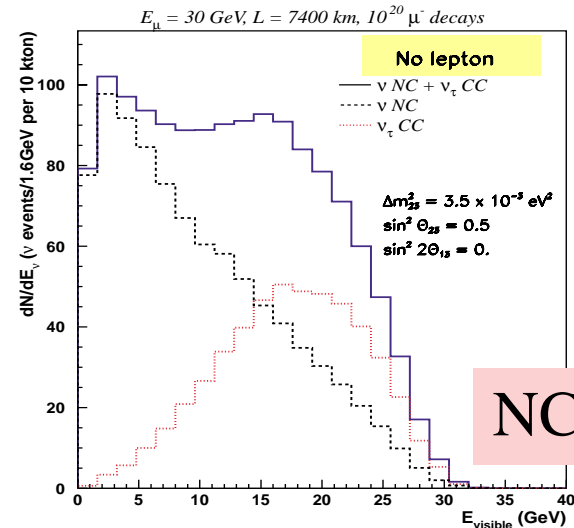


Wrong sign  $\mu$

**ICARUS-like  
10kton**



Electrons  
(no charge info)



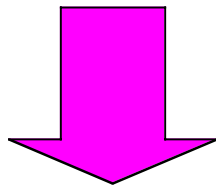
NC-like

*Combining all classes  $\Rightarrow$  (over-constrained) sensitivity to all oscillations!*



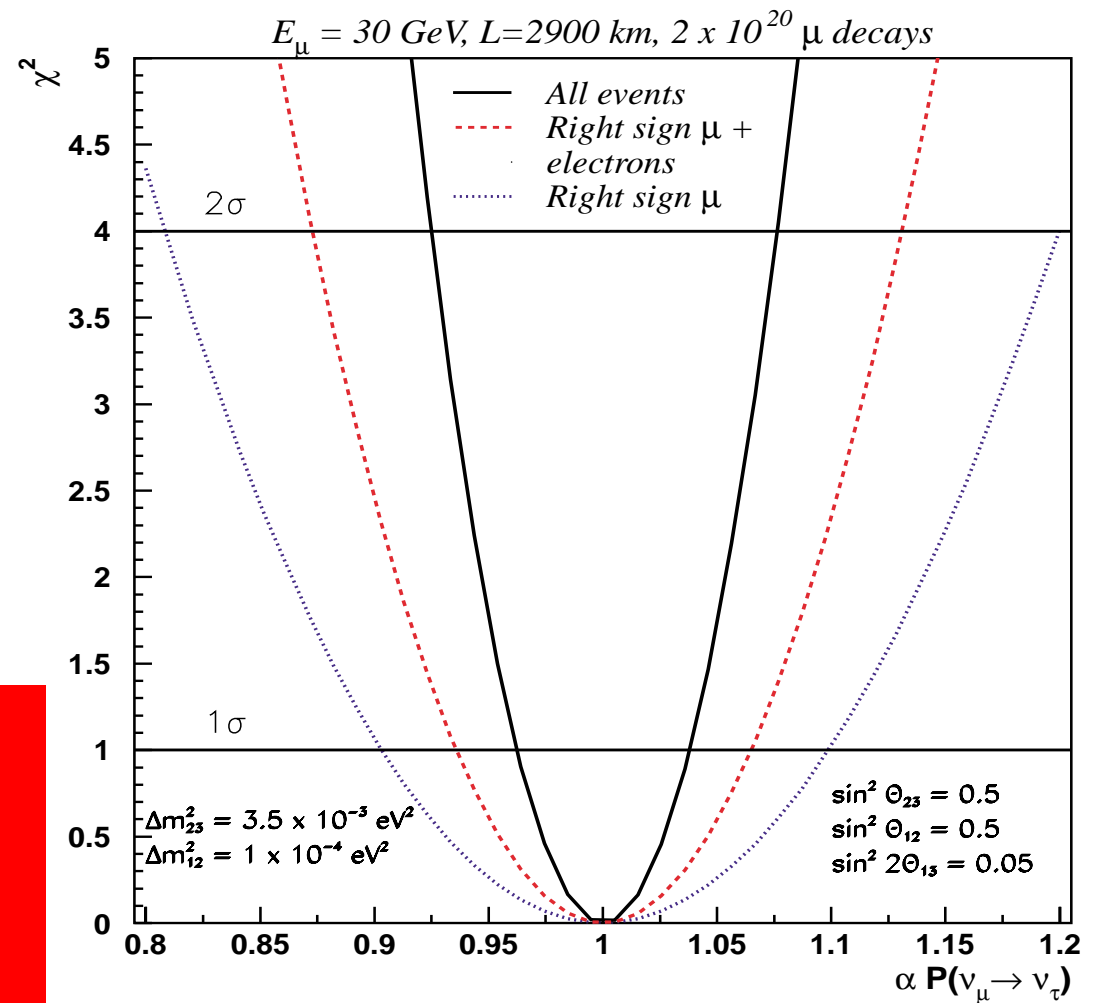
# Over-constraining the parameters (II)

- \* Check consistency between different observed oscillation processes
- \* Proof/rule out the existence of sterile neutrinos
- \* **First observation of  $\nu_e \rightarrow \nu_\tau$**



**Ability to detect  $\tau$  appearance is crucial**

## ICARUS-like 10kton



A. Bueno et.al. , Nucl.Phys.B589 (2000) 577

# Measurement/limit on $\Theta_{13}$

**Wrong sign muons** are  
the ideal way to detect  
 $\nu_e \rightarrow \nu_\mu$  oscillations

**ICARUS-like 10kton  
E=30 GeV**

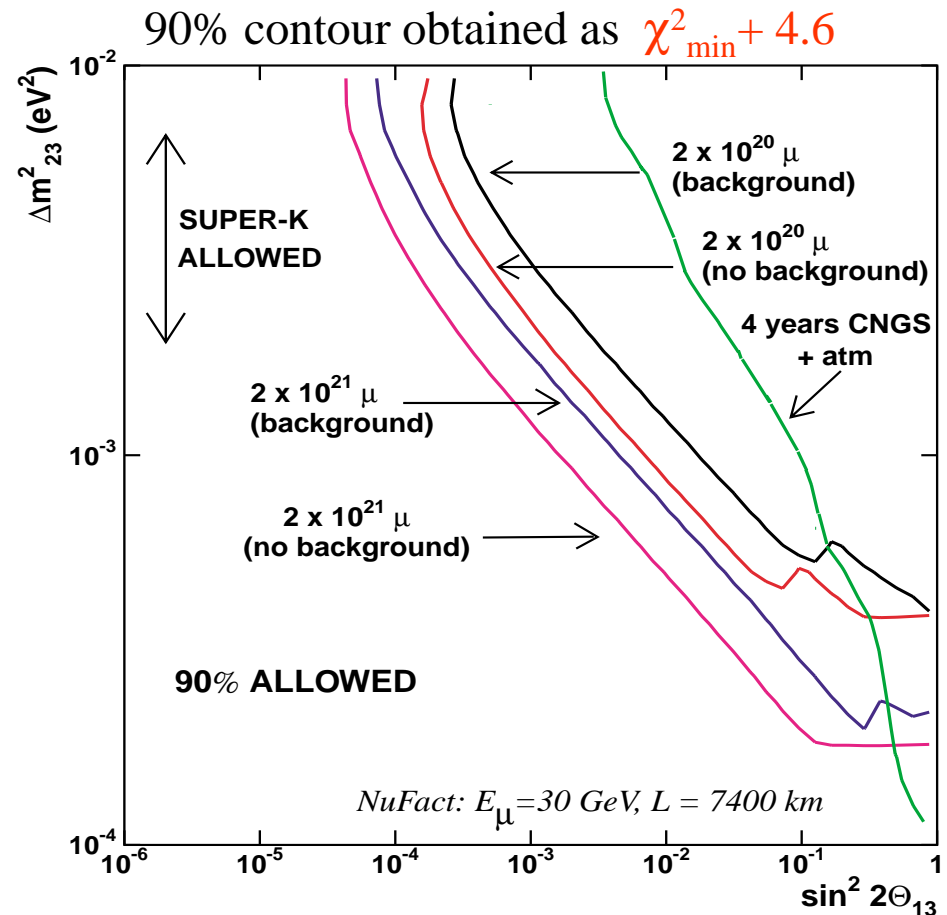
Assuming  $\Delta m_{23}^2 > 0 \Rightarrow$  *Matter enhanced  $\nu$  oscillation*  $\Rightarrow$  better measurement at longer distances

$$\delta(\sin^2 2\Theta_{13}) = 15\% \quad (L=2900 \text{ km})$$

$$\delta(\sin^2 2\Theta_{13}) = 10\% \quad (L=7400 \text{ km})$$

for  $\sin^2 2\Theta_{13} = 0.05$

$$\sin^2 2\Theta_{13} > 10^{-4}$$



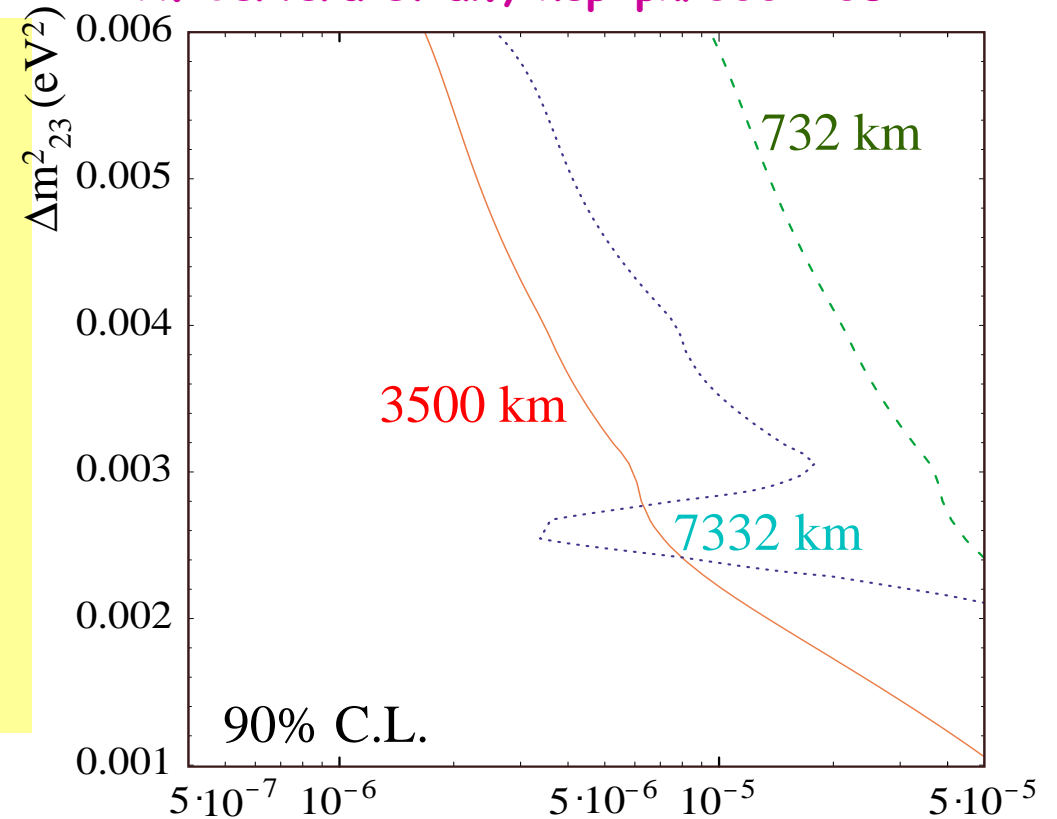
A. Bueno et.al. , Nucl.Phys.B589 (2000) 577

# Ultimate sensitivity on $\Theta_{13}$

- 40 kT Fe-Scintillator detector
- $E_\mu = 50$  GeV
- $10^{21}$   $\mu$  decays
- Include background and detector efficiencies
- Tight cuts to suppress backgrounds (e.g. charm)

$$\sin^2 2\theta_{13} \gtrsim 10^{-5}$$

A. Cervera et al., hep-ph/0002108



Beware:  $\sin^2 2\theta_{13} \approx 4 \sin^2 \theta_{13}$

## Observing effects related to the $\delta$ -phase

Optimizing the search for a complex phase in the leptonic mixing matrix far from trivial

- A priori, the effect depends on **L** and **E** in a complicated way (In vacuum, the scaling of the effect with **L/E** can help an intuitive understanding of the oscillation behavior)
- Measurement precision depends on **practical limits** on machine power, maximal energy/flux, detector mass

The choice of the baseline is critical: at the time of the Neutrino Factory, there will be already experiments located at a distance of **250 km** from JHF and **730 km** from CERN and FNAL; if **new sites** are really needed, due to physics considerations, that would require **major new investments for sites and detectors**.

