

---

**ISAPP**

*Valencia, 2008*

**Neutrino Oscillation Phenomenology - II**

**Thomas Schwetz**

**CERN**

# Outline

---

## Lecture 1:

- **Neutrino oscillations**  
oscillations in vacuum and matter
- **Present neutrino oscillation experiments**  
solar, atmospheric, reactor, accelerator

## Lecture 2:

- **$\theta_{13}$  and global three flavour analysis**  
discussion of three flavour effects  
summary of present status and open questions
- **the LSND puzzle and MiniBooNE results**

# 3-flavour oscillation parameters

---

$$U = \begin{matrix} & \Delta m_{31}^2 & & & \Delta m_{21}^2 \\ \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} & \begin{pmatrix} c_{13} & 0 & e^{-i\delta} s_{13} \\ 0 & 1 & 0 \\ -e^{i\delta} s_{13} & 0 & c_{13} \end{pmatrix} & \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \end{matrix}$$

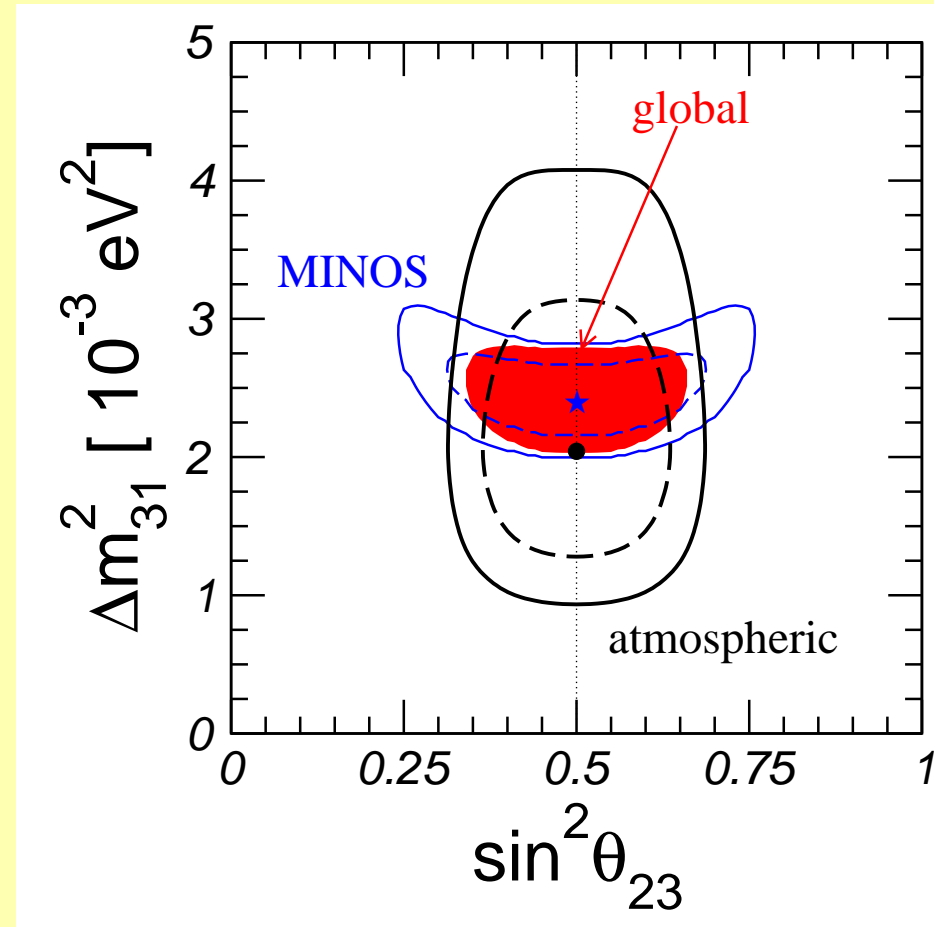
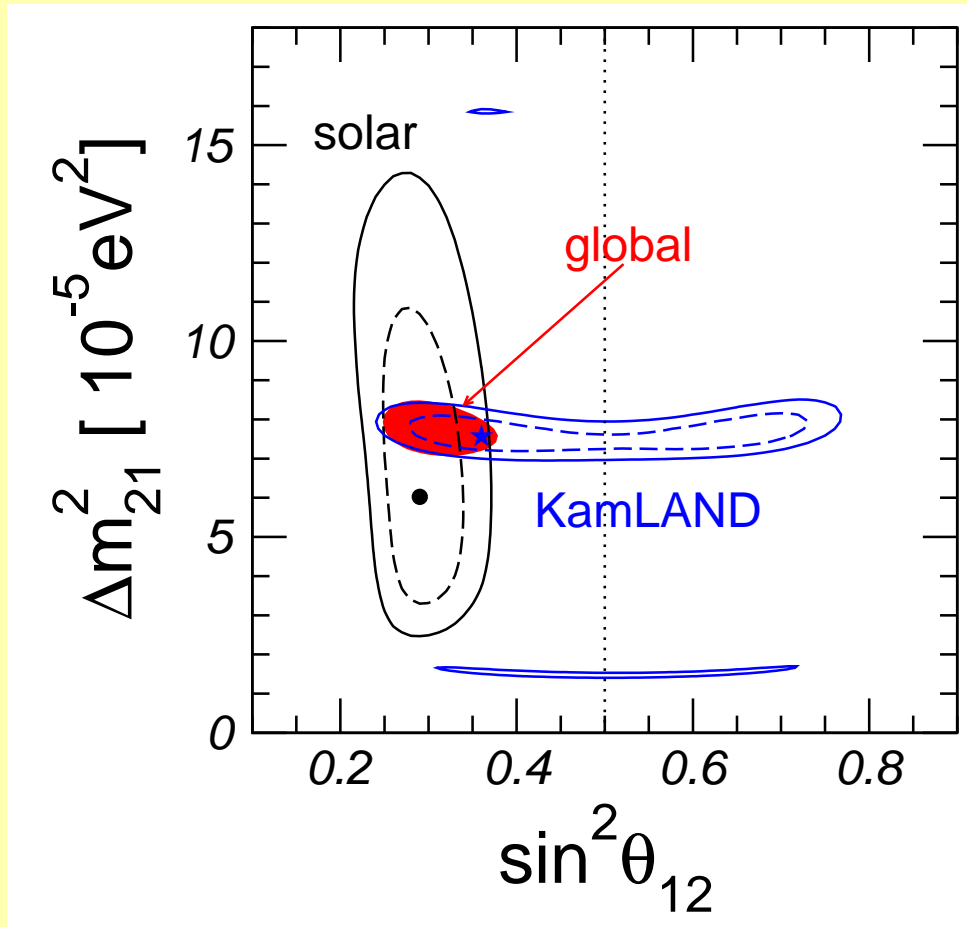
3-flavour effects are suppressed because

$$\theta_{13} \ll 1 \text{ und } \Delta m_{21}^2 \ll \Delta m_{31}^2$$

⇒ dominant oscillations are well described by effective two-flavour oscillations

# *Dominant oscillations*

90% and 99.73% CL contours



---

# $\theta_{13}$ and 3-flavour effects

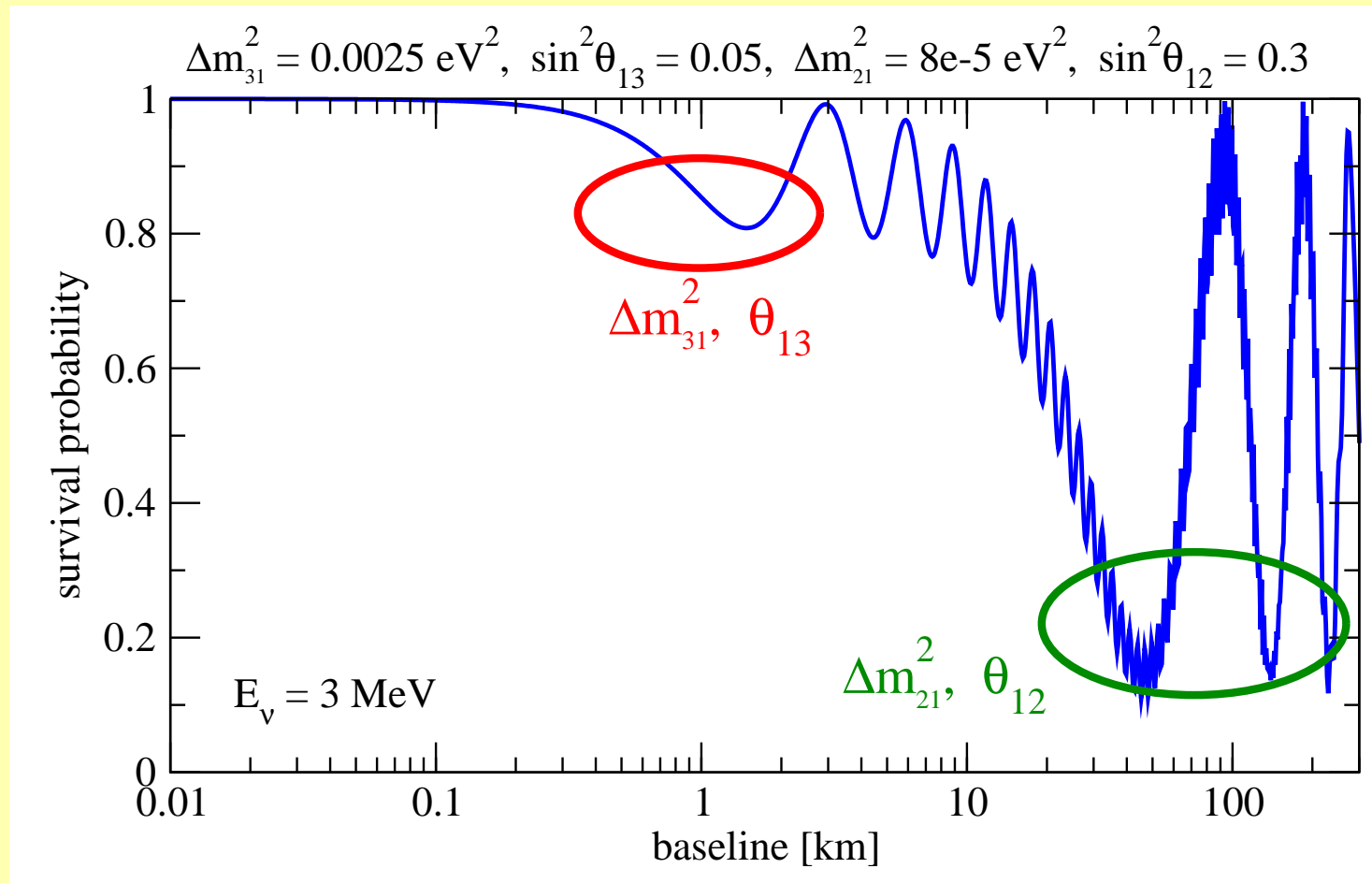
# Three flavour effects

---

- $\theta_{13}$  effects in oscillations with  $\Delta m_{31}^2$
- $\theta_{13}$  effects in oscillations with  $\Delta m_{21}^2$
- $\Delta m_{21}^2$  effects in oscillations with  $\Delta m_{31}^2$
- effects of  $\delta_{\text{CP}}$

# $P_{ee}$ at reactors

The 3-flavour  $\bar{\nu}_e \rightarrow \bar{\nu}_e$  survival probability:



# *The Chooz reactor experiment*

---

reactor experiment with a baseline of 1 km:

$$\frac{E_\nu}{L} \sim \frac{4 \text{ MeV}}{1 \text{ km}} \sim 4 \times 10^{-3} \text{ eV}^2$$

$\bar{\nu}_e$  disappearance at the “atmospheric”  $\Delta m^2$  scale

$$P_{ee} = 1 - \sin^2 2\theta_{13} \underbrace{\sin^2 \frac{\Delta m_{31}^2 L}{2E_\nu}}_{\mathcal{O}(1)\text{@CHOOZ}} + \mathcal{O}(\Delta m_{21}^2 / \Delta m_{31}^2)$$



# The Chooz reactor experiment

---

reactor experiment with a baseline of 1 km:

$$\frac{E_\nu}{L} \sim \frac{4 \text{ MeV}}{1 \text{ km}} \sim 4 \times 10^{-3} \text{ eV}^2$$

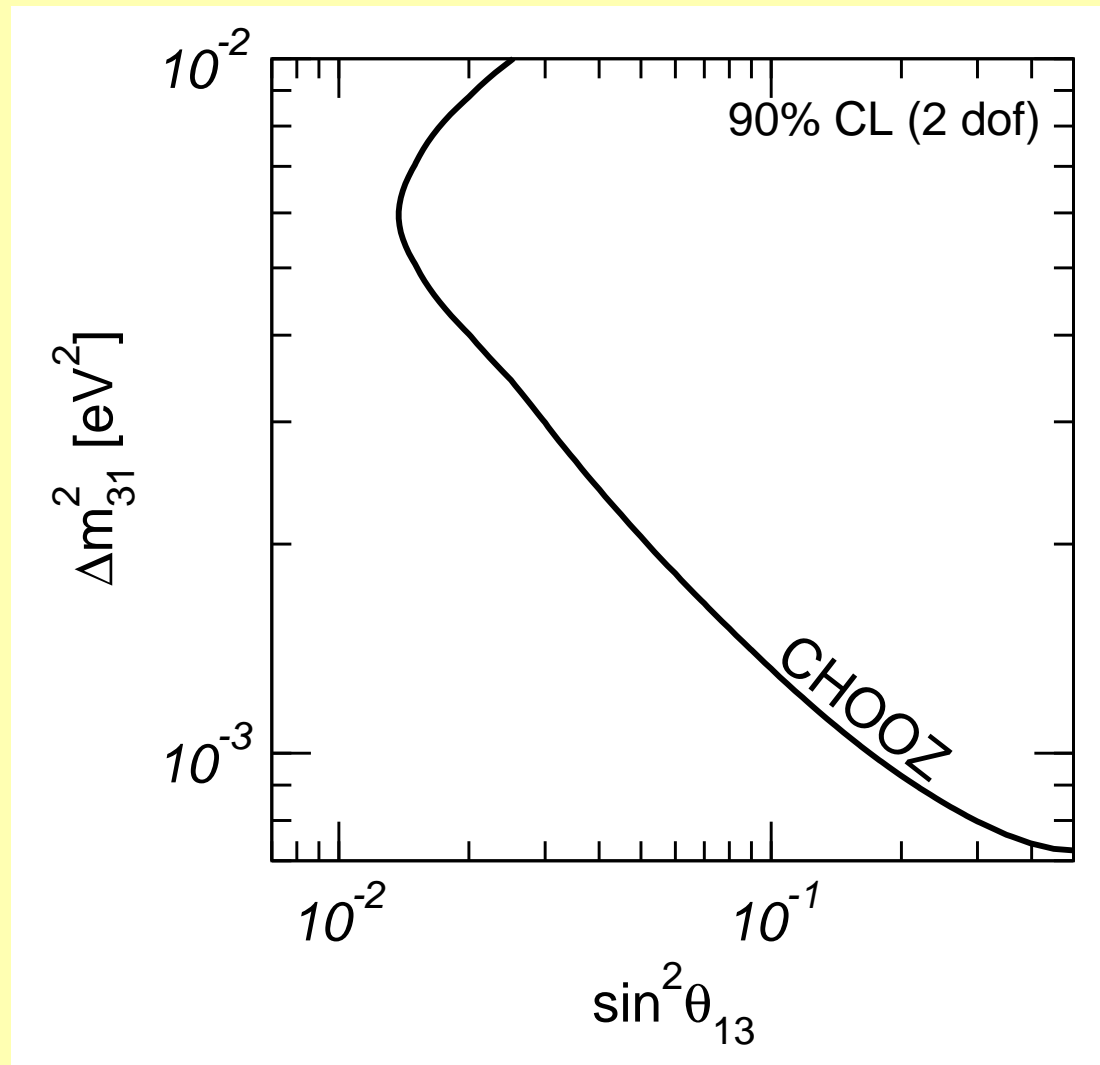
$\bar{\nu}_e$  disappearance at the “atmospheric”  $\Delta m^2$  scale

$$P_{ee} = 1 - \sin^2 2\theta_{13} \underbrace{\sin^2 \frac{\Delta m_{31}^2 L}{2E_\nu}}_{\mathcal{O}(1)\text{@CHOOZ}} + \mathcal{O}(\Delta m_{21}^2 / \Delta m_{31}^2)$$