# $\nu_e \rightarrow \nu_\mu$ oscillation probability

Following the conventional formalism for leptonic mixing, CP-/T-violating effects are observed in *appearance transitions involving the first family*. Therefore, transitions between electron and muon flavors are clearly favored.

These probabilities are composed of three terms:

$$\begin{aligned}
 P(\nu_e \rightarrow \nu_\mu) = P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) = & \\
 4c_{13}^2 [\sin^2 \Delta_{23} s_{12}^2 s_{13}^2 + c_{12}^2 (\sin^2 \Delta_{13} s_{13}^2 s_{23}^2 + \sin^2 \Delta_{12} s_{12}^2 (1 - (1 + s_{13}^2) s_{23}^2))] & \quad \text{Independent of } \delta \\
 -1/2 c_{13}^2 \sin^2 \theta_{12} s_{13} \sin^2 \theta_{23} \cos \delta [\cos^2 \Delta_{13} - \cos^2 \Delta_{23} - 2 \cos^2 \theta_{12} \sin^2 \Delta_{12}] & \\
 +1/2 c_{13}^2 \sin \delta \sin 2\theta_{12} s_{13} \sin^2 \theta_{23} [\sin^2 \Delta_{12} - \sin^2 \Delta_{13} + \sin^2 \Delta_{23}] & \quad \text{CP-even}
 \end{aligned}$$

CP-odd

Beat of frequencies

## *To fix numbers*

*Unless otherwise specified, we assume following parameters:*

$$\Delta m_{32}^2 = 3 \times 10^{-3} eV^2,$$

$$\Delta m_{12}^2 = 1 \times 10^{-4} eV^2,$$

$$\sin^2 \theta_{23} = 0.5,$$

$$\sin^2 \theta_{12} = 0.5,$$

$$\sin^2 2\theta_{13} = 0.05$$

*Consistent with atmospheric data and LMA solar data  
(assuming maximal mixing).*

# Looking for effects of $\delta$ !

$$P(\nu_e \rightarrow \nu_\mu)$$

Effect “largest” when  
beat of three sin-  
functions:

$$\Delta m^2_{21} (L/4E_\nu) \approx 1$$

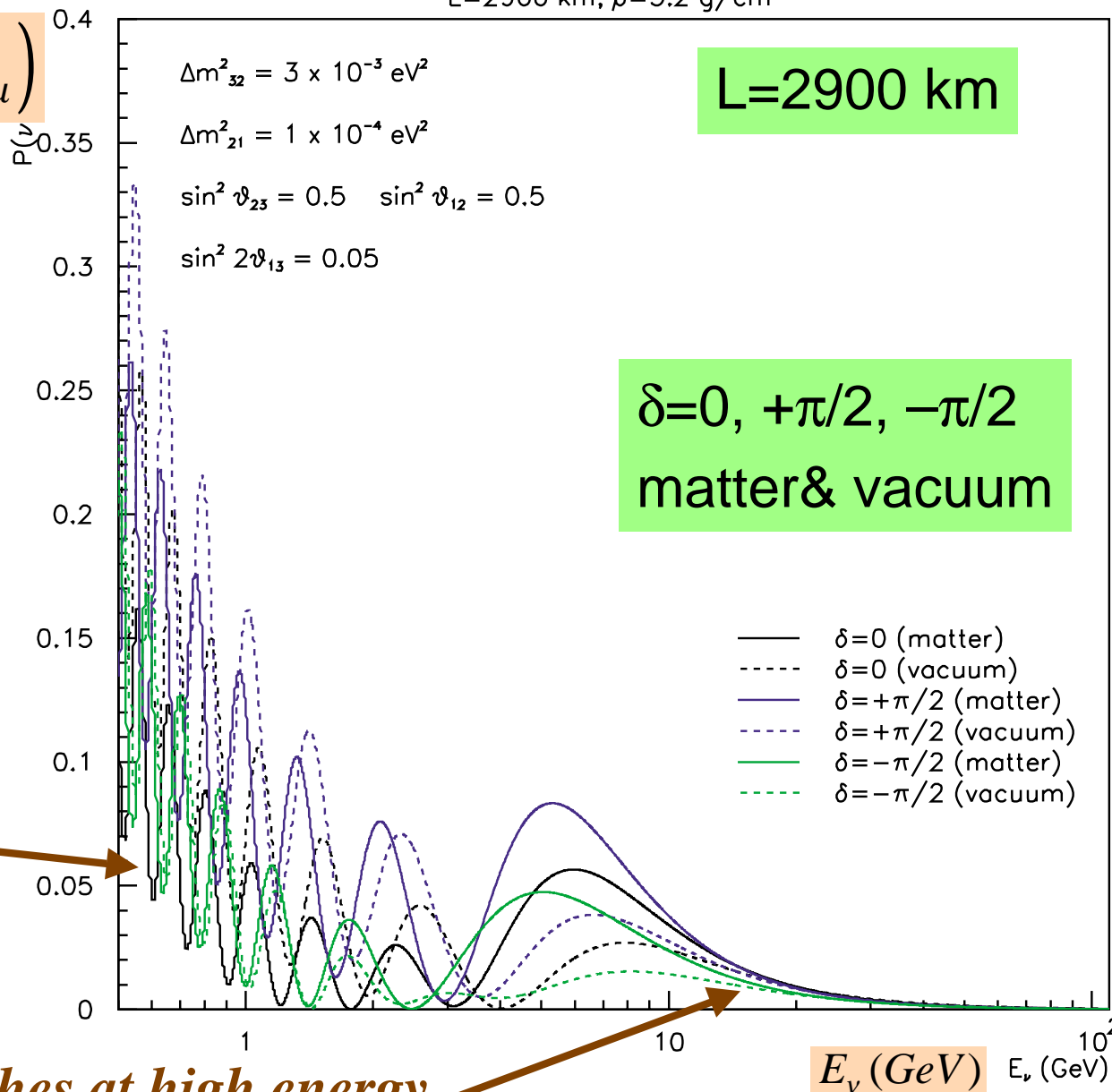
&

$$\Delta m^2_{32} (L/4E_\nu) > 1$$

$\Rightarrow L/E$  of “solar” !

Effect vanishes at high energy

$L=2900 \text{ km}, \rho=3.2 \text{ g/cm}^3$

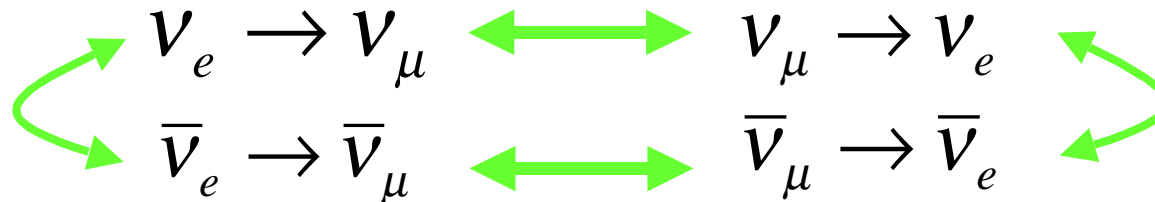


# The effect is

For a complex mixing matrix (in vacuum)

$$\begin{aligned}
 P(\nu_e \rightarrow \nu_\mu) = P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) = & 4c_{13}^2 [\sin^2 \Delta_{23} s_{12}^2 s_{13}^2 + c_{12}^2 (\sin^2 \Delta_{13} s_{13}^2 s_{23}^2 + \sin^2 \Delta_{12} s_{12}^2 (1 - (1 + s_{13}^2) s_{23}^2))] \\
 & - 1/2 c_{13}^2 \sin^2 \theta_{12} s_{13} \sin^2 \theta_{23} \cos \delta [\cos^2 \Delta_{13} - \cos^2 \Delta_{23} - 2 \cos^2 \theta_{12} \sin^2 \Delta_{12}] \\
 & + 1/2 c_{13}^2 \sin \delta \sin 2\theta_{12} s_{13} \sin^2 \theta_{23} [\sin^2 \Delta_{12} - \sin^2 \Delta_{13} + \sin^2 \Delta_{23}]
 \end{aligned}$$

1. A **precision measurement of the transition probability** can yield information on the  **$\delta$ -phase** provided we know all other parameters very precisely!  
**OR**
2. We can try to **directly measure a difference of probability between neutrinos or antineutrinos** (T or CP-violation)



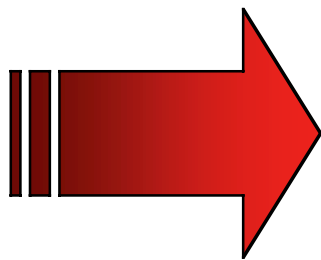


# *In fact*

In vacuum

$$\Delta\text{CP} = \Delta\text{T} =$$

$$2 \cos\theta_{13} \sin\delta \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \times \\ \sin(\Delta m_{12}^2 L/4E_\nu) \sin(\Delta m_{13}^2 L/4E_\nu) \sin(\Delta m_{23}^2 L/4E_\nu)$$



1. Only depends on  $\sin\delta$   
and
2. Only depends on  $L/E_\nu$

## Comment with respect to $\theta_{13}$

$$P(\nu_e \rightarrow \nu_\mu) =$$

$$4c_{13}^2 [\sin^2 \Delta_{23} s_{12}^2 s_{13}^2 + c_{12}^2 (\sin^2 \Delta_{13} s_{13}^2 s_{23}^2 + \sin^2 \Delta_{12} s_{12}^2 (1 - (1 + s_{13}^2) s_{23}^2))] -$$

$$1/2 c_{13}^2 \sin^2 \theta_{12} s_{13} \sin^2 \theta_{23} \cos \delta [\cos^2 \Delta_{13} - \cos^2 \Delta_{23} - 2 \cos^2 \theta_{12} \sin^2 \Delta_{12}] +$$

$$1/2 c_{13}^2 \sin \delta \sin 2\theta_{12} s_{13} \sin^2 \theta_{23} [\sin^2 \Delta_{12} - \sin^2 \Delta_{13} + \sin^2 \Delta_{23}]$$

$$\Delta CP = \Delta T \propto \sin \theta_{13}$$

$$P \propto \sin^2 \theta_{13}$$

$$\left. \begin{array}{l} \Delta CP = \Delta T \propto \sin \theta_{13} \\ P \propto \sin^2 \theta_{13} \end{array} \right\} \frac{\Delta CP}{\sqrt{P}} \propto \frac{\sin \theta_{13}}{\sqrt{\sin^2 \theta_{13}}} \text{ independent of } \theta_{13}$$

***This is true as long as***

1. we have events in the detector
2. we can neglect the second term in the probability  
(cannot be done for  $\theta_{13} \rightarrow 0$ )

# Matter effects

$$\sin^2 2\theta_m(D) = \frac{\sin^2 2\theta}{\sin^2 2\theta + \left( \pm \frac{D}{\Delta m^2} - \cos 2\theta \right)^2}$$

+ for neutrinos  
- for antineutrinos

$$\lambda_m = L \times \sqrt{\sin^2 2\theta + \left( \pm \frac{D}{\Delta m^2} - \cos 2\theta \right)^2}$$

where

$$D(E_\nu) = 2\sqrt{2}G_F n_e E_\nu \approx 7.56 \times 10^{-5} \text{ eV}^2 \left( \frac{\rho}{\text{gcm}^{-3}} \right) \left( \frac{E}{\text{GeV}} \right)$$

For example, for neutrinos:

**Resonance:**  $D \approx \Delta m^2 \cos 2\theta$   $\longrightarrow$   $\sin^2 2\theta_m(D) \approx 1$

**Suppression:**  $D > 2\Delta m^2 \cos 2\theta$   $\longrightarrow$   $\sin^2 2\theta_m(D) < \sin^2 2\theta$

*Mixing in matter smaller than  
in vacuum*

Effect tends to become “visible” for  $L > \approx 1000 \text{ km}$

# A way to rescale probabilities..

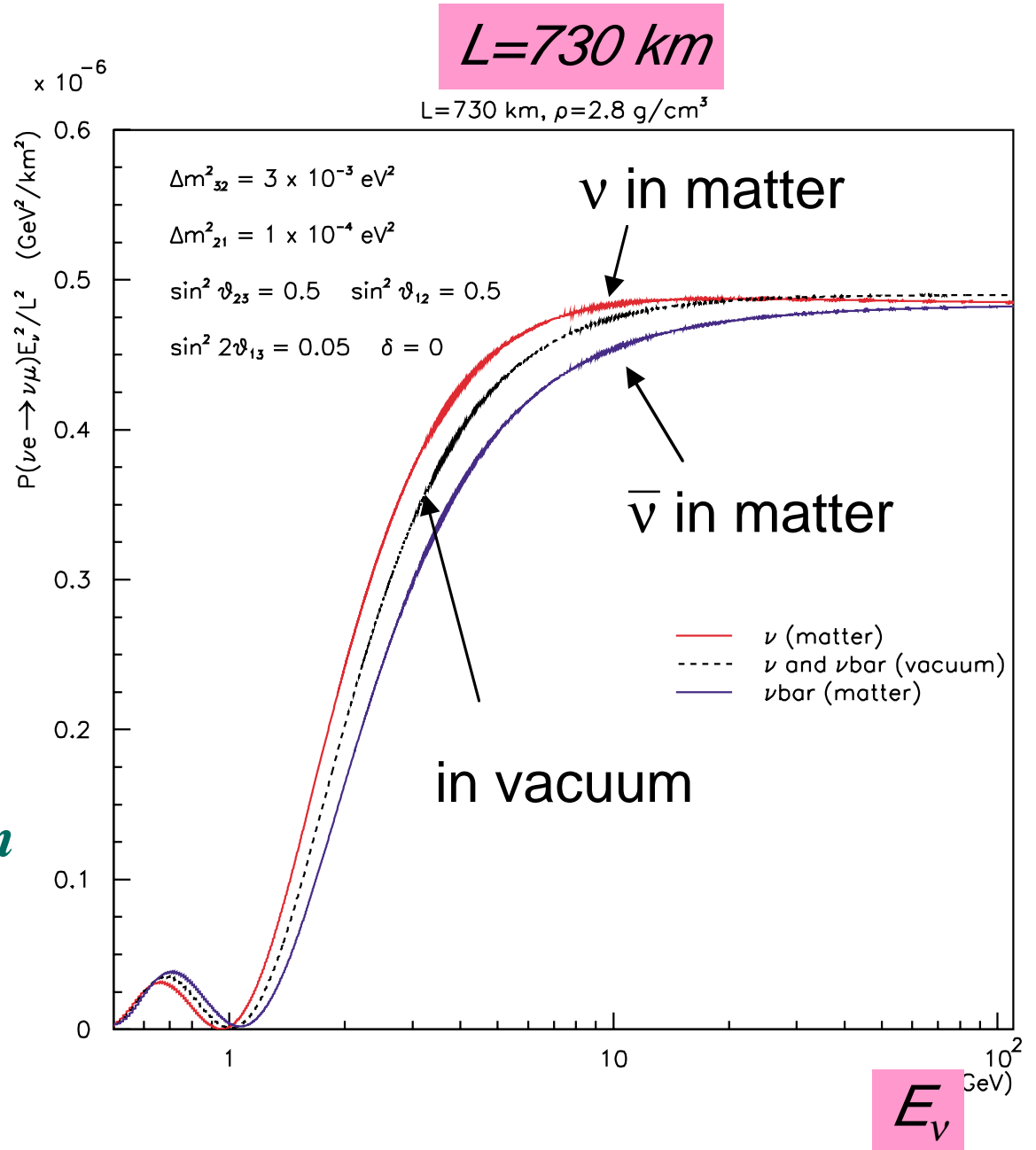
$$p \equiv P(\nu_e \rightarrow \nu_\mu) \times E_\nu^2 / L^2$$

probability

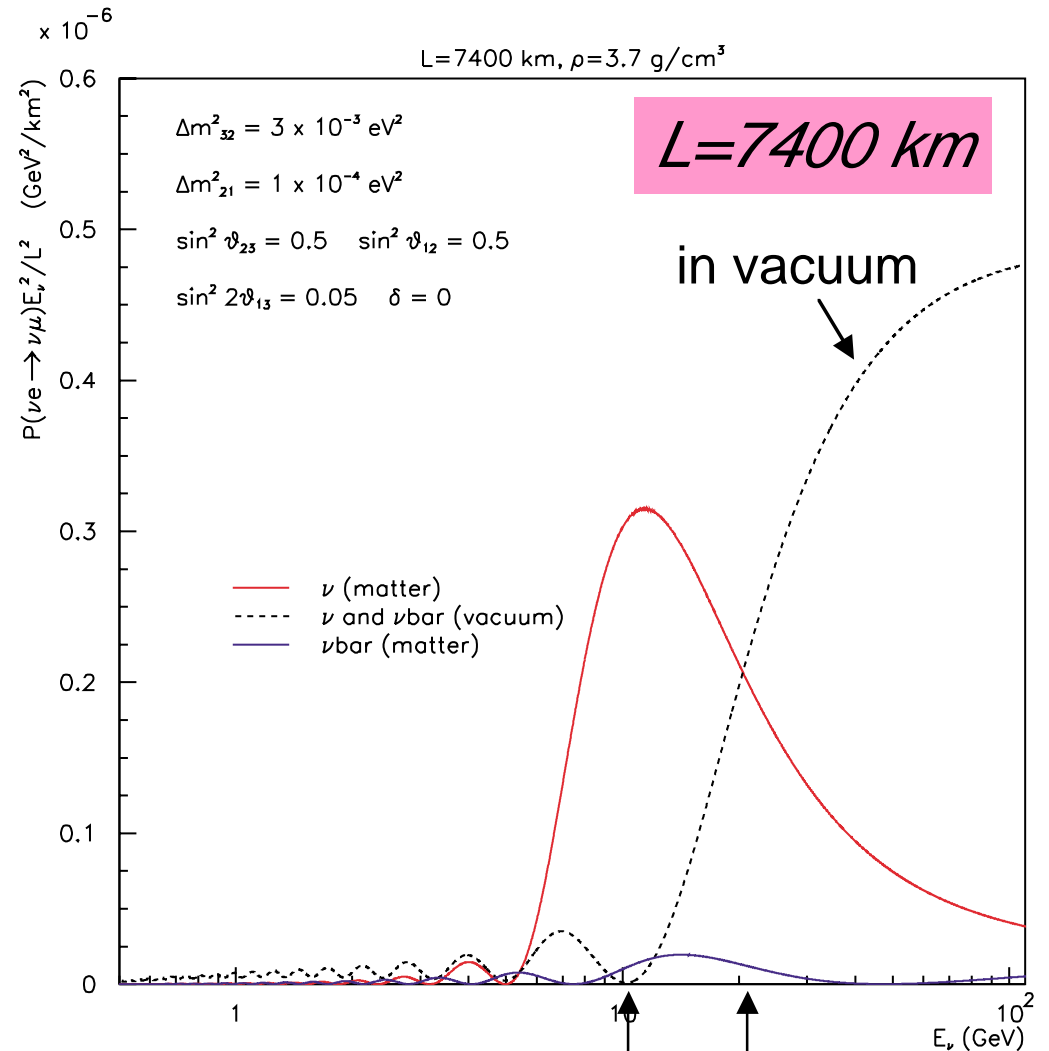
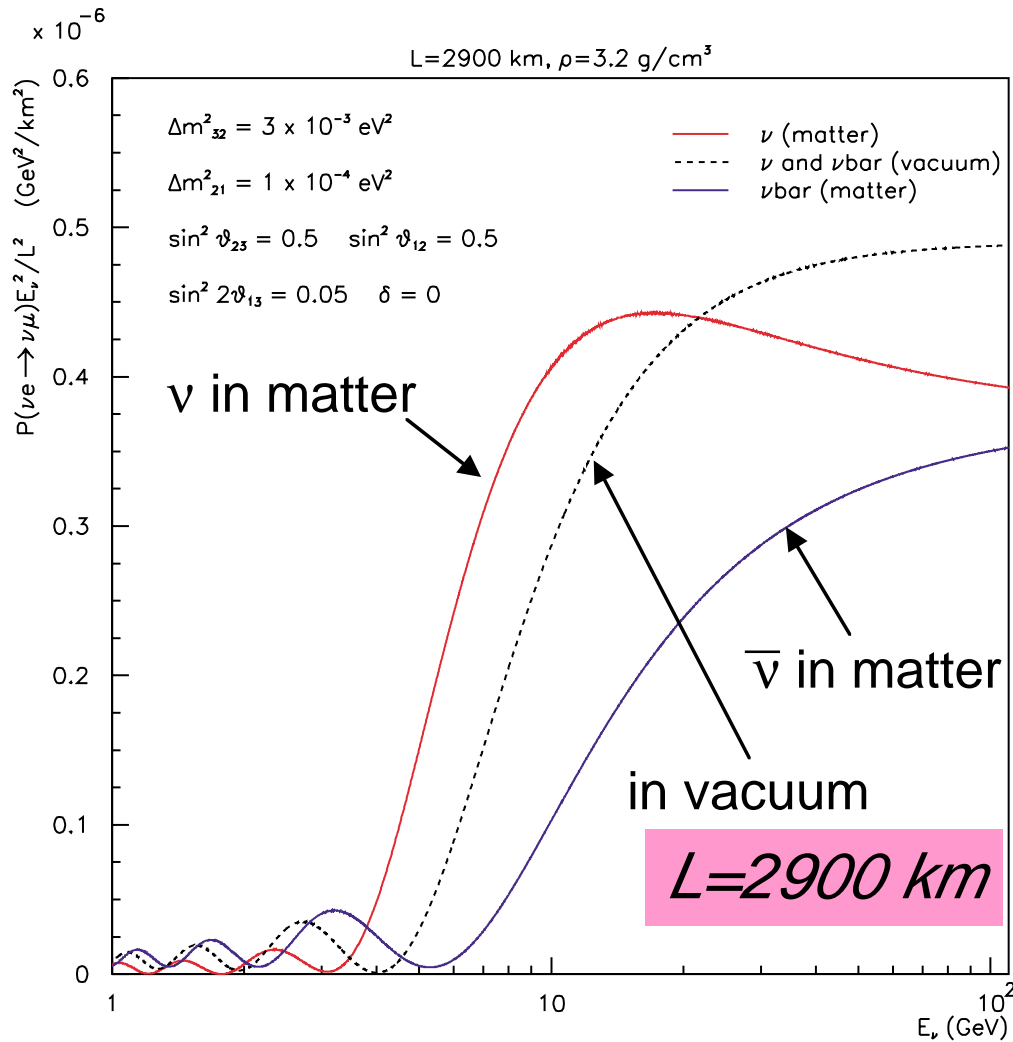
Approximate  $E_\nu$ -dependence of NF  $\nu$ -spectrum

Flux attenuation with distance

1.  $p \rightarrow \text{const}$  when  $E_\nu \rightarrow \infty$
2. It *correctly “weighs”* the probabilities with the  $E_\nu$  dependence of the NF  $\nu$  spectrum
3.  $p$  can be *directly compared at different baselines*



# Behaviour at larger distances...



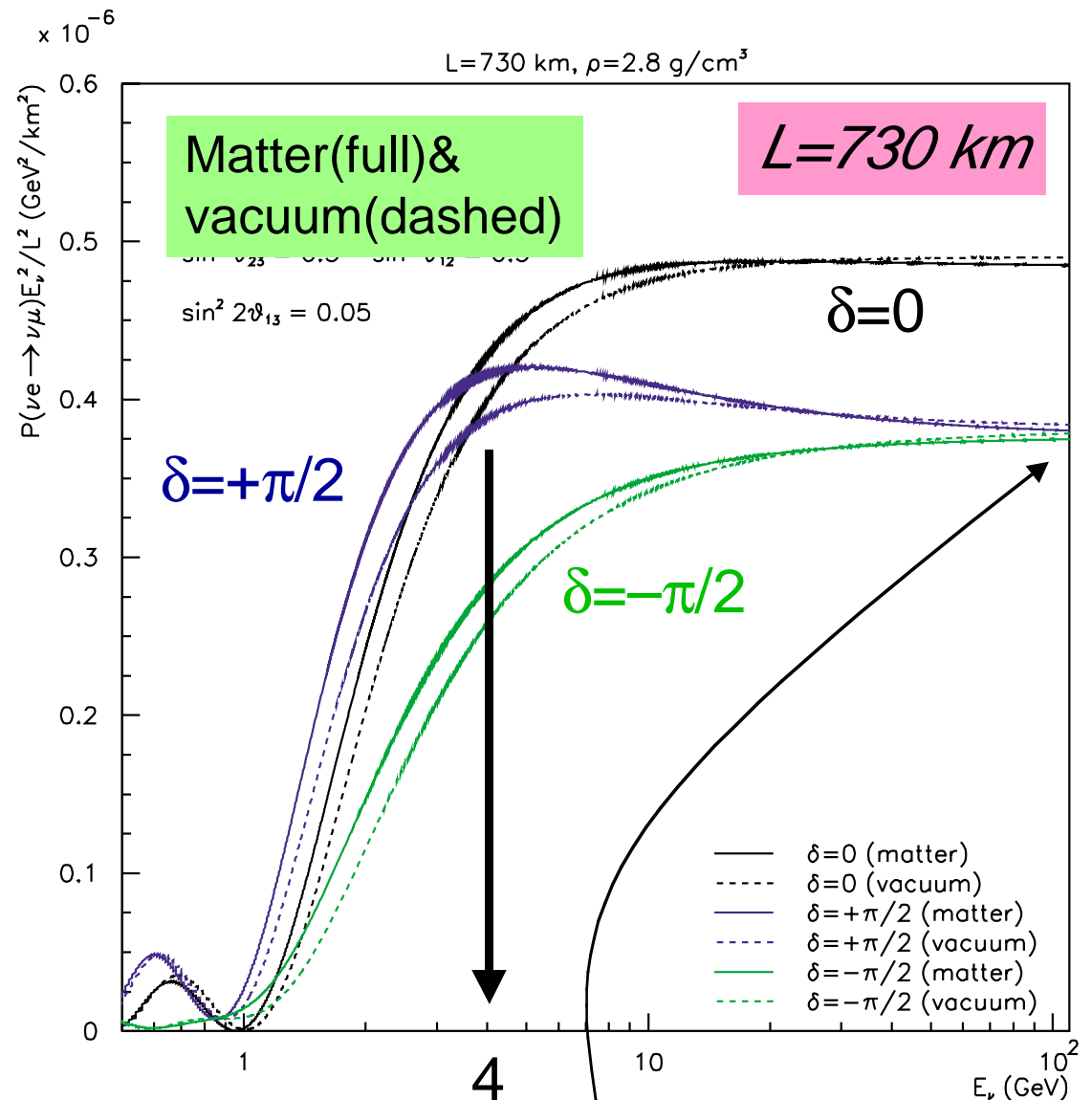
At large distances, matter effect suppresses oscillations!

$D \approx 2\Delta m^2 \cos 2\theta$   
 $D \approx \Delta m^2 \cos 2\theta$

# So what about the effects of $\delta$ ?

$$P(\nu_e \rightarrow \nu_\mu) \times E_\nu^2 / L^2$$

1. The  $E_\nu^2$  term takes into account that the NF likes to go to high energy  $\Rightarrow$  damps the part  $\Delta m_{21}^2 (L/4E_\nu) \approx 1$
2. At “high energy”, i.e.  $\Delta m_{21}^2 (L/4E_\nu) \ll 1$  &  $\Delta m_{32}^2 (L/4E_\nu) \ll 1$ , there is no more oscillation  $\Rightarrow$  change of  $\delta =$  change of  $\theta_{13}$  !!!
3. At “high energy”, the CP-effect goes like  $\cos\delta \Rightarrow$  cannot measure sign of  $\delta$



$$P\left(\nu_e \rightarrow \nu_\mu, \delta = \frac{\pi}{2}\right) - P\left(\nu_e \rightarrow \nu_\mu, \delta = 0\right) \propto \cos\delta$$

# So where is the compromise in $L/E$ ?

We must compromise at “medium” energy to

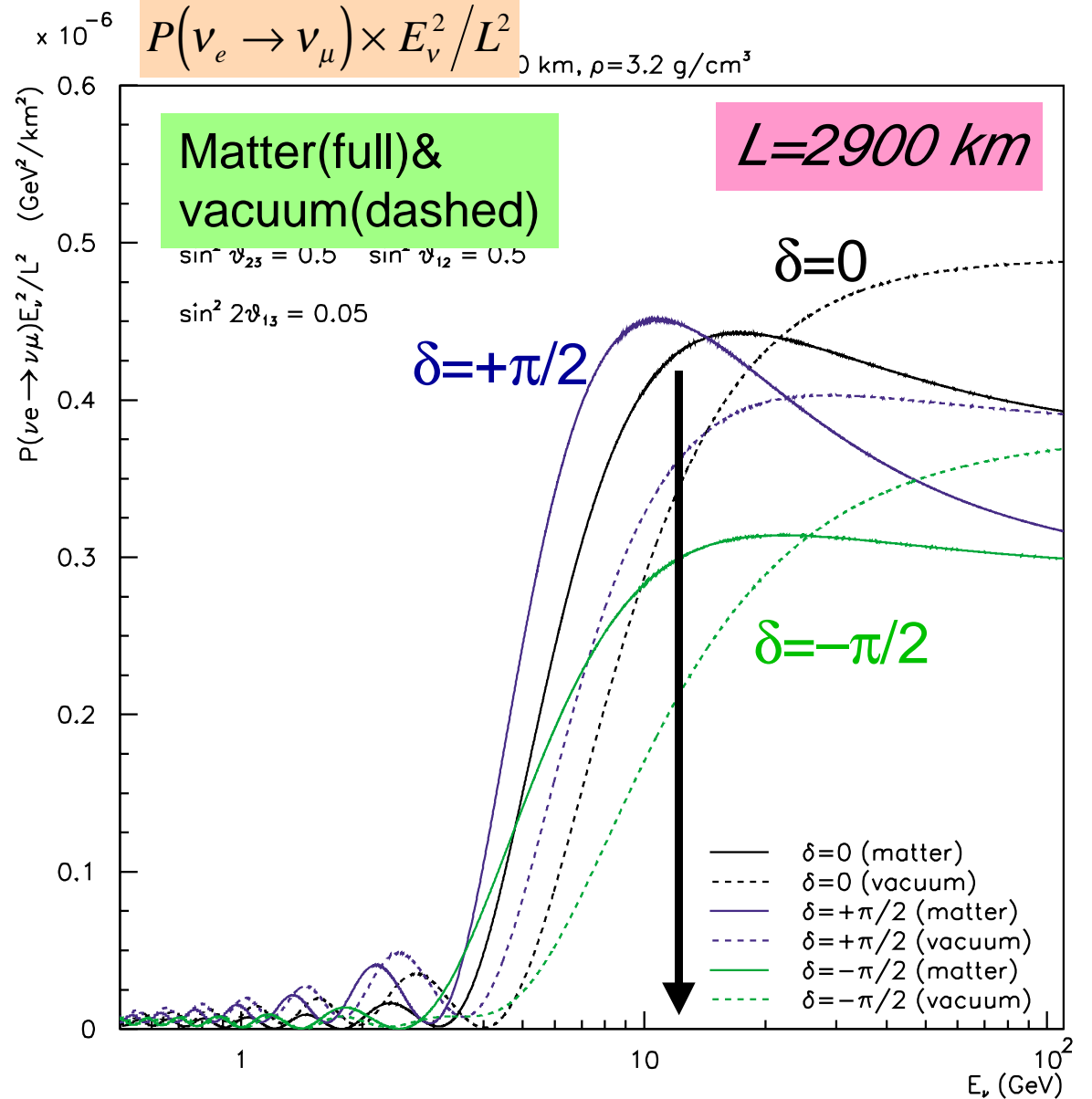
1. This means  $\Delta m^2_{21}(L/4E_\nu) \ll 1$   
&  $\Delta m^2_{32}(L/4E_\nu) \approx 1$
2. To gain from the  $E_\mu^3$  behavior of the NF
3. To guarantee the possibility to disentangle  $\delta$  from  $\theta_{13}$

➔

$$\frac{L}{E_\nu} \approx \frac{4\pi}{2\Delta m^2_{32}}$$

⚠  $E_{\nu, \text{MAX}} \sim 2 \text{ GeV}$  for  $L=732 \text{ km}$

⚠  $E_{\nu, \text{MAX}} \sim 8 \text{ GeV}$  for  $L=2900 \text{ km}$



## *If $L/E_\nu$ is fixed, what should be $L$ and $E_\nu$ ?*

The magnitude of the CP effect (given by  $J$ ) is known to be unaffected by matter

$$J = \cos\theta_{13} \sin\delta \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} / 8$$

Our “choice-point” for CP is at the fixed  $L/E_{\nu,\max}$  given by: 
$$E_{\nu,\max} = \frac{2 \times 1.27 \times \Delta m^2 L}{\pi}$$

When the neutrino energy becomes close to the MSW resonance, the effective oscillation wavelength increases, hence the CP effect at a fixed distance  $L$  becomes less visible.

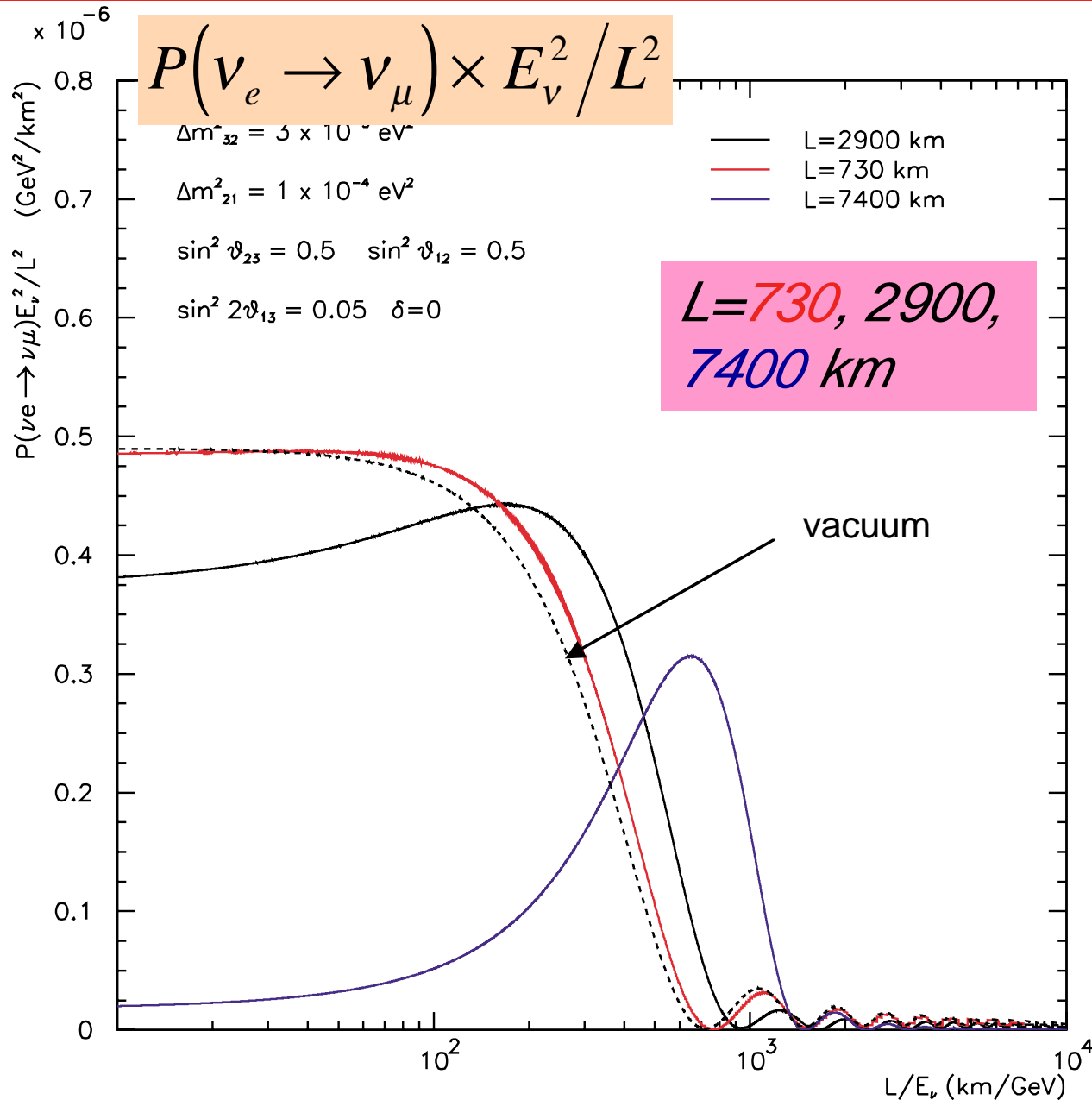
*Hence, we gain until the MSW resonance region and then loose.*

$$2\sqrt{2}G_F n_e E_\nu < \Delta m^2 \cos 2\theta \quad \longrightarrow \quad 2\sqrt{2}G_F n_e \frac{2 \times 1.27 \Delta m^2 L}{\pi} < \Delta m^2 \cos 2\theta$$

$$L < \frac{\pi \cos 2\theta}{2 \times 1.27 \times 7.56 \times 10^{-5} \text{ eV}^2 \left( \frac{\rho}{\text{gcm}^{-3}} \right)} \approx \frac{1.5 \times 10^4 \text{ km}}{\left( \frac{\rho}{\text{gcm}^{-3}} \right)} \approx 5000 \text{ km}$$



# Dependence of probability in matter on $L/E_\nu$



*The “scaling” with  $L/E_\nu$  of the probabilities is violated when  $E_{\nu, \text{max}} > E_{\nu, \text{resonance}}$  due to matter effects.*

*The longest baseline is clearly disfavored!*

**$L/E \text{ (km / GeV)}$**

# How to experimentally observe the $\delta$ -phase?

$$\bullet \Delta\delta \equiv P(\nu_e \rightarrow \nu_\mu; \delta = \pi/2) - P(\nu_e \rightarrow \nu_\mu; \delta = 0)$$