**CHOOZ Result:** observed over expected number of events:

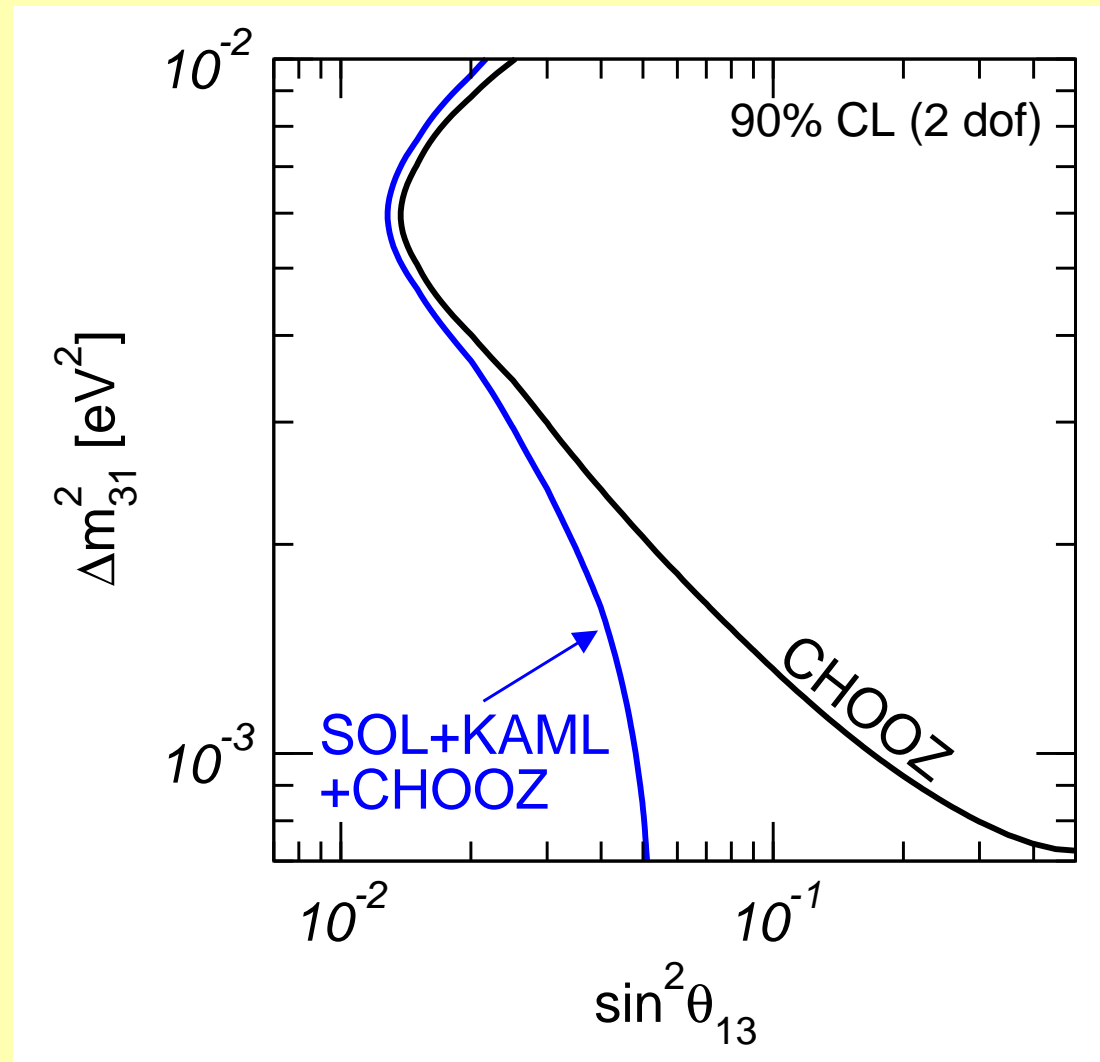
$$R = 1.01 \pm 2.8\% \pm 2.7\%$$

# The bound on $\theta_{13}$



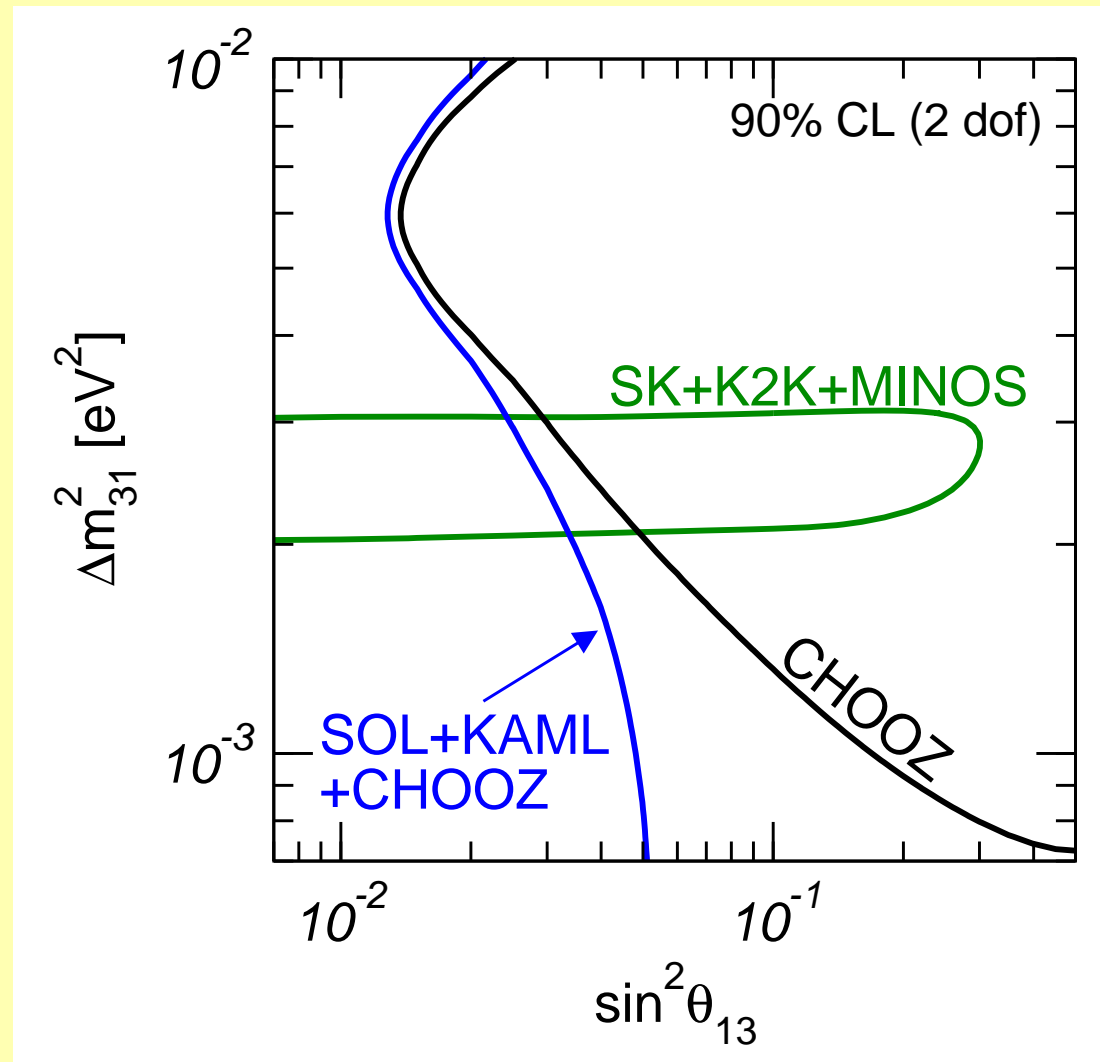
# The bound on $\theta_{13}$

... from interplay of global data:



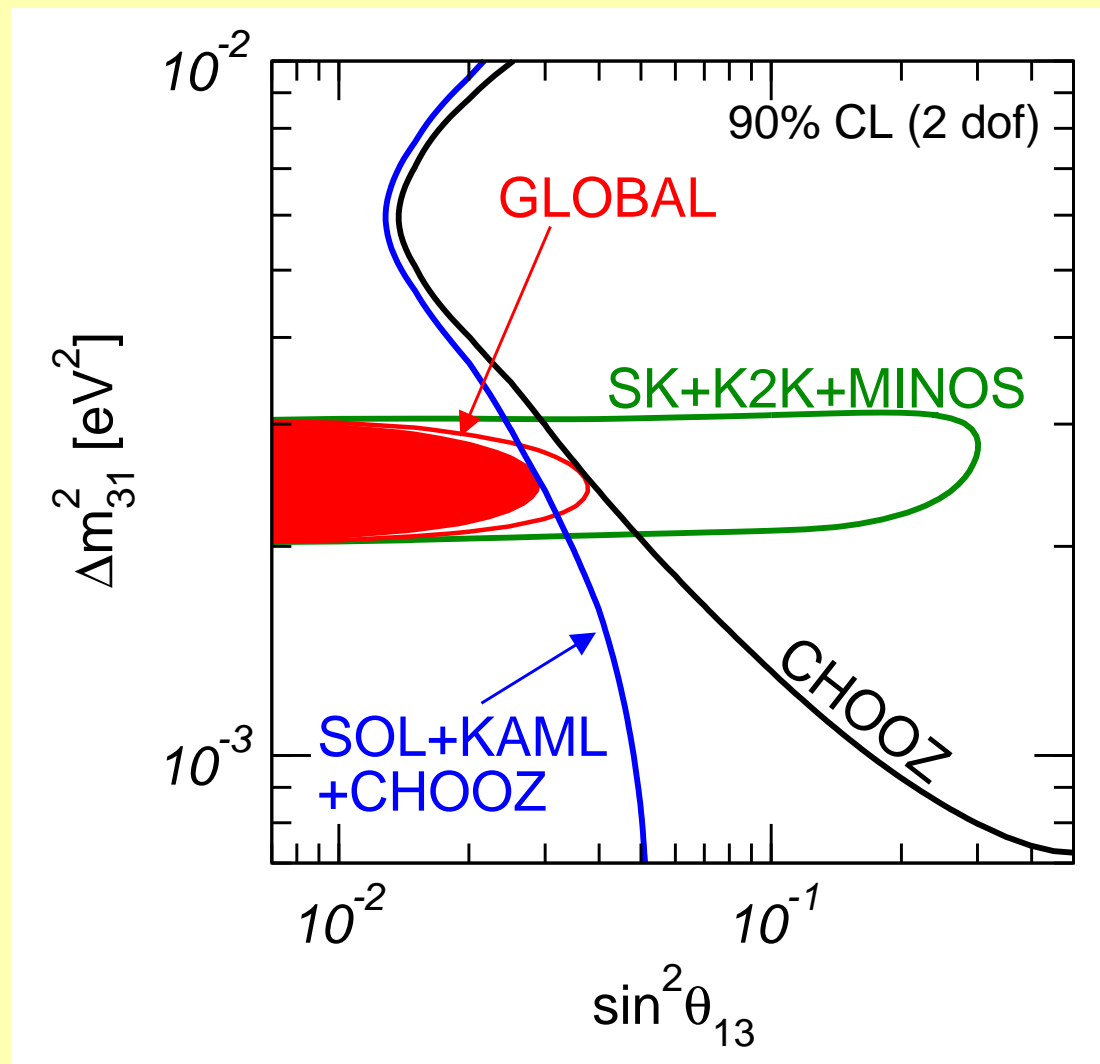
# The bound on $\theta_{13}$

... from interplay of global data:



# The bound on $\theta_{13}$

... from interplay of global data:



# $\theta_{13}$ in *Solar and KamLAND*

---

$$\begin{aligned} H_{\text{mat}}^\nu &= U_{23}U_{13}U_{12} \text{diag}(0, \Delta_{21}, \Delta_{31}) U_{12}^\dagger U_{13}^\dagger U_{23}^\dagger + \text{diag}(V, 0, 0) \\ &= U_{23}U_{13} \left[ U_{12} (0, \Delta_{21}, \Delta_{31}) U_{12}^\dagger + U_{13}^\dagger (V, 0, 0) U_{13} \right] U_{13}^\dagger U_{23}^\dagger \end{aligned}$$

# $\theta_{13}$ in Solar and KamLAND

---

$$\begin{aligned} H_{\text{mat}}^\nu &= U_{23}U_{13}U_{12} \text{diag}(0, \Delta_{21}, \Delta_{31}) U_{12}^\dagger U_{13}^\dagger U_{23}^\dagger + \text{diag}(V, 0, 0) \\ &= U_{23}U_{13} \left[ U_{12} (0, \Delta_{21}, \Delta_{31}) U_{12}^\dagger + U_{13}^\dagger (V, 0, 0) U_{13} \right] U_{13}^\dagger U_{23}^\dagger \end{aligned}$$

for solar and KamLAND:

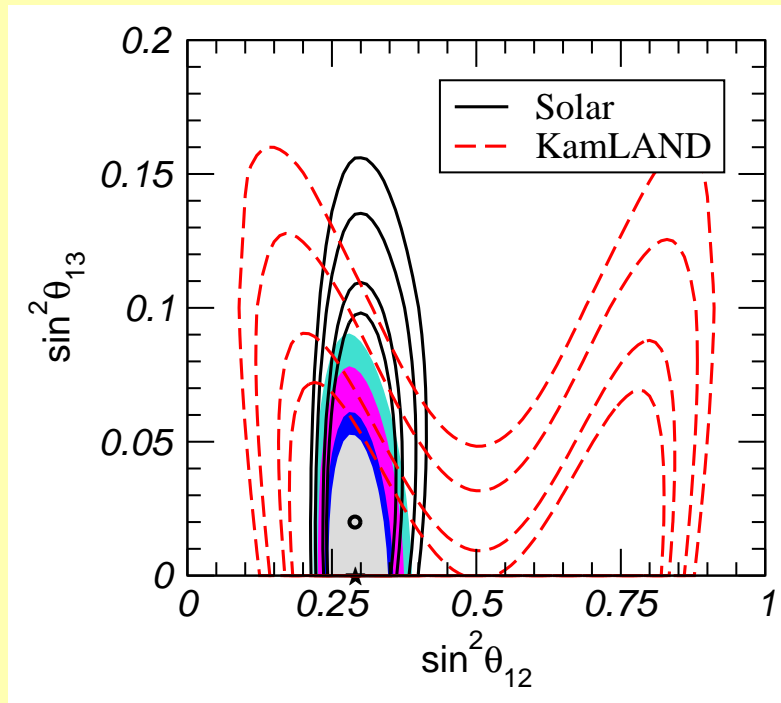
$$\frac{|\Delta m_{31}^2|L}{2E} \gg \frac{\Delta m_{21}^2 L}{2E} \sim 1, \quad |\Delta m_{31}^2| \gg EV_{\text{sun}} \sim \Delta m_{21}^2$$