Compares oscillation probabilities as a function of  $E_\nu$  measured with wrong-sign muon event spectra, to MonteCarlo predictions of the spectrum in absence of CP violation

$$\bullet \Delta\text{CP}(\delta) \equiv P(\nu_e \rightarrow \nu_\mu; \delta) - P(\bar{\nu}_e \rightarrow \bar{\nu}_\mu; \delta)$$

Compares oscillation probabilities measured using the appearance of  $\nu_\mu$  and  $\bar{\nu}_\mu$ , running the storage ring with a beam of stored  $\mu^+$  and  $\mu^-$ , respectively. Matter effects are dominant at large distances

$$\bullet \Delta T(\delta) \equiv P(\nu_e \rightarrow \nu_\mu; \delta) - P(\nu_\mu \rightarrow \nu_e; \delta)$$

Compares the appearance of  $\nu_\mu$  and  $\nu_e$  in a beam of stored  $\mu^+$  and  $\mu^-$ . As opposite to the previous case, matter effects are the same, thus cancel out in the difference

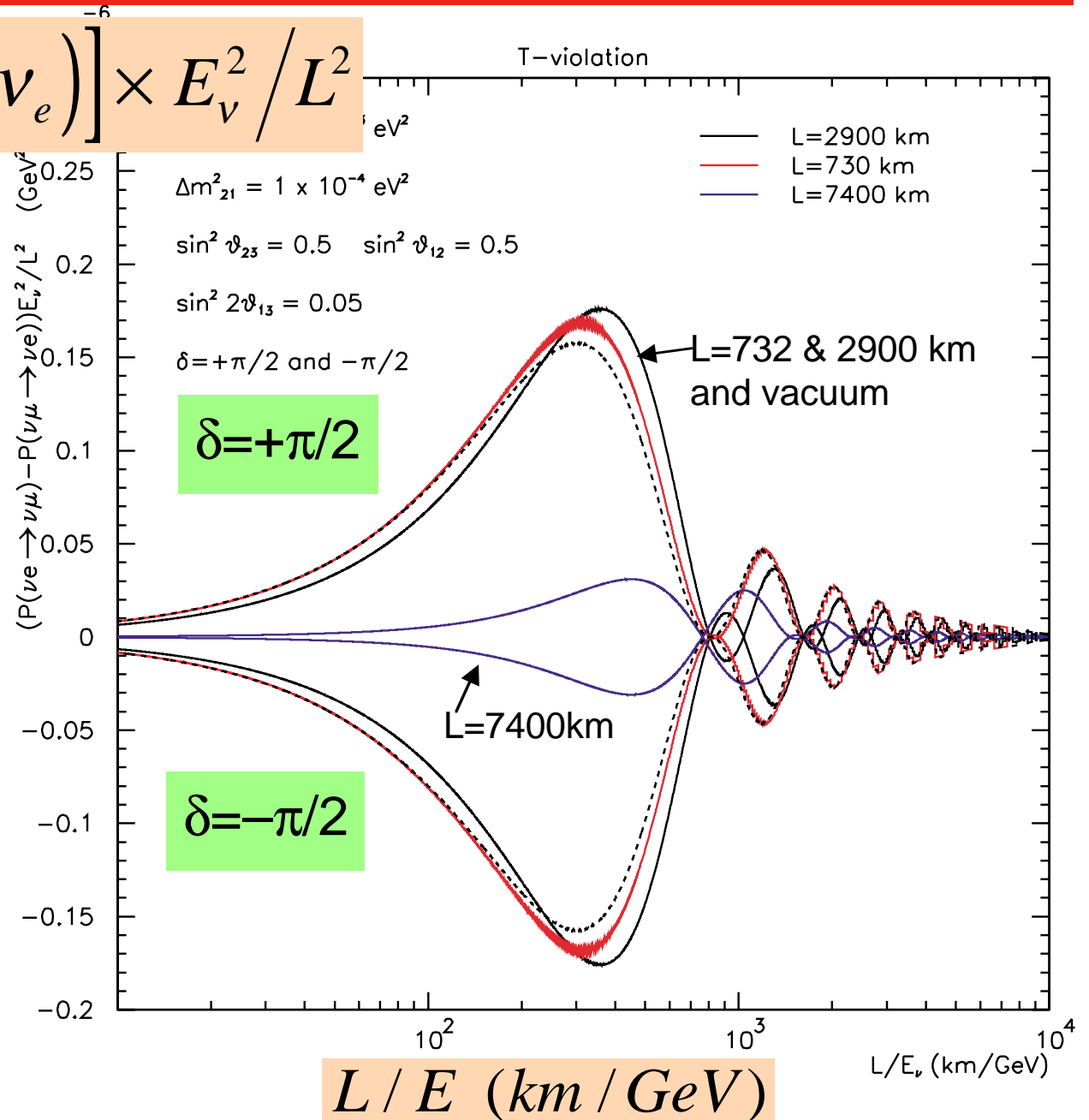
$$\bullet \Delta\bar{T}(\delta) \equiv P(\bar{\nu}_e \rightarrow \bar{\nu}_\mu; \delta) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e; \delta)$$

Same as previous case, but with antineutrinos. This effect is usually matter-suppressed with respect to the neutrino case.

# The $\Delta T$ dependence on $L/E_\nu$

$$\left[ P(\nu_e \rightarrow \nu_\mu) - P(\nu_\mu \rightarrow \nu_e) \right] \times E_\nu^2 / L^2$$

- ❖ The effect as function of  $L/E$  is the approximately the same at  $L=732$  or  $2900$  km and in vacuum.
- ❖ The dependence to the  $\delta$ -phase is reduced by matter at  $L=7400$  km

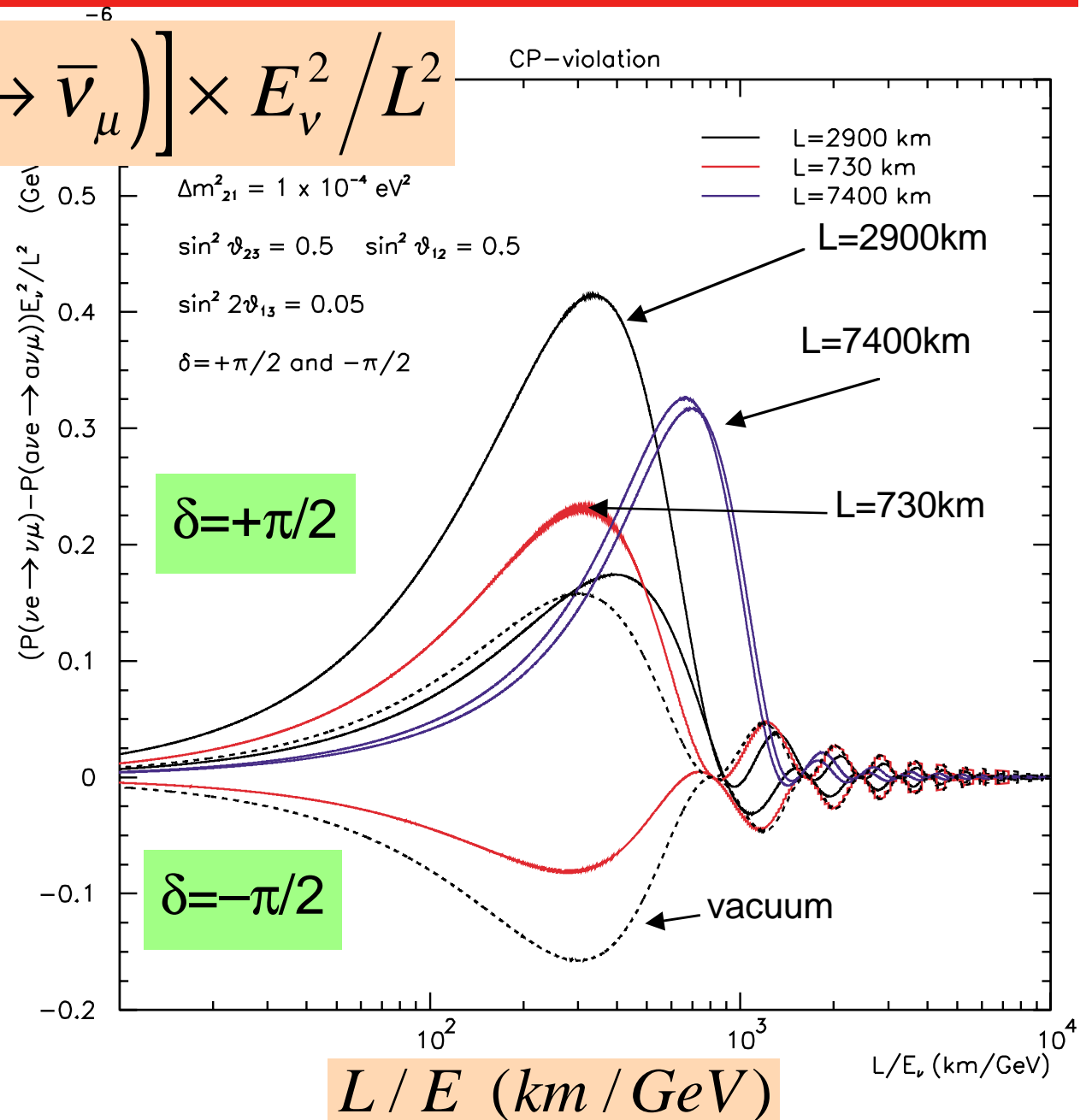


# The $\Delta CP$ dependence dependence on $L/E_\nu$

$$\left[ P(\nu_e \rightarrow \nu_\mu) - P(\bar{\nu}_e \rightarrow \bar{\nu}_\mu) \right] \times E_\nu^2 / L^2$$

CP-violation

- ❖ Matter introduces a large asymmetry, independent of  $\delta$
- ❖ The dependence to the  $\delta$ -phase is reduced by matter at  $L=7400$  km



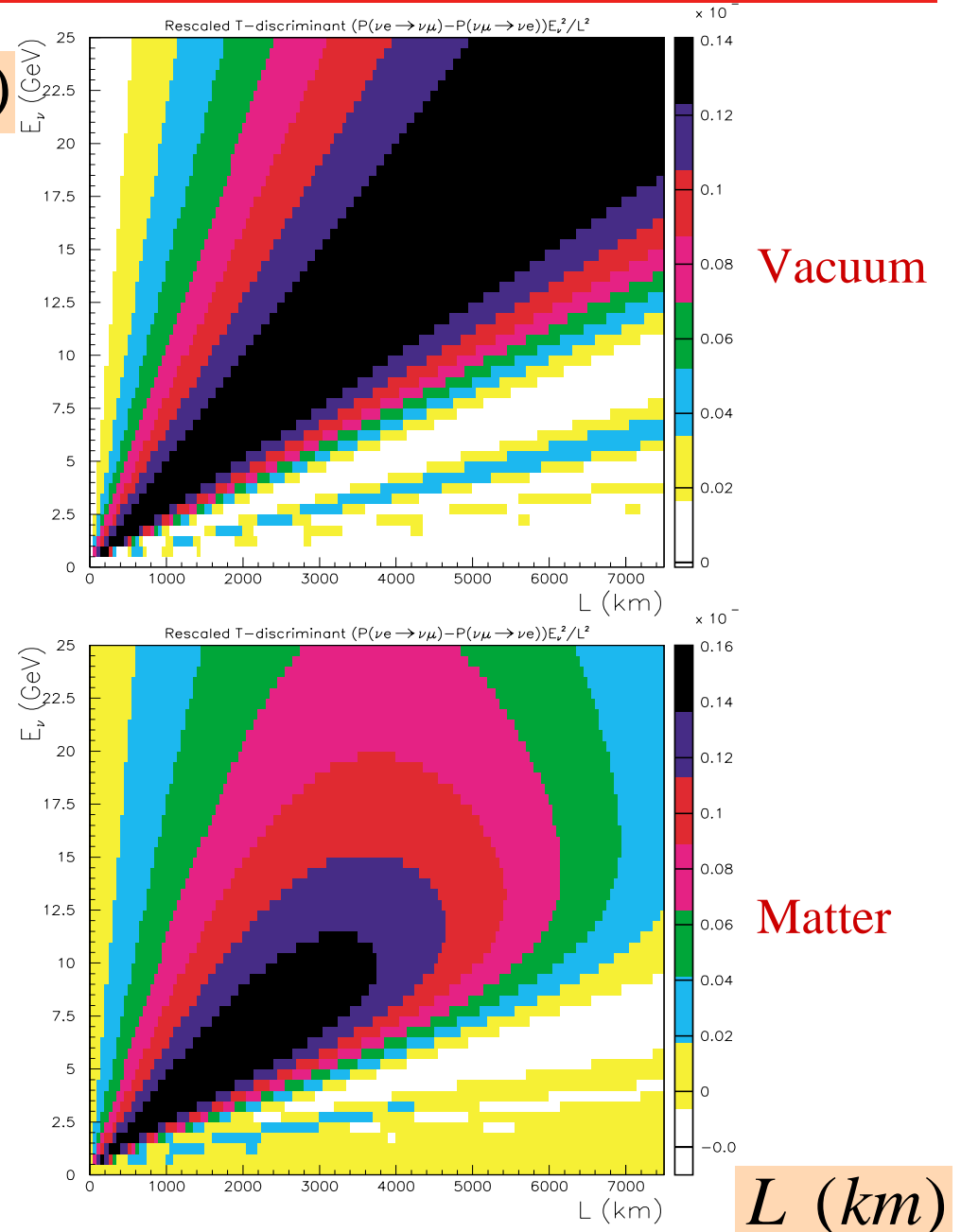
# Effects of matter on $\Delta T$

$E_\nu$  (GeV)

The cut-off of the scaled T-violating term in matter for  $L \approx 4000$  km destroys  $L/E$  scaling. It is useless to go above this distance for T- and CP-violation studies

The above considerations have nothing to do with the necessity of subtracting fake-CP violation due to matter  $\nu$ - $\bar{\nu}$  asymmetry!