$\Rightarrow$  can set  $\Delta m_{31}^2 \rightarrow \infty$

$$P_{ee}^{\text{sun,KL}} = c_{13}^4 P_{ee}^{2\nu}(\theta_{12}, \Delta_{12}) + s_{13}^4 \quad \text{with} \quad V \rightarrow c_{13}^2 V$$

# $\theta_{13}$ in Solar and KamLAND

complementarity between solar and KamLAND data



Maltoni et al., hep-ph/0405172

see also Goswami and Smirnov,  
hep-ph/0411359

KamLAND spectrum  $\Rightarrow$

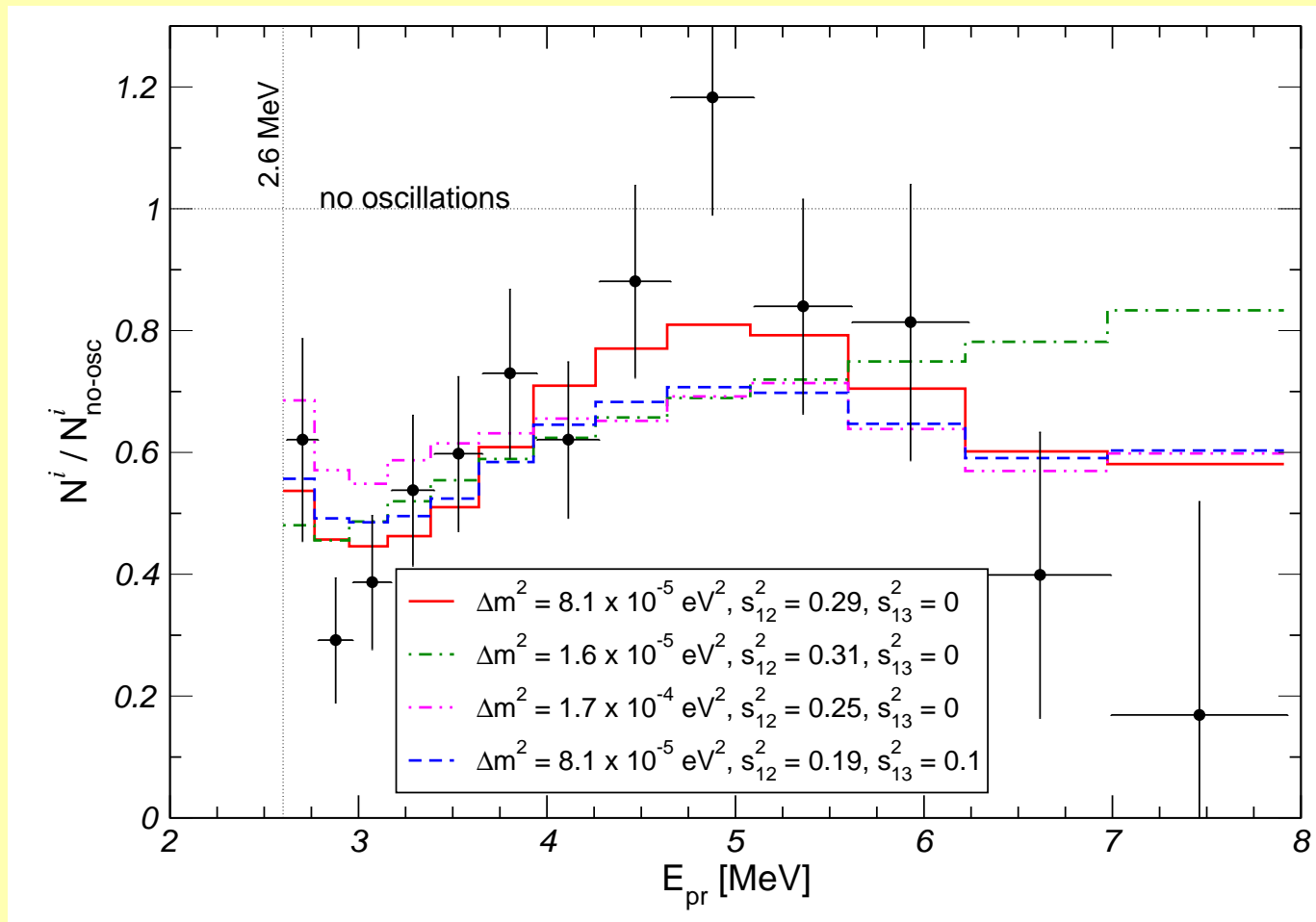
$$P_{\text{KL}} \approx (1 - 2 \sin^2 \theta_{13}) \left( 1 - \sin^2 2\theta_{12} \sin^2 \frac{\Delta m_{21}^2 L}{4E_\nu} \right)$$

$$P_{\text{Sol}} \approx (1 - 2 \sin^2 \theta_{13}) \begin{cases} \sin^2 \theta_{12} & \text{high } E_\nu \\ (1 - 0.5 \sin^2 2\theta_{12}) & \text{low } E_\nu \end{cases}$$



# The KamLAND energy spectrum

$\theta_{13}$  leads to a flatter energy spectrum



# 3-flavour effects in $\Delta m_{31}^2$ oscillations

---

$$H_{\text{mat}}^\nu = U_{23}U_{13}U_{12} \text{diag}(0, \Delta_{21}, \Delta_{31}) U_{12}^\dagger U_{13}^\dagger U_{23}^\dagger + \text{diag}(V, 0, 0)$$

for  $\Delta m_{12}^2 = 0$  and  $\theta_{13} = 0$  one gets  $\nu_\mu \rightarrow \nu_\tau$  vacuum oscillations:

$$H_{\text{mat}}^\nu = \begin{pmatrix} V & 0 \\ 0 & H^{2\nu} \end{pmatrix}, \quad \text{with} \quad H^{2\nu} = O_{23} \begin{pmatrix} 0 & 0 \\ 0 & \Delta m_{31}^2 \end{pmatrix} O_{23}^T$$

$$\Rightarrow P_{ee} = 1, P_{\mu\mu} = P^{2\nu}$$

## $\theta_{13}$ in MINOS

---

let's keep  $\Delta m_{21}^2 \approx 0$  but allow for  $\theta_{13} \neq 0$ :

$$P_{\mu\mu} = \sin^2 2\theta_{\text{eff}} \sin^2 \frac{\Delta m_{31}^2 L}{4E}, \quad \sin^2 \theta_{\text{eff}} = \sin^2 \theta_{23} \cos^2 \theta_{13}$$

neglect matter effect

# $\theta_{13}$ in MINOS

---

let's keep  $\Delta m_{21}^2 \approx 0$  but allow for  $\theta_{13} \neq 0$ :

$$P_{\mu\mu} = \sin^2 2\theta_{\text{eff}} \sin^2 \frac{\Delta m_{31}^2 L}{4E}, \quad \sin^2 \theta_{\text{eff}} = \sin^2 \theta_{23} \cos^2 \theta_{13}$$

neglect matter effect

$\nu_e$  appearance:

$$P_{\mu e} = \sin^2 \theta_{23} \sin^2 2\theta_{13} \sin^2 \frac{\Delta m_{31}^2 L}{4E} + \mathcal{O}(\Delta m_{21}^2 \theta_{13}, \Delta m_{21}^2)$$

MINOS analysis in progress ( $e^-$  detection is difficult)

expect minor improvement on CHOOZ

$\Rightarrow$  main goal of future LBL experiments (T2K, NOvA)

# *Sub-leading effects in atmospheric neutrinos*

---

$$\begin{aligned}\phi_e^{\text{obs}} &= \phi_e^0 P_{ee} + \phi_\mu^0 P_{\mu e} \\ \phi_\mu^{\text{obs}} &= \phi_\mu^0 P_{\mu\mu} + \phi_e^0 P_{e\mu}\end{aligned}$$

e-like events are a good place to look for 3-flavour effects

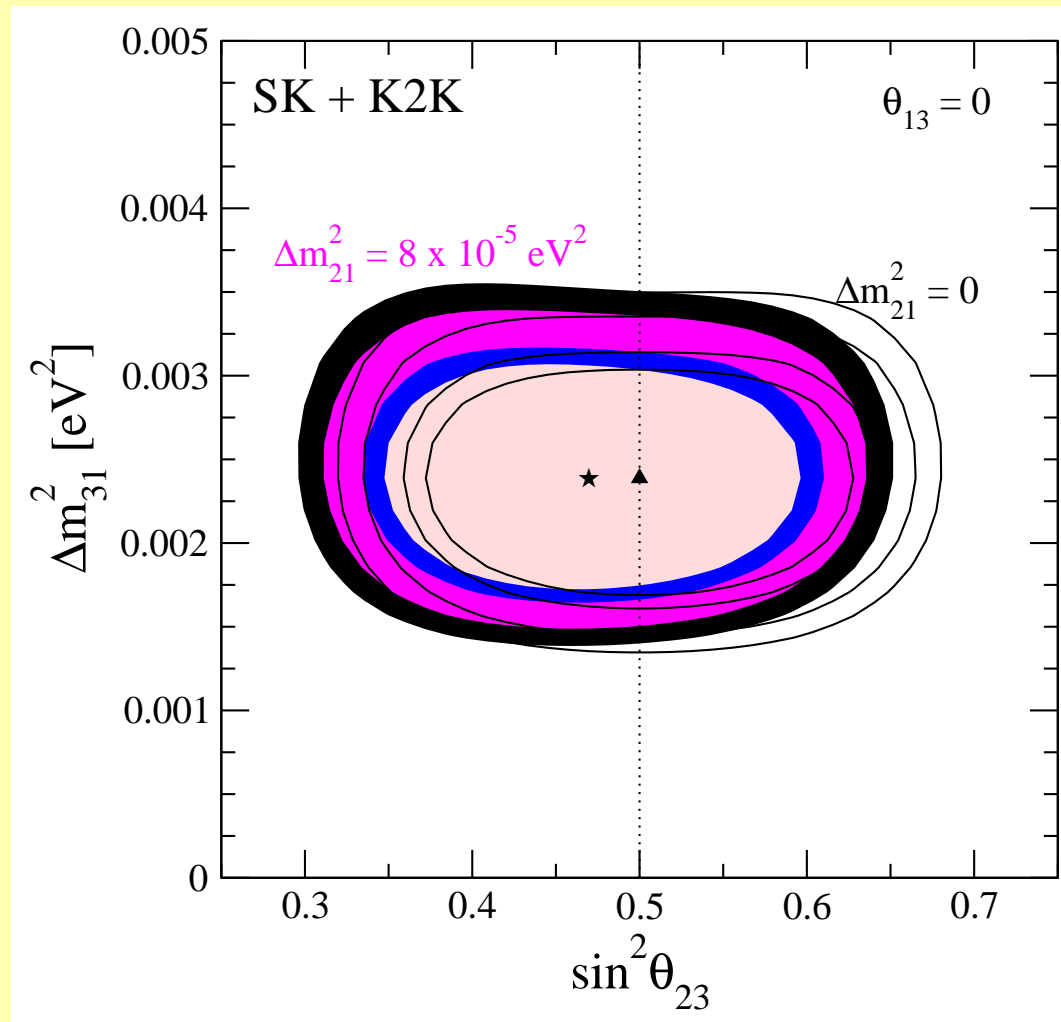
# Sub-leading effects in atmospheric neutrinos

excess of electron-like events:

$$\begin{aligned} \frac{N_e}{N_e^0} - 1 &\simeq (r s_{23}^2 - 1) P_{2\nu}(\Delta m_{31}^2, \theta_{13}) && \theta_{13}\text{-effects} \\ &+ (r c_{23}^2 - 1) P_{2\nu}(\Delta m_{21}^2, \theta_{12}) && \Delta m_{21}^2\text{-effects} \\ &- 2s_{13}s_{23}c_{23} r \operatorname{Re}(A_{ee}^* A_{\mu e}) && \text{interference: } \delta_{\text{CP}} \end{aligned}$$

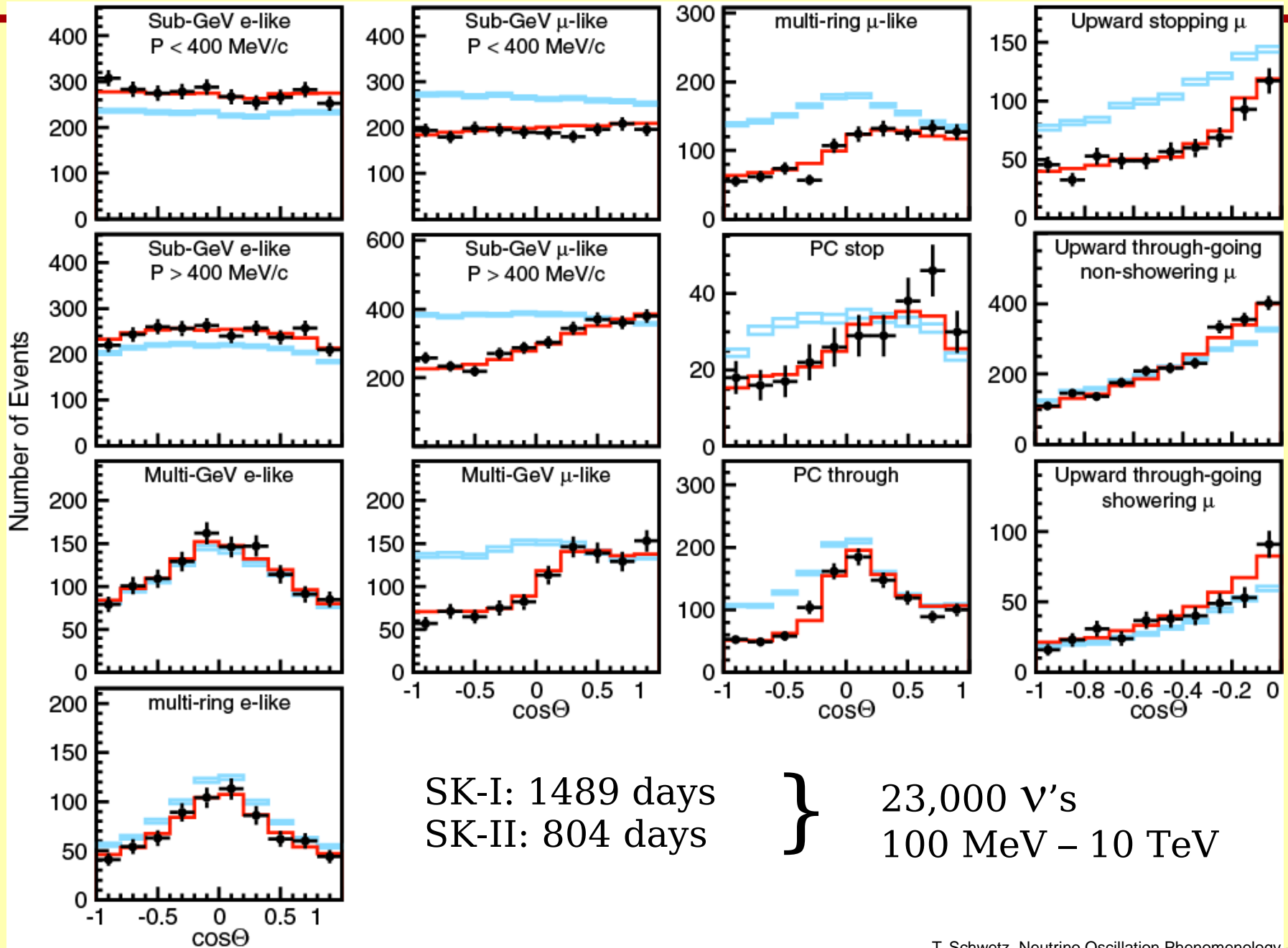
$$r = r(E_\nu) \equiv \frac{\phi_\mu^0(E_\nu)}{\phi_e^0(E_\nu)} \quad \begin{array}{l} r \approx 2 \quad (\text{sub-GeV}) \\ r \approx 2.6 - 4.5 \quad (\text{multi-GeV}) \end{array}$$