They affect both  $\Delta T$  and  $\Delta CP$ .



# Measuring $\Delta T$

The comparison of  $\nu_{\mu} \rightarrow \nu_e$  and  $\nu_e \rightarrow \nu_{\mu}$  oscillation probabilities offers a **direct way** to highlight a **complex** component in the mixing matrix, independent of matter and other oscillation parameters.

This measurement is not directly accessible at a neutrino Factory with a conventional detector due to the large  $\nu_e$  background in the beam. It would add a **considerable improvement** to the physics reach of a Neutrino Factory

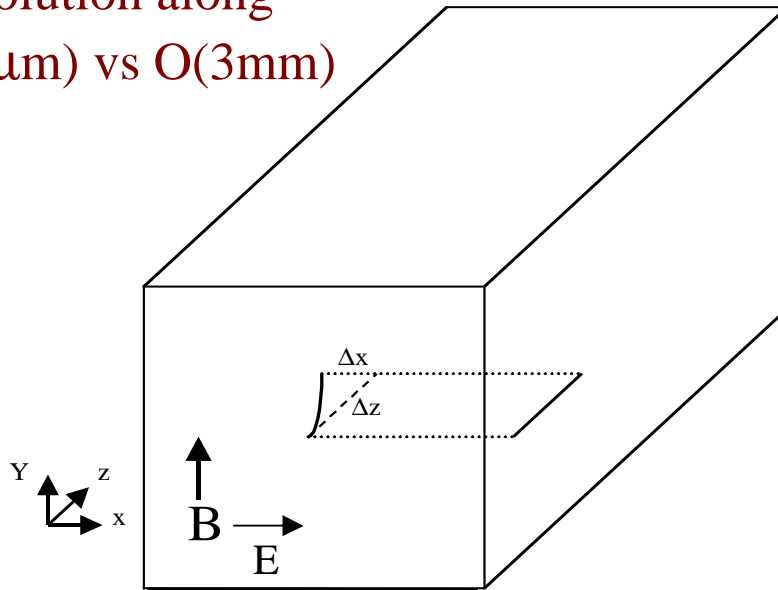
**Two methods have been proposed to solve the problem of beam  $\nu_e$  background :**

- ★ **Beam polarization** (not very effective; see A.Blondel, A.Bueno, M.Campanelli, A.Rubbia, Monterey NUFACT 00 proceedings)
- ★ **Electron charge**

# MC simulation for electron charge

MC simulations of electrons in a magnetic field have been performed assuming a magnetized liquid argon imaging TPC (Magnetized ICARUS-like detector)

Magnetic and electric fields are perpendicular to exploit the better resolution along drift ( $O(300 \mu\text{m})$  vs  $O(3\text{mm})$  wire pitch)



Purities obtained (for 10% efficiency) are encouraging, but clearly require high fields

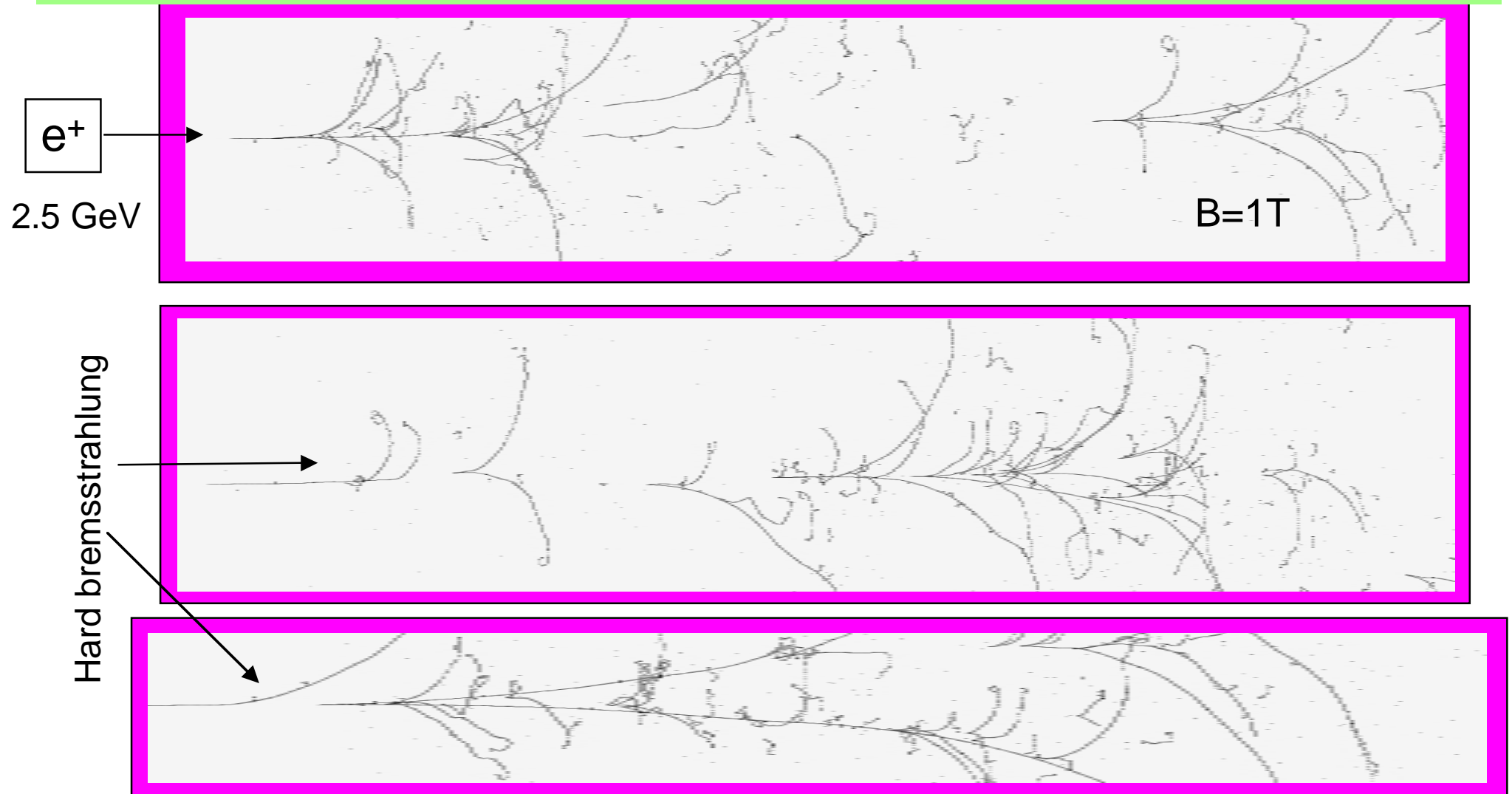
$E_e = 5 \text{ GeV}$

B field (T)	Charge confusion (%)
0.2	35
0.5	15
1.0	3

**Actual R&D (imaging in B-field) and electron test beams required...**

# *On the possibility to measure the electron charge*

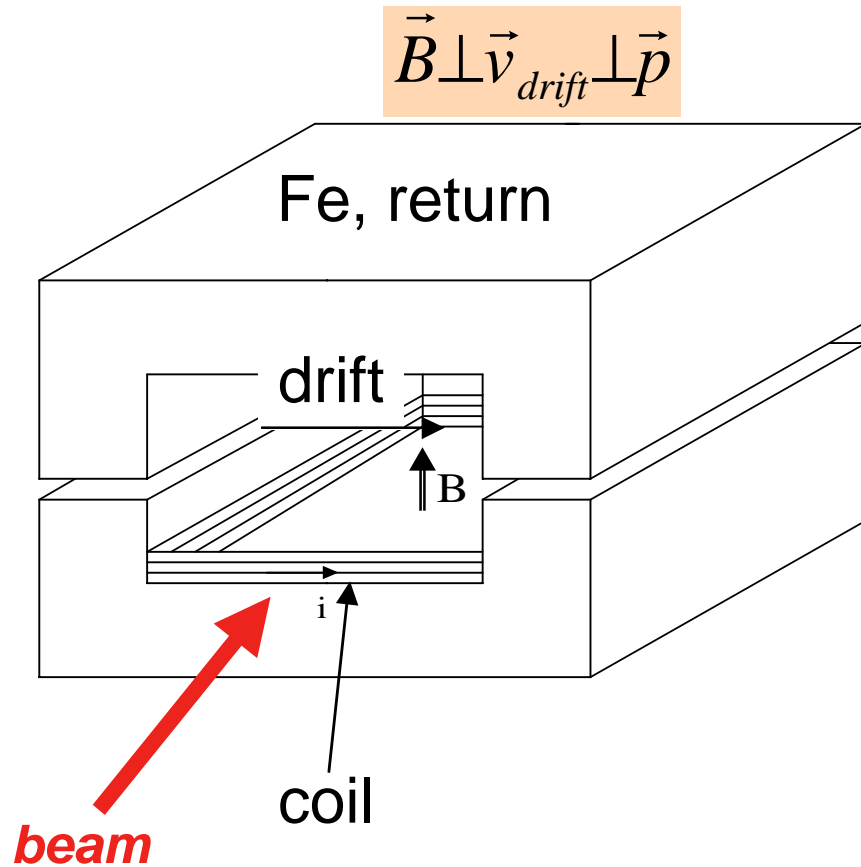
This appears to be only practically conceivable for electron energies  $\leq 5 \text{ GeV}$





# A large magnet ?

An interesting possibility, *to be further understood*, is the creation of the B-field over the large volume encompassing the LAr with the help of a very large solenoid



Joule Power (non-superconducting):

$$P = \rho \frac{2(a+b)hB^2}{md\mu_0^2}$$

d=coil thickness, m=#windings, h=height, a=width, b=length

Parameter	
Argon volume	$8 \times 8 \times 16m^3$
Argon mass	1.4 kton
Magnetic field	1.0 T
Current	2000 A
Conductor length	150 km
Resistance	$1 \Omega$
Dissipated power	4 MW
Iron mass	5 kton

# The proof that it could work

In order to prove L/E scaling, and explore the physical reach in practical examples, we have studied in detail two cases with a 10 kton detector:

- L = 732 km,  $E_\mu = 7.5$  GeV,  $10^{21}$   $\mu$  decays for  $\Delta\text{CP}$  and  $\Delta\text{T}$
- L = 2900 km,  $E_\mu = 30$  GeV,  $2.5 \times 10^{20}$   $\mu$  decays for  $\Delta\text{CP}$  only

Process		$E_\mu = 7.5$ GeV $L = 732$ km $10^{21} \mu^-$	$E_\mu = 30$ GeV $L = 2900$ km $2.5 \times 10^{20} \mu^-$
Non-oscillated rates	$\nu_\mu$ CC	41690	36050
	$\nu_\mu$ NC	10700	10300
	$\bar{\nu}_e$ CC	14520	13835
	$\bar{\nu}_e$ NC	4266	4975
Oscillated events ( $\delta = \pi/2$ )	$\bar{\nu}_e \rightsquigarrow \bar{\nu}_\mu$ CC	88	50
	$\nu_\mu \rightsquigarrow \nu_e$ CC	258	238
Oscillated events ( $\delta = 0$ )	$\bar{\nu}_e \rightsquigarrow \bar{\nu}_\mu$ CC	100	54
	$\nu_\mu \rightsquigarrow \nu_e$ CC	385	333
Oscillated events ( $\delta = -\pi/2$ )	$\bar{\nu}_e \rightsquigarrow \bar{\nu}_\mu$ CC	100	55
	$\nu_\mu \rightsquigarrow \nu_e$ CC	376	330

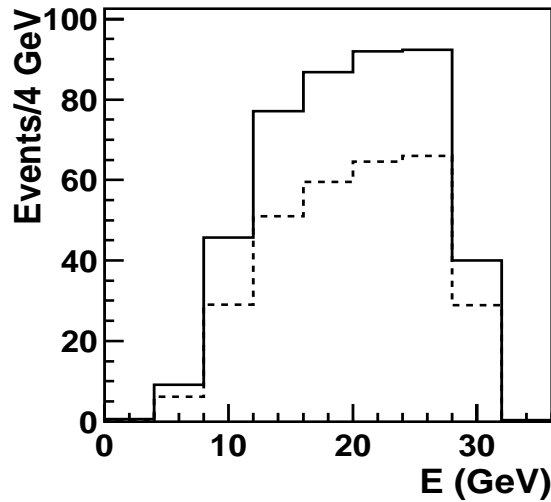
Process		$E_\mu = 7.5$ GeV $L = 732$ km $10^{21} \mu^+$	$E_\mu = 30$ GeV $L = 2900$ km $2.5 \times 10^{20} \mu^+$
Non-oscillated rates	$\bar{\nu}_\mu$ CC	16570	15962
	$\bar{\nu}_\mu$ NC	5096	5600
	$\nu_e$ CC	37570	32100
	$\nu_e$ NC	9143	9175
Oscillated events ( $\delta = \pi/2$ )	$\nu_e \rightsquigarrow \nu_\mu$ CC	445	397
	$\bar{\nu}_\mu \rightsquigarrow \bar{\nu}_e$ CC	86	46
Oscillated events ( $\delta = 0$ )	$\nu_e \rightsquigarrow \nu_\mu$ CC	438	387
	$\bar{\nu}_\mu \rightsquigarrow \bar{\nu}_e$ CC	86	45
Oscillated events ( $\delta = -\pi/2$ )	$\nu_e \rightsquigarrow \nu_\mu$ CC	289	277
	$\bar{\nu}_\mu \rightsquigarrow \bar{\nu}_e$ CC	77	42

$\tau \rightarrow e$  background: another reason to require low energies!

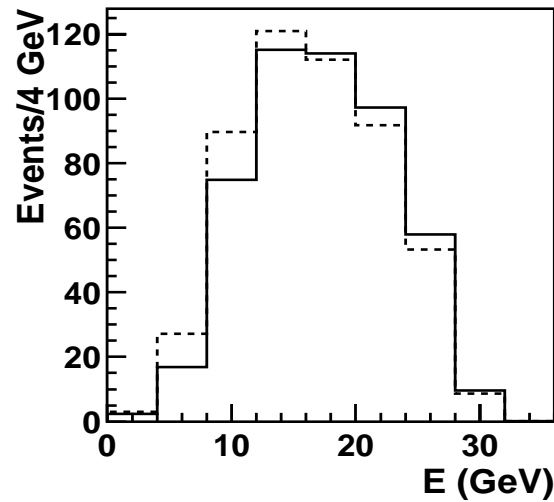
Assume BG rejection factor for electrons  $O(10^{-3})$  for 20% efficiency

# L/E scaling

Wrong-sign  
electrons



Wrong-sign  
muons

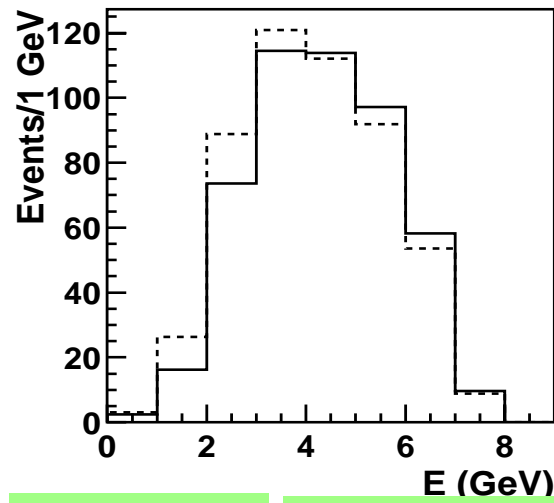
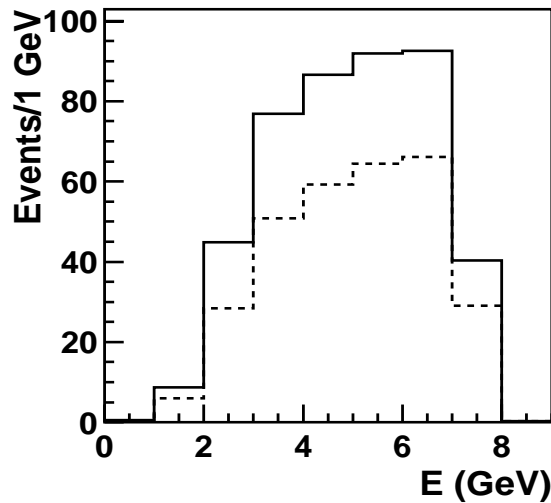


10 kton detector

$L=2900$  km,  
 $E_\mu=30$  GeV  
 $L/E_\mu \approx 100$  km/GeV

$10^{21}$   $\mu$  decays

*Identical  
L/E's  
yield  
identical  
effects!*



$L=732$  km,  
 $E_\mu=7.5$  GeV  
 $L/E_\mu \approx 100$  km/GeV

$2.5 \times 10^{21}$   $\mu$  decays

—  $\delta=0$

.....  $\delta=+\pi/2$

# Direct extraction of the oscillation probabilities (I)

- ★ From the visible energy distributions of the collected events, one can extract the oscillation probabilities

$$P_i(\nu_e \rightarrow \nu_\mu) \equiv \frac{N_i(ws\mu) - N_i^0(ws\mu)}{\varepsilon_i(p_\mu > p_\mu^{cut})N_i^0(e)} \quad \mu^+ \text{ decays}$$

$N_i(ws\mu)$  = number of wrong - sign muon events in the  $i$ th bin of energy

$N_i^0(ws\mu)$  = number of background events

$\varepsilon_i(p_\mu > p_\mu^{cut})$  = efficiency of the muon threshold cut in that bin

$N_i^0(e)$  = number of electron events in absence of oscillations

Similar quantity can be defined for  $\mu^-$  decays

## Direct extraction of the oscillation probabilities (II)

- ★ Similar quantities for measuring electron appearance

$$P_i(\nu_\mu \rightarrow \nu_e) \equiv \frac{N_i(wse) - N_i^0(wse)}{\varepsilon_e(1 - p_{conf})N_i^0(rs\mu)} \quad \mu^- \text{ decays}$$

$N_i(wse)$  = number of wrong - sign electron events in the  $i$ th bin of energy

$N_i^0(wse)$  = number of background events

$\varepsilon_e$  = efficiency for charge identification of electrons

$N_i^0(rs\mu)$  = number of right - sign muon events in absence of oscillations

Similar quantity can be defined for  $\mu^+$  decays

# Direct extraction of the oscillation probabilities (III)

- ★ Binned discriminants for extraction of CP/T effects

For every energy bin  $i$ :

$$\Delta_{\text{CP}}(i) \equiv P_i(\nu_e \rightarrow \nu_\mu) - P_i(\bar{\nu}_e \rightarrow \bar{\nu}_\mu)$$

$$\Delta_{\text{T}}(i) \equiv P_i(\nu_\mu \rightarrow \nu_e) - P_i(\nu_e \rightarrow \nu_\mu)$$

*and similar for  $\bar{\Delta}_{\text{T}}(i)$  for antineutrinos*

- ★ For checking matter-effects, we can define

$$\Delta_{\text{CPT}}(i) \equiv P_i(\nu_\mu \rightarrow \nu_e) - P_i(\bar{\nu}_e \rightarrow \bar{\nu}_\mu)$$

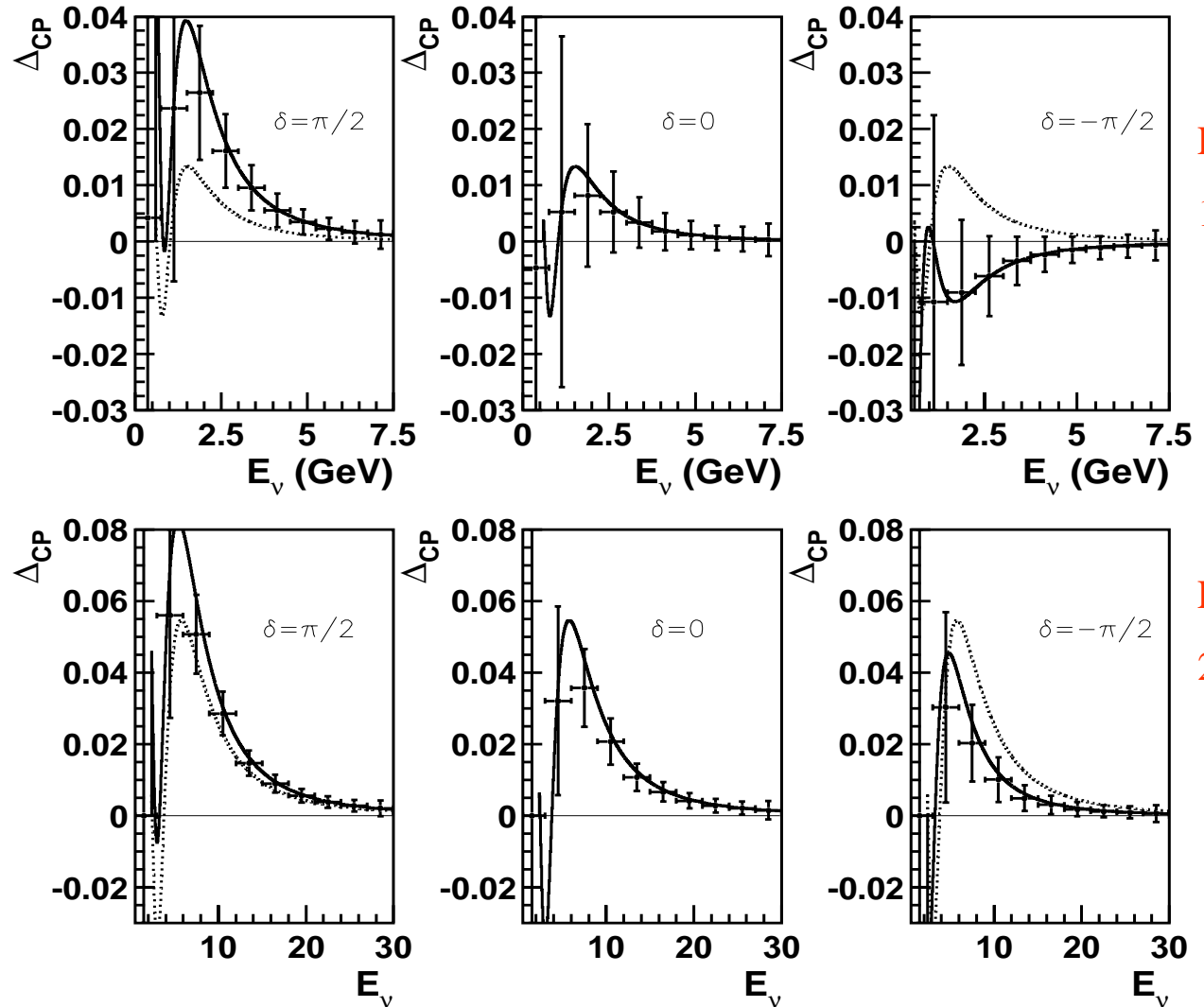
# Binned CP violation discriminant

10 kton detector

The  $\nu_e \rightarrow \nu_\mu$  and  $\bar{\nu}_e \rightarrow \bar{\nu}_\mu$  oscillation probabilities obtained from wrong-sign muons.