# Taking into account $\Delta m_{21}^2$



Gonzalez-Garcia, Maltoni, Smirnov, hep-ph/0408170

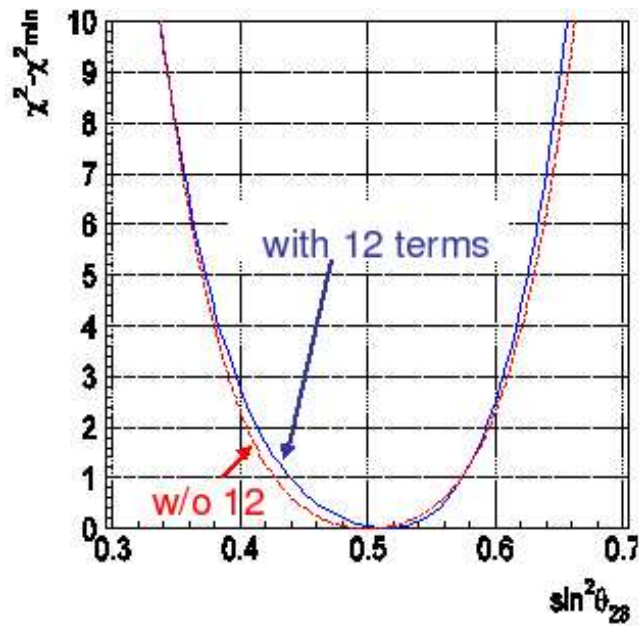
# Super-K atmospheric neutrino data





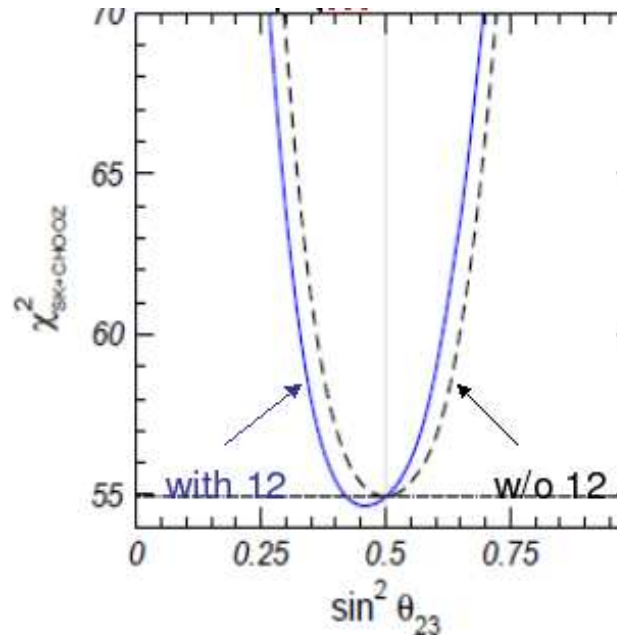
# Is there an indication for a non-max $\theta_{23}$ ?

Super-K Coll.  
T. Kajita, NuFact05



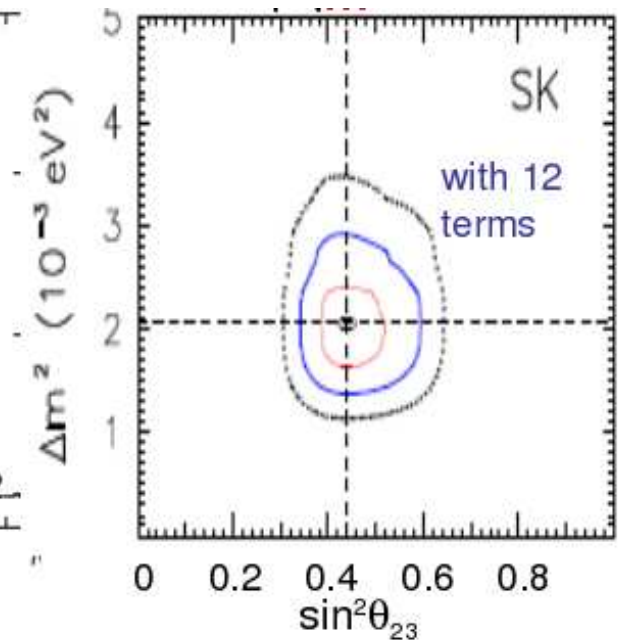
best fit:  $\sin^2 \theta_{23} = 0.51$   
max  $\theta_{23}$ :  $\Delta\chi^2 \approx 0.1$

Gonzalez-Garcia, Maltoni, Smirnov  
hep-ph/0408170



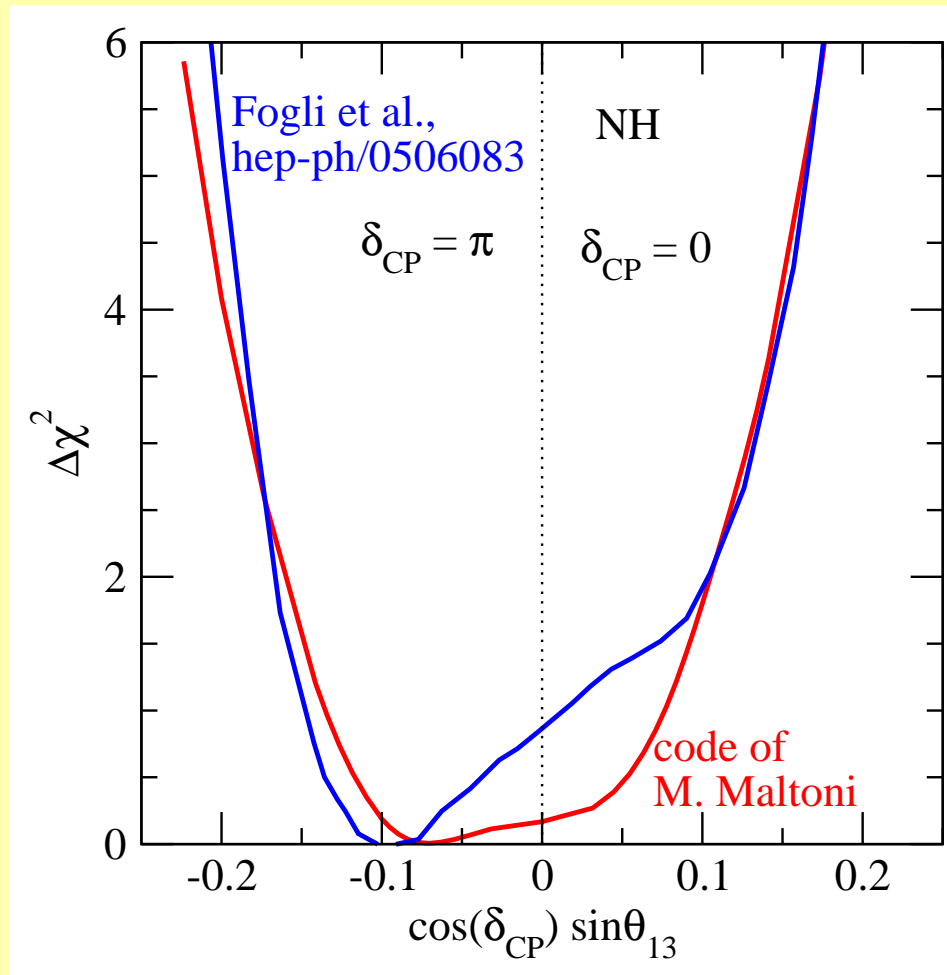
$\sin^2 \theta_{23} = 0.46$   
 $\Delta\chi^2 \approx 0.3$

Fogli et al.,  
hep-ph/0506083



$\sin^2 \theta_{23} = 0.44$   
 $\Delta\chi^2 \approx 0.8$

# Is there an indication for $\theta_{13} \neq 0$ ?



Bari: best fit:  $\sin^2 \theta_{13} \approx 0.01$ ,  $\Delta\chi^2 \approx 0.85$  for  $\theta_{13} = 0$

Maltoni: best fit:  $\sin^2 \theta_{13} \approx 0.005$ ,  $\Delta\chi^2 \approx 0.16$  for  $\theta_{13} = 0$

# Effects of $\delta_{\text{CP}}$

To observe an effect of  $\delta_{\text{CP}}$  one needs

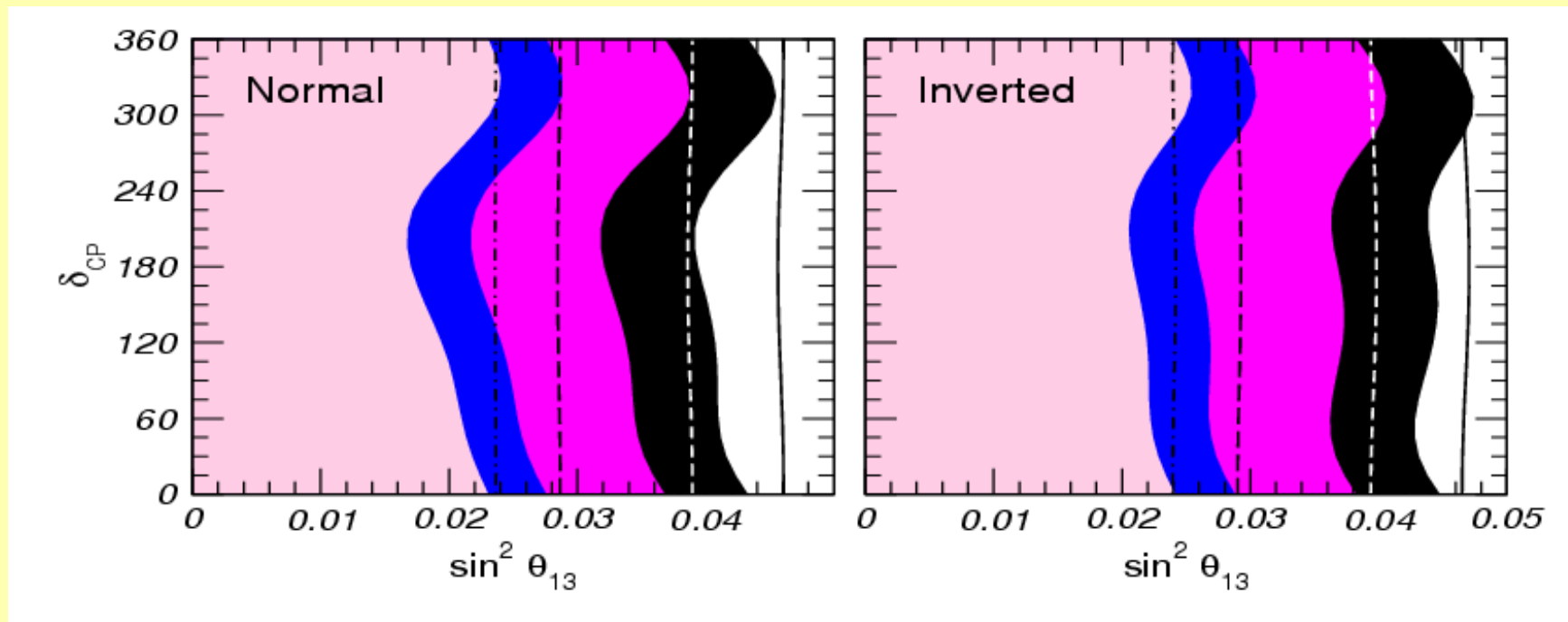
- $\theta_{13} \neq 0$ , and
- sensitivity to  $\Delta m_{21}^2$

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & e^{-i\delta} s_{13} \\ 0 & 1 & 0 \\ -e^{i\delta} s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$H_{\text{mat}}^\nu = U_{23}U_{13}U_{12} \text{diag}(0, \Delta_{21}, \Delta_{31}) U_{12}^\dagger U_{13}^\dagger U_{23}^\dagger + \text{diag}(V, 0, 0)$$

# $\delta_{CP}$ effects in present data

bound on  $\theta_{13}$  depends on  $\delta_{CP}$  and on hierarchy:  
(atmospheric data)