Will be different from zero due to matter effects, even for  $\delta=0$

At  $L=732$  km, matter effects are smaller, and large negative values of  $\delta$  can reverse the sign of  $\Delta_{CP}$



$L=732$  km  
 $10^{21} \mu$

$L=2900$  km  
 $2.5 \times 10^{20} \mu$

Expected statistical errors only

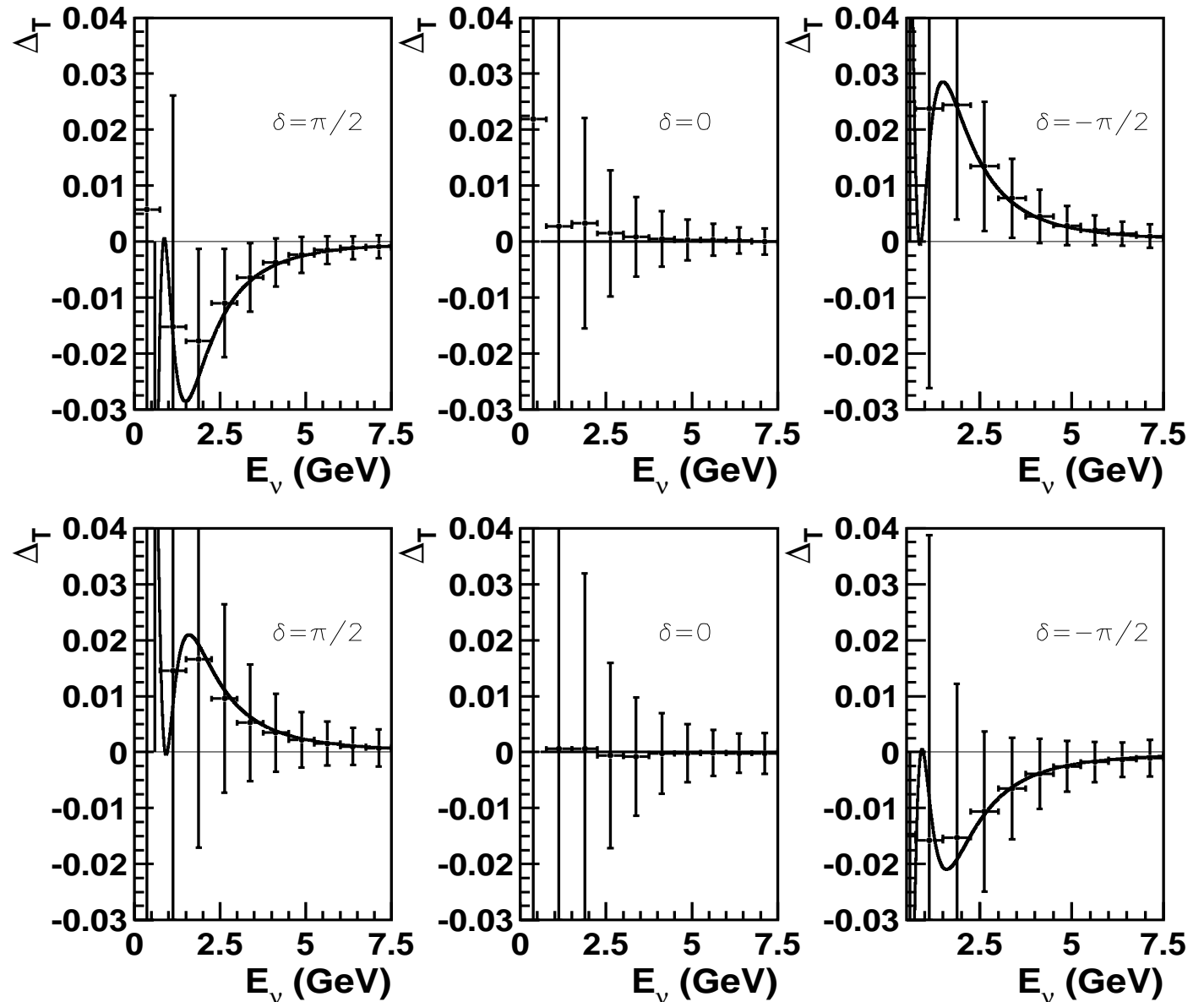
# Binned $\Delta T$ discriminant

The difference in probability for wrong-sign muons and wrong-sign electrons is a direct proof of T-violation. Matter effects are the same, and cancel out in the difference.

**L=732 km**

**$10^{21}$   $\mu$  decays**

**Expected statistical errors only**



10 kton detector



# Defining sensitivities to the $\delta$ -phase

- ★ One can define  $\chi^2$ -significance of the effects to set sensitivity contours

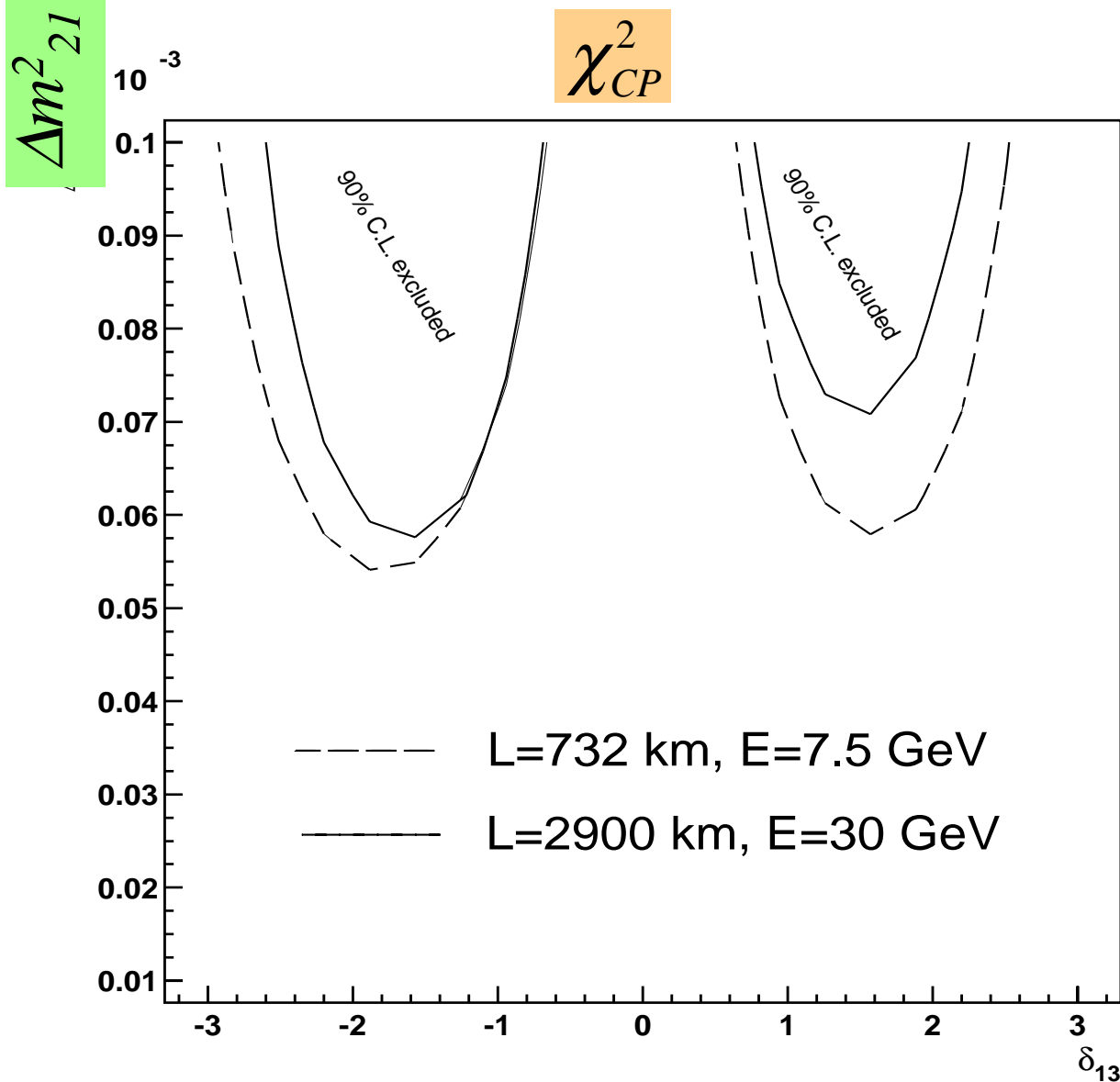
For CP-discriminant:

$$\chi_{CP}^2 \equiv \sum_i \frac{(\Delta_{CP}(i, \delta) - \Delta_{CP}(i, \delta = 0))^2}{(\sigma(\Delta_{CP}(i, \delta)))^2}$$

For T-discriminant:

$$\chi_T^2 \equiv \sum_i \frac{(\Delta_T(i, \delta) - \Delta_T(i, \delta = 0))^2}{(\sigma(\Delta_T(i, \delta)))^2} + \sum_i \frac{(\bar{\Delta}_T(i, \delta) - \bar{\Delta}_T(i, \delta = 0))^2}{(\sigma(\bar{\Delta}_T(i, \delta)))^2}$$

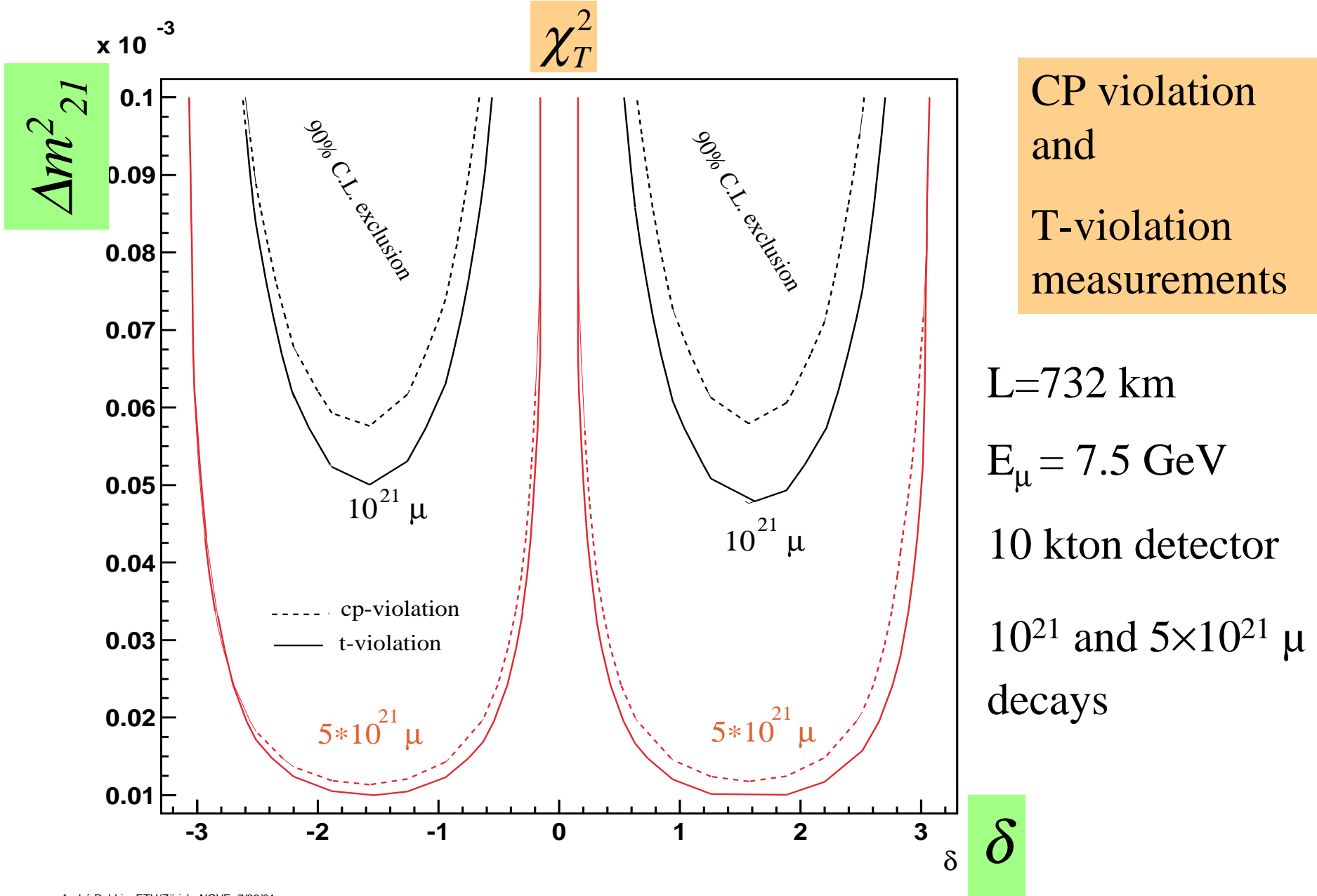
# $L/E_\mu$ scaling at work for direct CP measurement



90% contours in the  $\Delta m^2_{12}$ - $\delta$  plane, obtained translating the probability differences into  $\Delta\chi^2$

The sensitivity for the two cases is similar, proving the validity of the  $L/E_\mu$  scaling at constant machine power. Actually, the shorter distance is even better due to the smaller influence of matter effects

# Direct T-violation measurements sensitivity



# Conclusion

- ★ The current round of LBL experiments will be a **confirmation** of the SuperKamiokande results.
- ★ The **next discovery** will come from the exploration of the so-called  **$\theta_{13}$  angle**, the connection between Sun and atmospheric oscillations.
  - This is a challenging task
  - It requires new high intensity beams, i.e Superbeams
- ★ In case of Superbeams, one has to take into account
  - intrinsic beam backgrounds
  - detector-associated backgrounds
- ★ One can hope to explore the  **$\delta$ -phase**, but only if  **$\theta_{13}$**  and solar LMA solution allow it...
  - One approach is the JHF(phase II)-HyperK(1Mton) detector
  - Our preferred approach relies on the cleanliness of the neutrino factory coupled to a detector capable of **measuring the electron charge**. This would add a **considerable improvement** of a NF for CP and T violation studies.