Gonzalez-Garcia, Maltoni, 0704.1800

---

# Summary 3-flavour oscillation parameters

# Three flavour osc. parameters summary

## mass-squared differences:

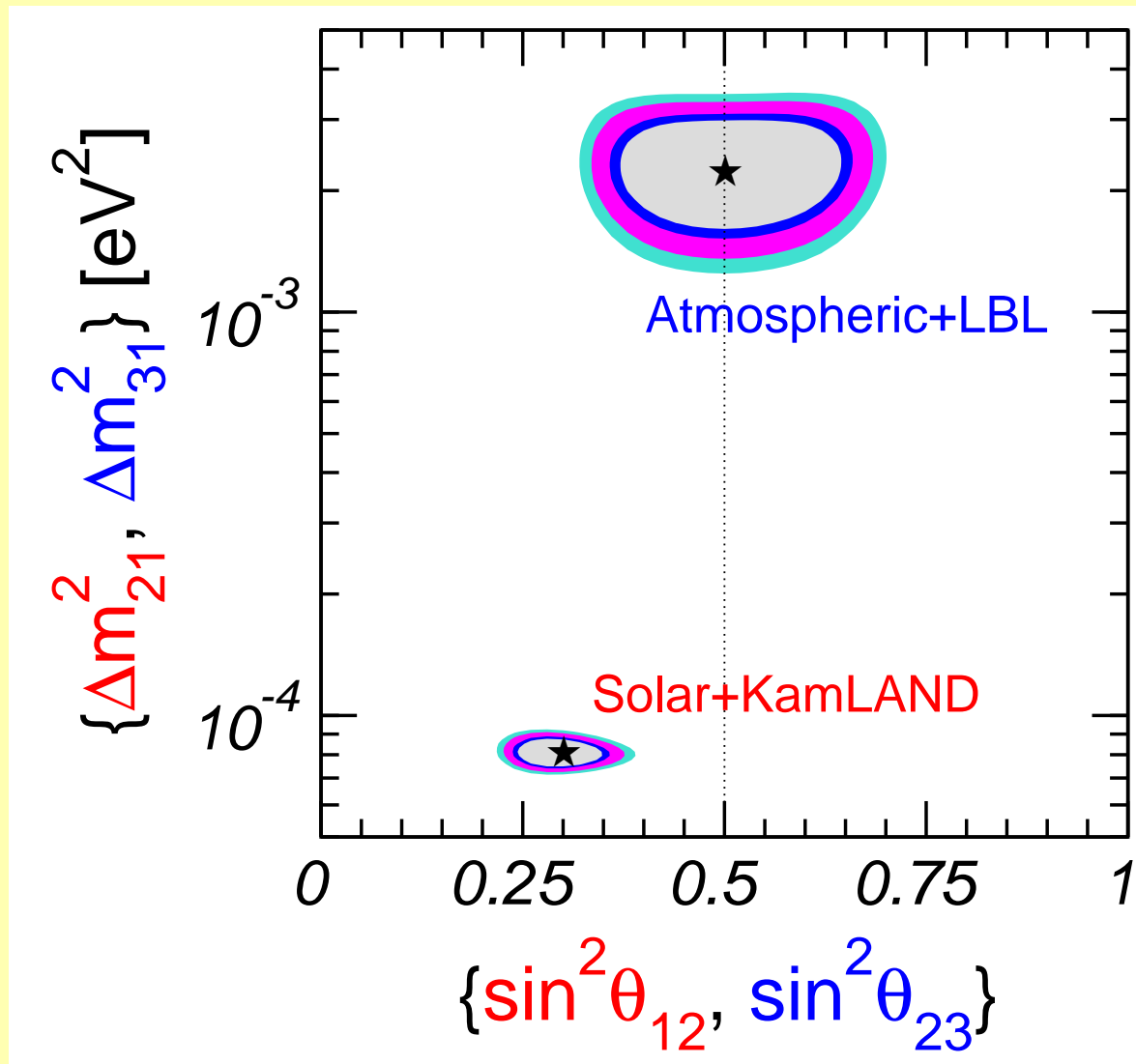
parameter	bf $\pm 1\sigma$	1 $\sigma$ acc.	3 $\sigma$ range
$\Delta m_{21}^2$ [ $10^{-5}\text{eV}^2$ ]	$7.59 \pm 0.21$	2.8%	7.05 – 8.35
$ \Delta m_{31}^2 $ [ $10^{-3}\text{eV}^2$ ]	$2.40^{+0.12}_{-0.10}$	4.6%	2.07 – 2.76

## mixing angles:

parameter	bf $\pm 1\sigma$	1 $\sigma$ acc.	3 $\sigma$ range
$\sin^2 \theta_{12}$	$0.31^{+0.016}_{-0.023}$	6.3%	0.25 – 0.37
$\sin^2 \theta_{23}$	$0.50^{+0.07}_{-0.06}$	13%	0.36 – 0.67
$\sin^2 \theta_{13}$	$0.01^{+0.016}_{-0.01}$	—	$\leq 0.056$

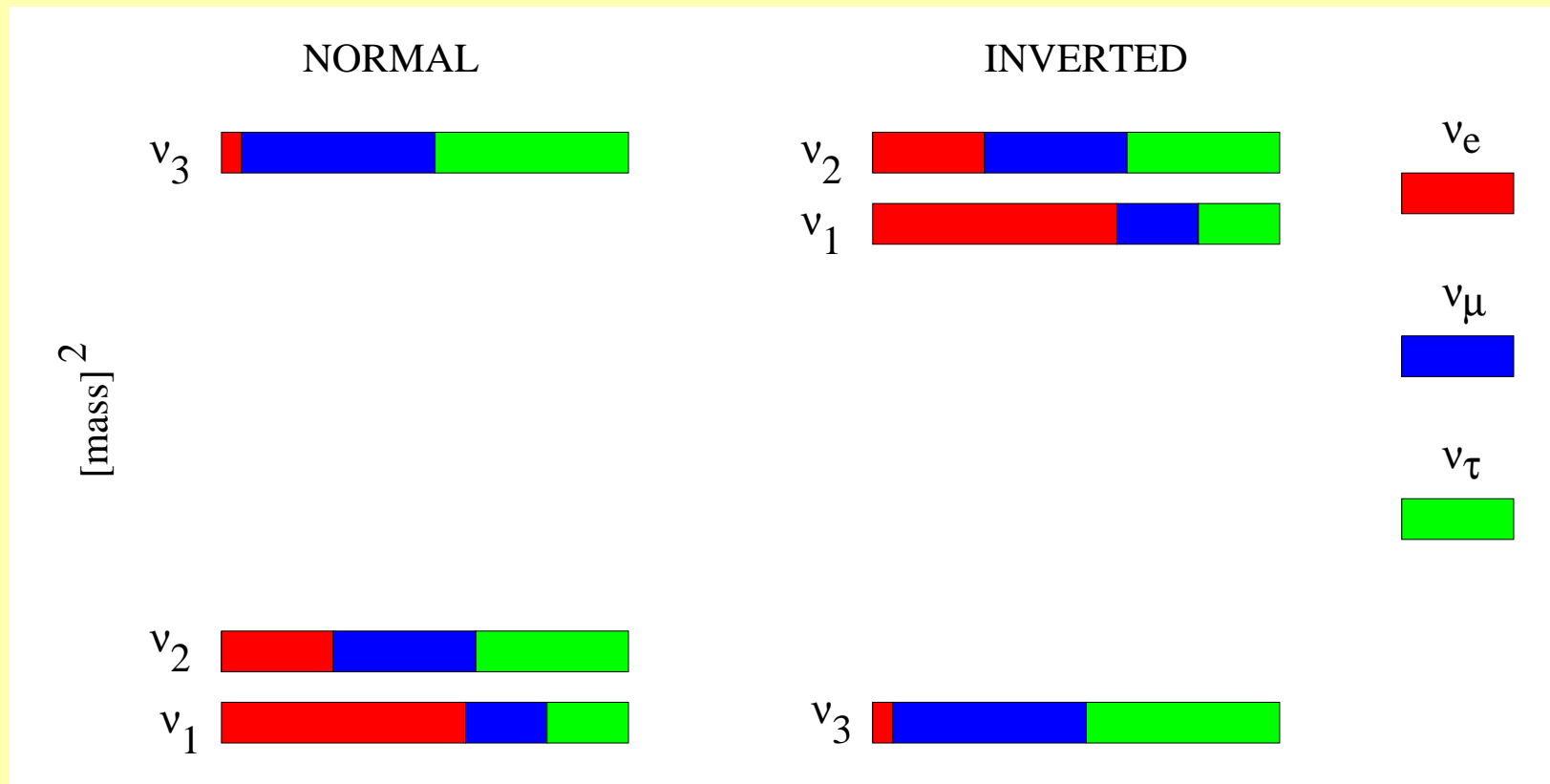
Schwet, Tortola, Valle, in preparation

# Three flavour osc. parameters summary



# Three flavour osc. parameters summary

two possibilities for the neutrino mass spectrum



$$\Delta m_{31}^2 > 0$$

$$\Delta m_{31}^2 < 0$$



# *The 1-2 mass ordering*

---

We know that the mass state containing most of  $\nu_e$  is the lighter of the two “solar mass” states

$$\Delta m_{21}^2 \equiv m_2^2 - m_1^2 > 0 \quad \text{and} \quad \theta_{12} < 45^\circ$$

thanks to the observation of the matter effect in the sun:

resonance condition:

$$\Delta m_{21}^2 \cos 2\theta_{12} = 2E_\nu V \quad \Rightarrow \quad \Delta m_{21}^2 \cos 2\theta_{12} > 0$$

# The 1-3 mass ordering

---

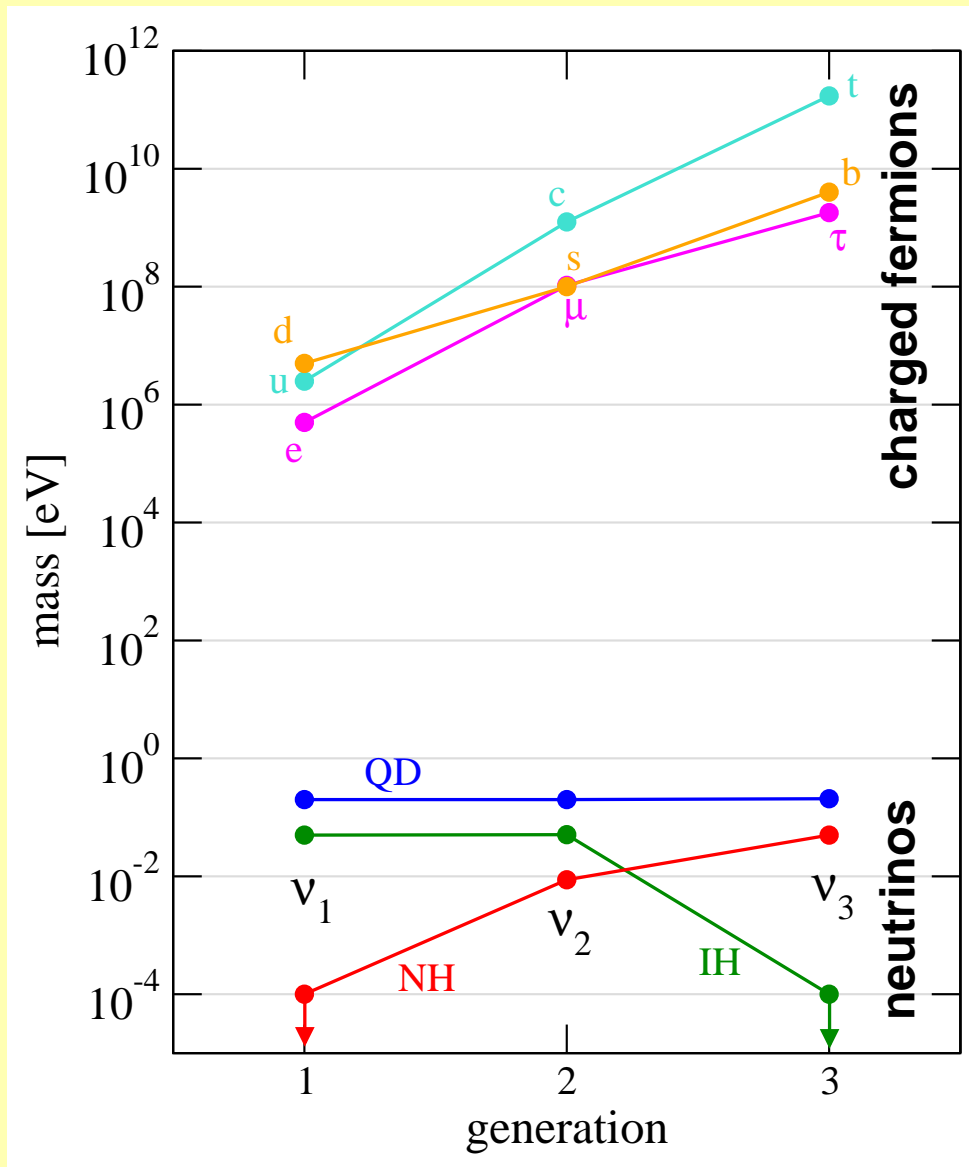
We do not know the sign of  $\Delta m_{31}^2$ !  
(normal or inverted mass ordering)

No matter effect has been observed for oscillations with  $\Delta m_{31}^2$ , only “vacuum”  $\nu_\mu \rightarrow \nu_\mu(\nu_\tau)$  oscillations:

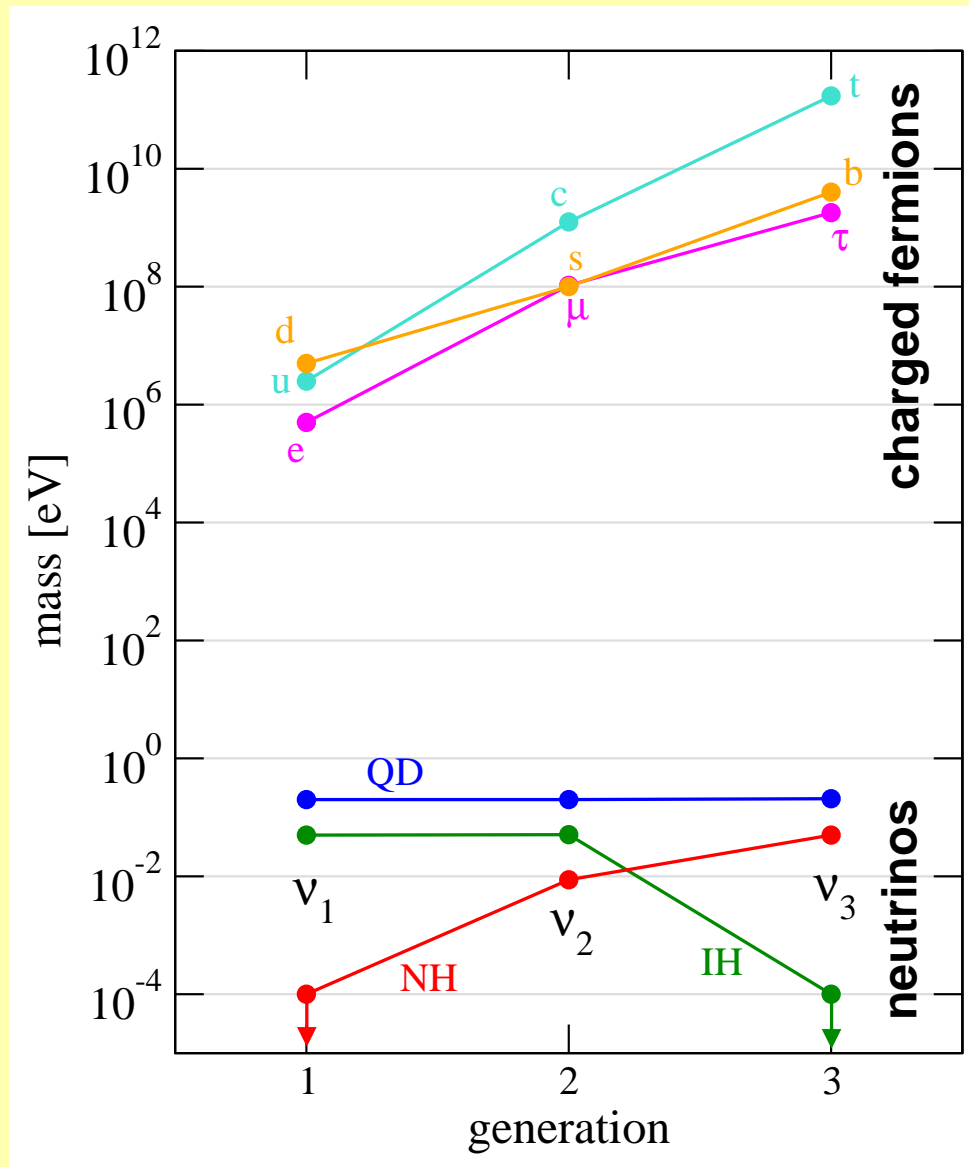
$$P_{\mu\mu} \approx 1 - \sin^2 2\theta_{23} \sin^2 \frac{\Delta m_{31}^2 L}{4E}$$

Has to look for matter effect in  $\nu_e \leftrightarrow \nu_\mu$  oscillations due to  $\Delta m_{31}^2, \theta_{13}$   
 $\Rightarrow$  future long-baseline experiments

# Why are neutrino masses so small?



# Why are neutrino masses so small?

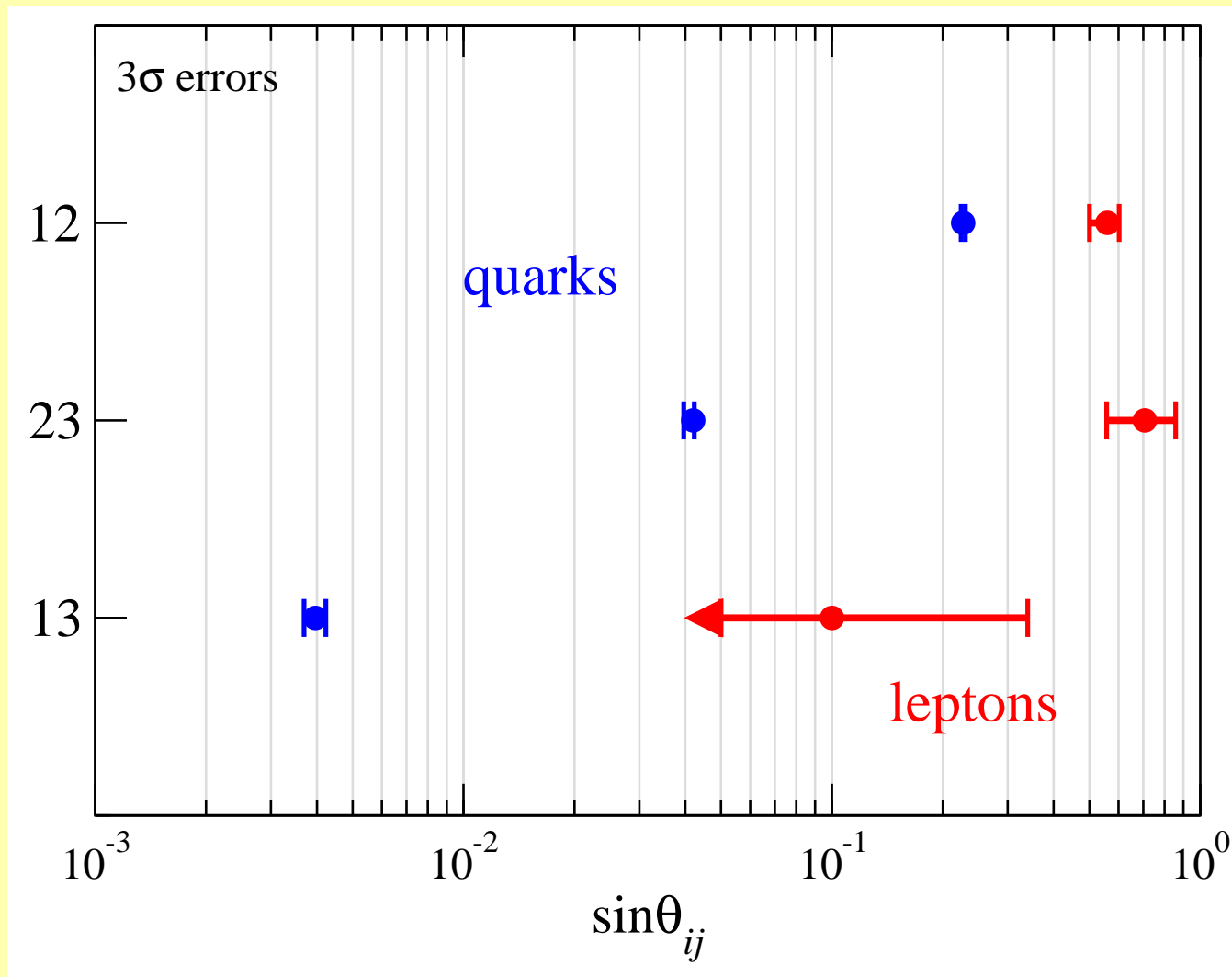


Is the smallness of  $m_\nu$  related to a high scale  $\Lambda$  (GUT scale?) via the seesaw mechanism?

$$m_\nu \sim \frac{v^2}{\Lambda}$$

$$v \sim 174 \text{ GeV}$$

# Why is lepton mixing large?



# Why is lepton mixing large?

---

Lepton mixing:

$$U_{PMNS} = \frac{1}{\sqrt{3}} \begin{pmatrix} \mathcal{O}(1) & \mathcal{O}(1) & \epsilon \\ \mathcal{O}(1) & \mathcal{O}(1) & \mathcal{O}(1) \\ \mathcal{O}(1) & \mathcal{O}(1) & \mathcal{O}(1) \end{pmatrix}$$

Quark mixing:

$$U_{CKM} = \begin{pmatrix} 1 & \epsilon & \epsilon \\ \epsilon & 1 & \epsilon \\ \epsilon & \epsilon & 1 \end{pmatrix}$$

# *Is there a special pattern in lepton mixing?*

---

## example: Tri-bimaximal mixing

Harrison, Perkins, Scott, PLB 2002, hep-ph/0202074

$$\sin^2 \theta_{12} = 1/3, \quad \sin^2 \theta_{23} = 1/2, \quad \sin^2 \theta_{13} = 0 \quad \Rightarrow$$

$$U = \begin{pmatrix} \sqrt{2/3} & 1/\sqrt{3} & 0 \\ -1/\sqrt{6} & 1/\sqrt{3} & 1/\sqrt{2} \\ 1/\sqrt{6} & -1/\sqrt{3} & 1/\sqrt{2} \end{pmatrix}$$

# *3-flavour oscillations*

---

Open questions:



# *3-flavour oscillations*

---

## Open questions:

- Is this basic picture correct?  
LSND hint?  
non-standard effects beyond oscillations?

# *3-flavour oscillations*

---

## Open questions:

- Is this basic picture correct?  
LSND hint?  
non-standard effects beyond oscillations?
- Increase the precision on solar and atmospheric parameters (e.g. Is  $\theta_{23}$  exactly  $45^\circ$ ?)

# *3-flavour oscillations*

---

## Open questions:

- Is this basic picture correct?  
LSND hint?  
non-standard effects beyond oscillations?
- Increase the precision on solar and atmospheric parameters (e.g. Is  $\theta_{23}$  exactly  $45^\circ$ ?)
- How small is  $\theta_{13}$ ?

# *3-flavour oscillations*

---

## Open questions:

- Is this basic picture correct?  
LSND hint?  
non-standard effects beyond oscillations?
- Increase the precision on solar and atmospheric parameters (e.g. Is  $\theta_{23}$  exactly  $45^\circ$ ?)
- How small is  $\theta_{13}$ ?
- What is the value of the CP phase  $\delta$ ?

# 3-flavour oscillations

---

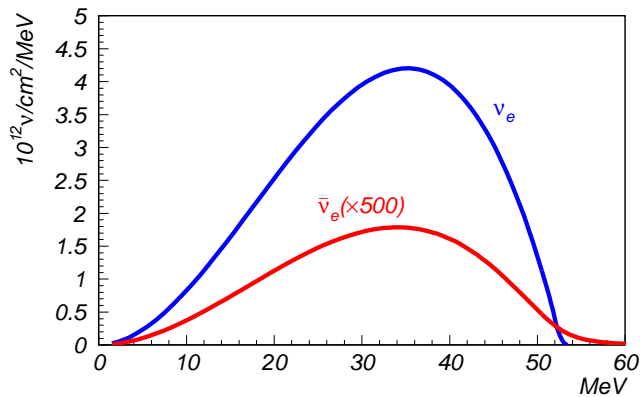
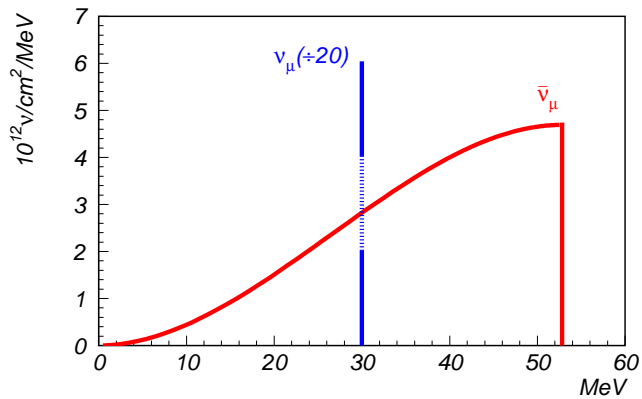
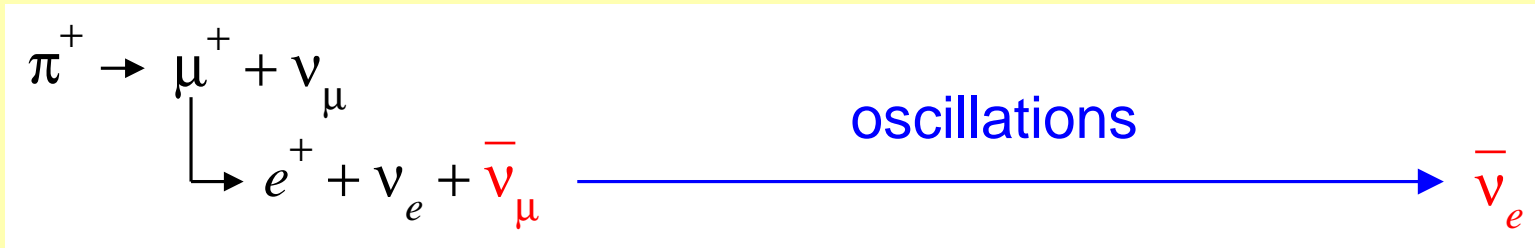
## Open questions:

- Is this basic picture correct?  
LSND hint?  
non-standard effects beyond oscillations?
- Increase the precision on solar and atmospheric parameters (e.g. Is  $\theta_{23}$  exactly  $45^\circ$ ?)
- How small is  $\theta_{13}$ ?
- What is the value of the CP phase  $\delta$ ?
- Type of the neutrino mass ordering (sign of  $\Delta m_{31}^2$ )

---

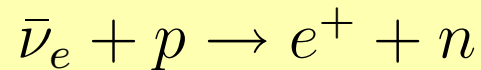
# The LSND puzzle

# The LSND signal

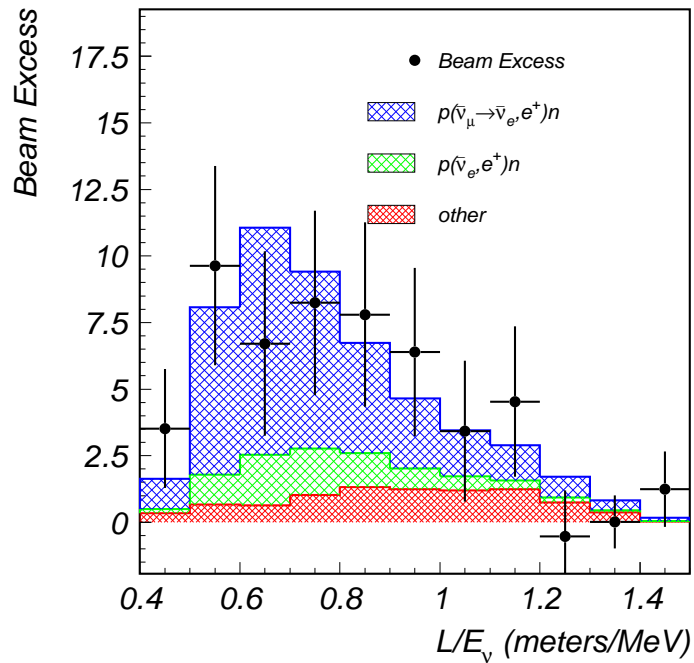
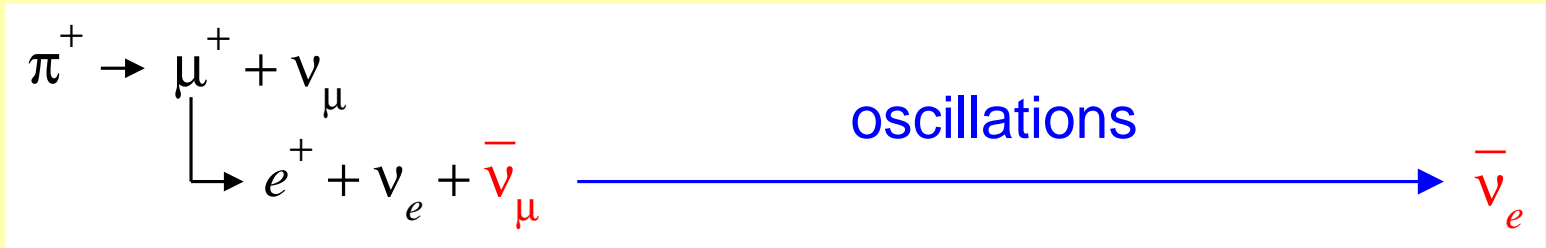


$L \simeq 35 \text{ m}$

signal:



# The LSND signal



$$L \simeq 35 \text{ m}$$

**evidence for  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  oscillations**

A. Aguilar *et al.*, PRD 64 (2001) 112007

$87.9 \pm 22.4 \pm 6.0$  excess events

$P = (0.264 \pm 0.067 \pm 0.045)\%$

$\sim 3.3\sigma$  away from zero

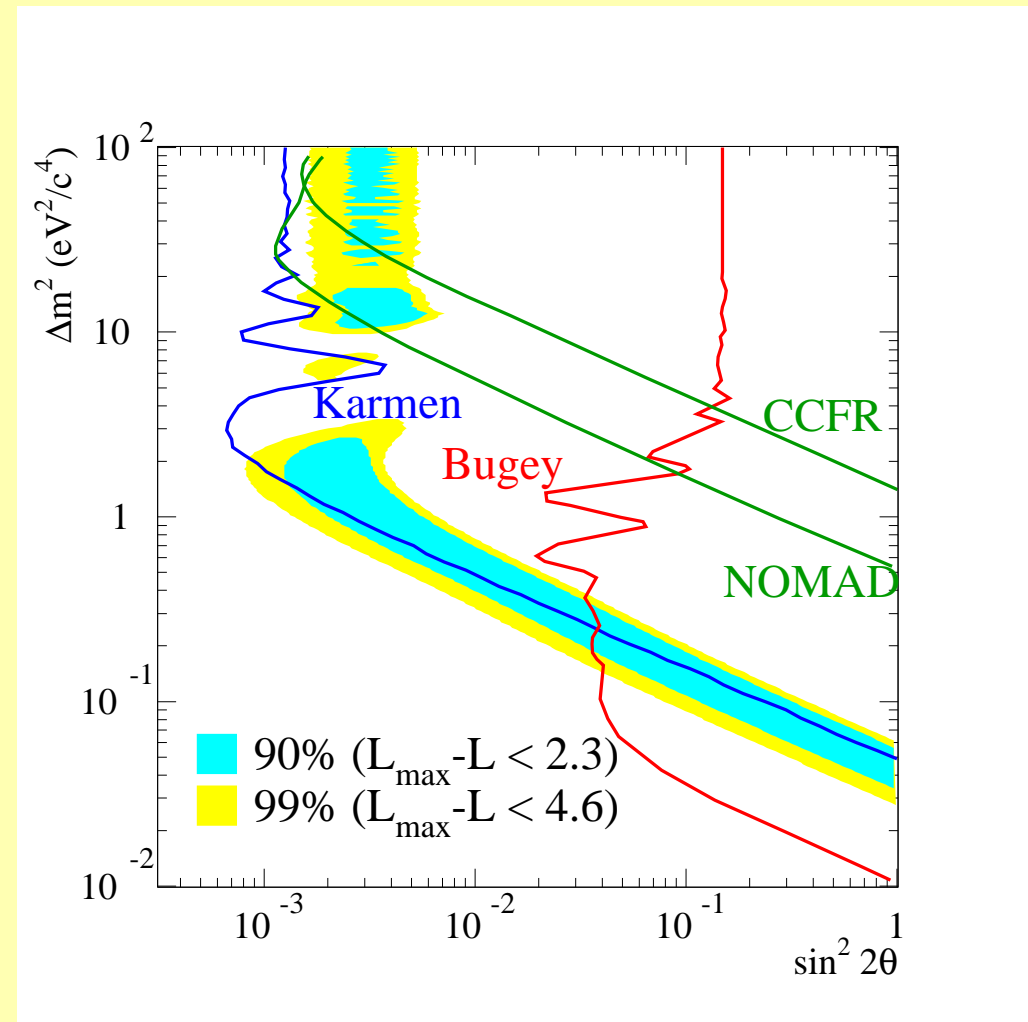


# Oscillation interpretation of LSND

several bounds from other  
no-evidence SBL experi-  
ments, (**KARMEN**)

combined analysis of  
LSND and KARMEN:

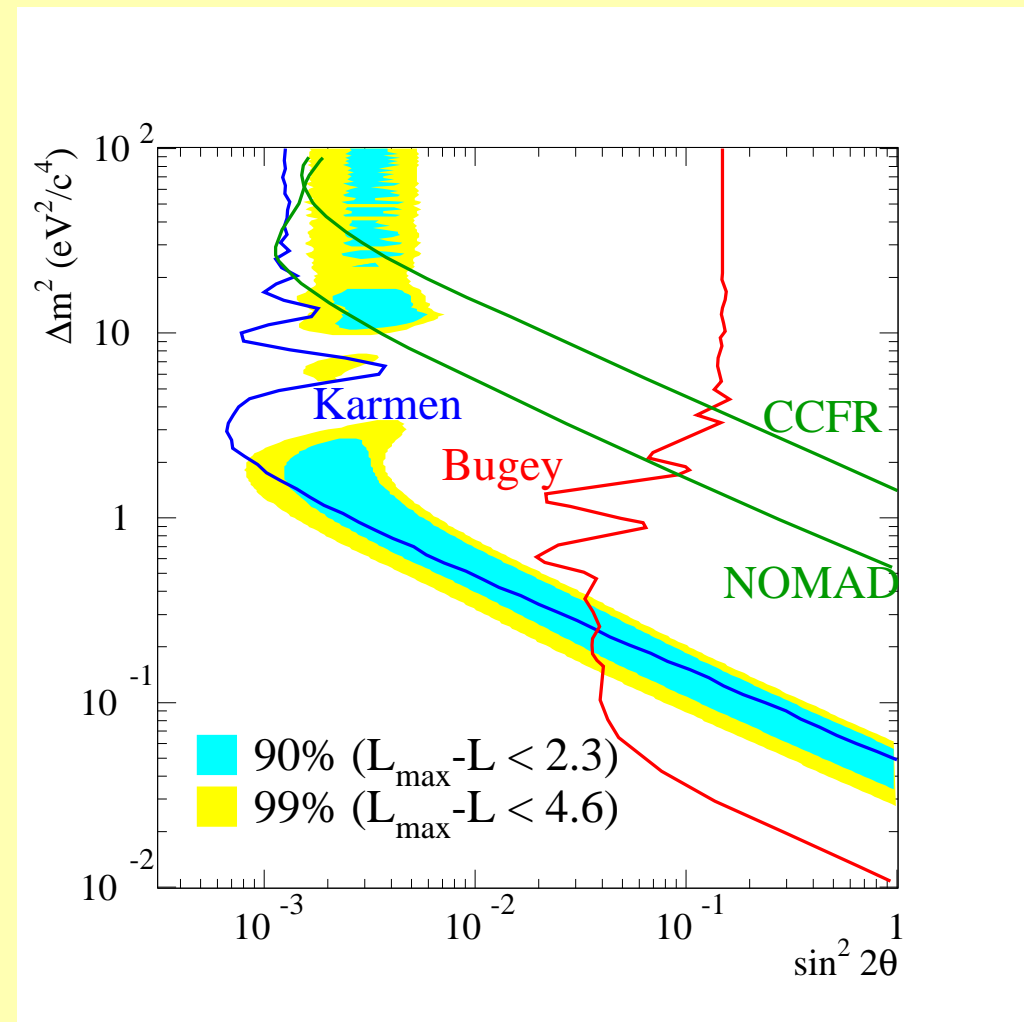
Church, Eitel, Mills, Steidl, PRD (2002)



# Oscillation interpretation of LSND

**the problem:**

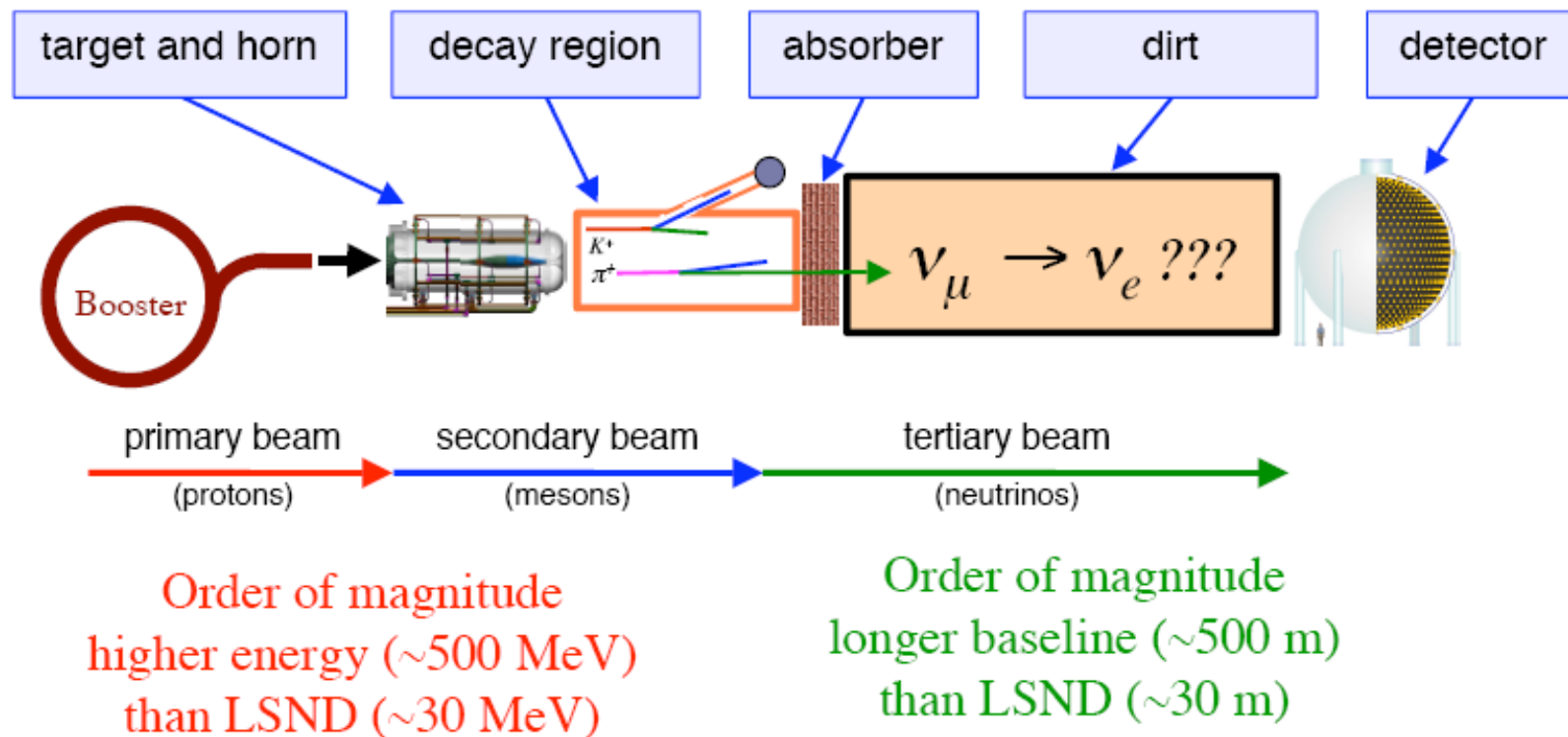
$\Delta m^2 \sim eV^2$  not consistent  
with solar ( $8 \times 10^{-5}$ )  
and atmospheric ( $2 \times 10^{-3}$ )  
mass splittings for three  
neutrinos!



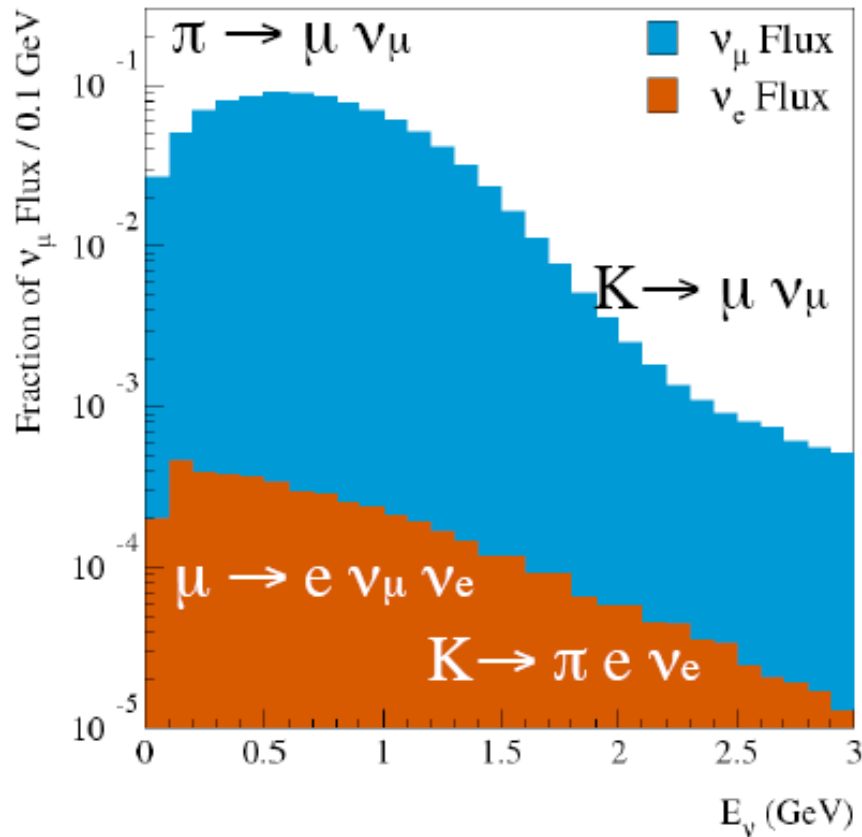
## MiniBooNE's Design Strategy...

Keep L/E same  
while changing systematics, energy & event signature

$$P(\nu_{\mu} \rightarrow \nu_e) = \sin^2 2\theta \sin^2(1.27 \Delta m^2 L/E)$$



# MiniBooNE neutrino flux



$$\nu_e / \nu_\mu = 0.5\%$$

Antineutrino content: 6%

“Intrinsic”  $\nu_e + \bar{\nu}_e$  sources:

$$\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e \quad (52\%)$$

$$\text{K}^+ \rightarrow \pi^0 e^+ \nu_e \quad (29\%)$$

$$\text{K}^0 \rightarrow \pi e \nu_e \quad (14\%)$$

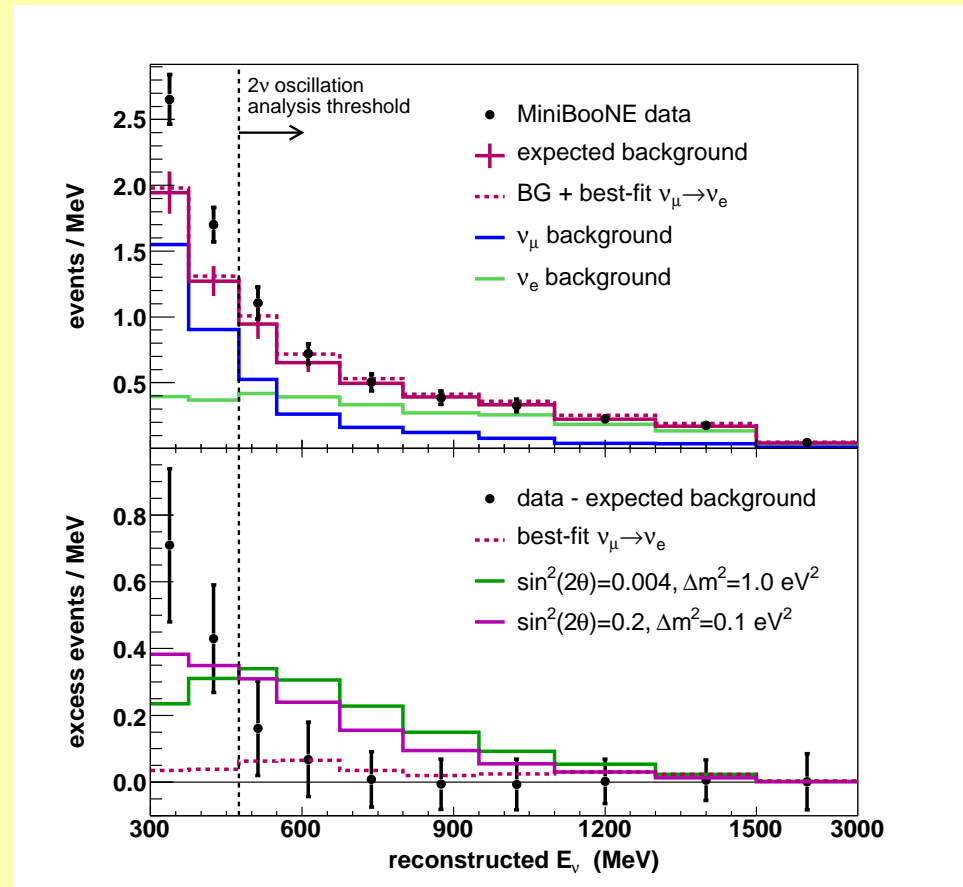
$$\text{Other} \quad (5\%)$$

# MiniBooNE results, April 2007

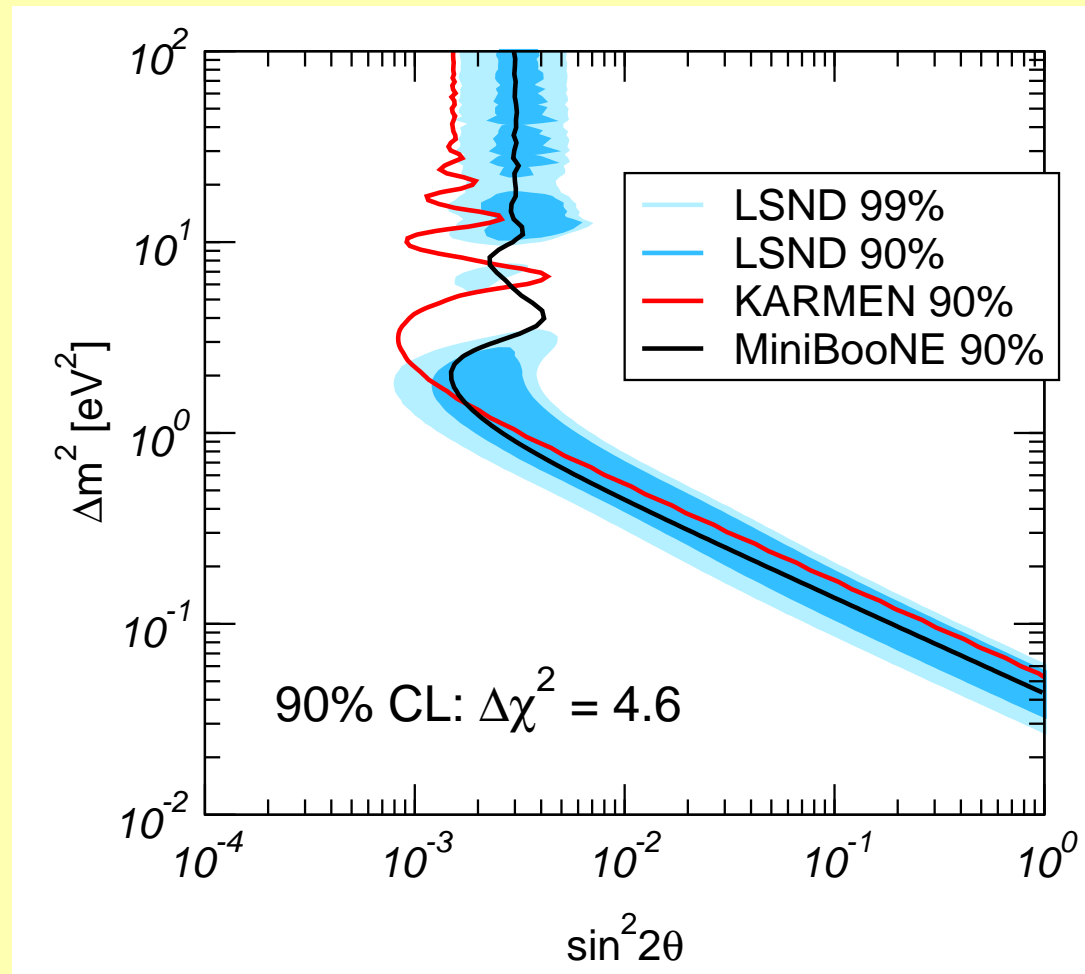
obs. events minus  
background:

$475 < E_{\nu}^{\text{QE}} < 1250 \text{ MeV}$ :  
 $22 \pm 19 \pm 35$  events  
(consistent with zero)

$300 < E_{\nu}^{\text{QE}} < 475 \text{ MeV}$ :  
 $96 \pm 17 \pm 20$  events  
(excess at  $3.6\sigma$ )



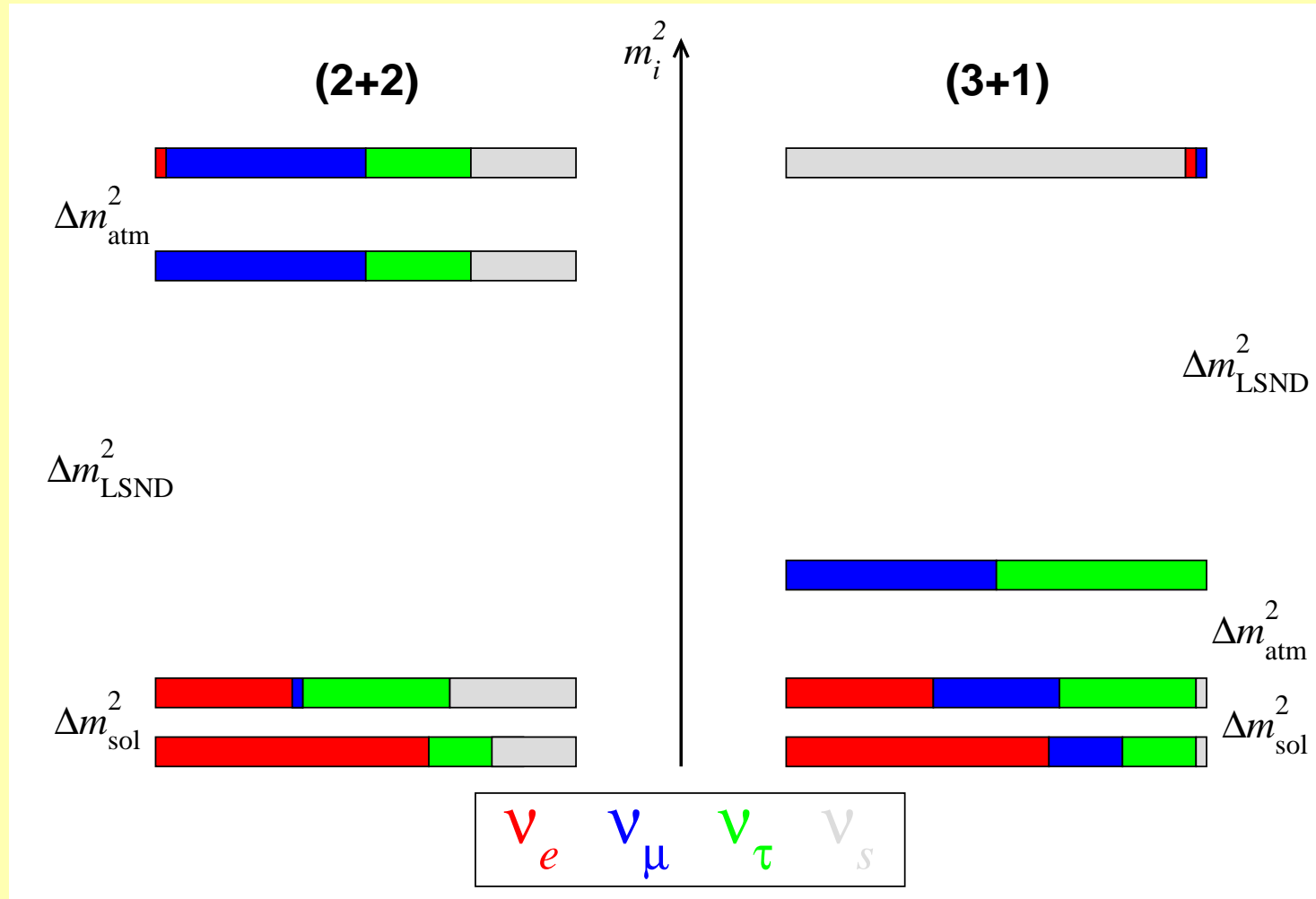
# The MiniBooNE 2-neutrino limit



In the 2-neutrino framework MiniBooNE and LSND are incompatible at the 98% CL Aguilar-Arevalo et al., PRL08

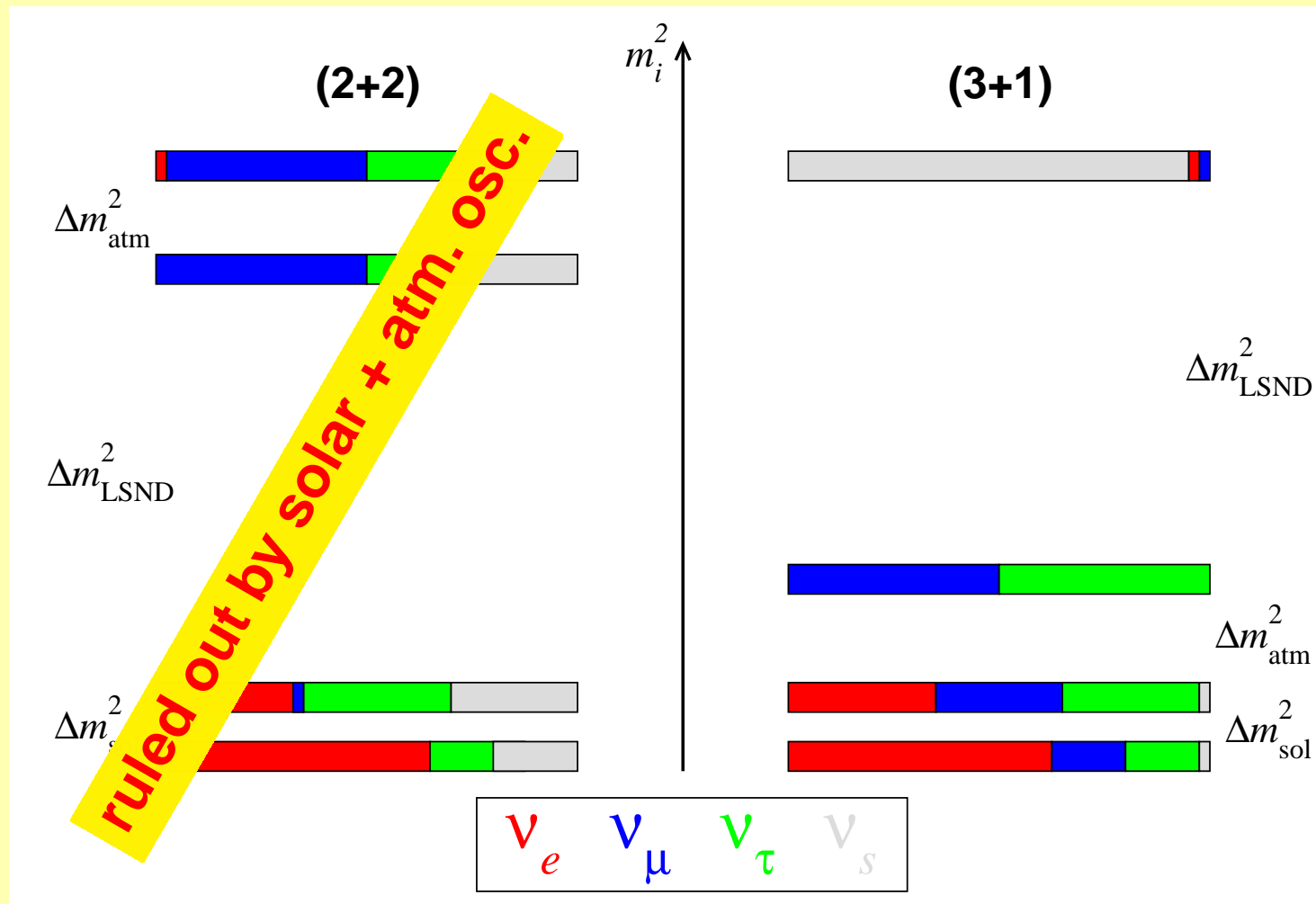
# Adding a sterile neutrino

## 4-neutrino mass schemes:



# Adding a sterile neutrino

## 4-neutrino mass schemes:





# *MB vs LSND in (3+1)*

---

In (3+1) schemes the SBL appearance probability is effectively 2- $\nu$  oscillations:

$$P_{\mu e} = \sin^2 2\theta_{\text{SBL}} \sin^2 \frac{\Delta m_{41}^2 L}{4E}$$

with

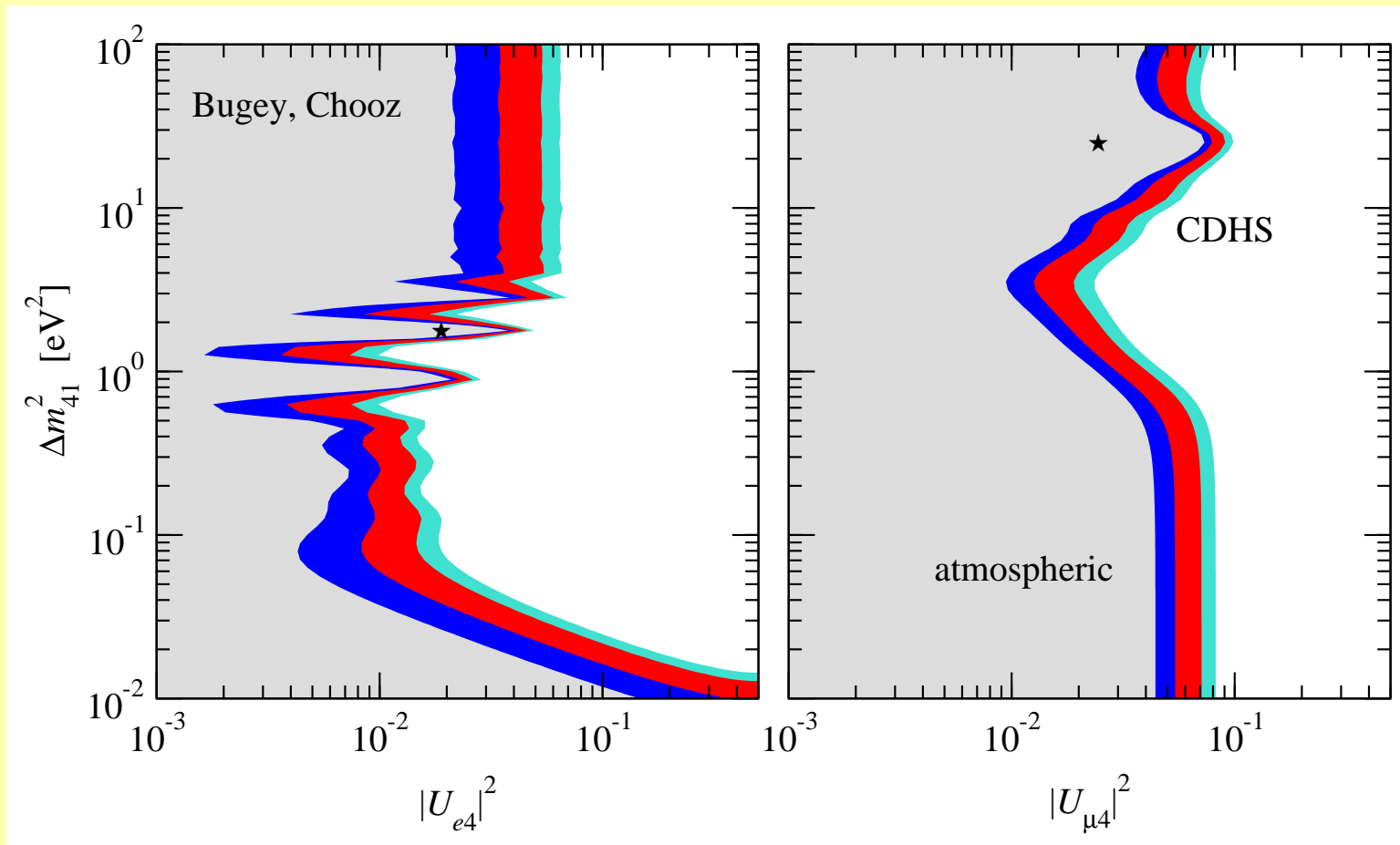
$$\sin^2 2\theta_{\text{SBL}} = 4|U_{e4}|^2|U_{\mu4}|^2$$

LSND / MiniBooNE inconsistency is the same as in the 2-flavour analysis presented by the MiniBooNE collaboration (98% CL)

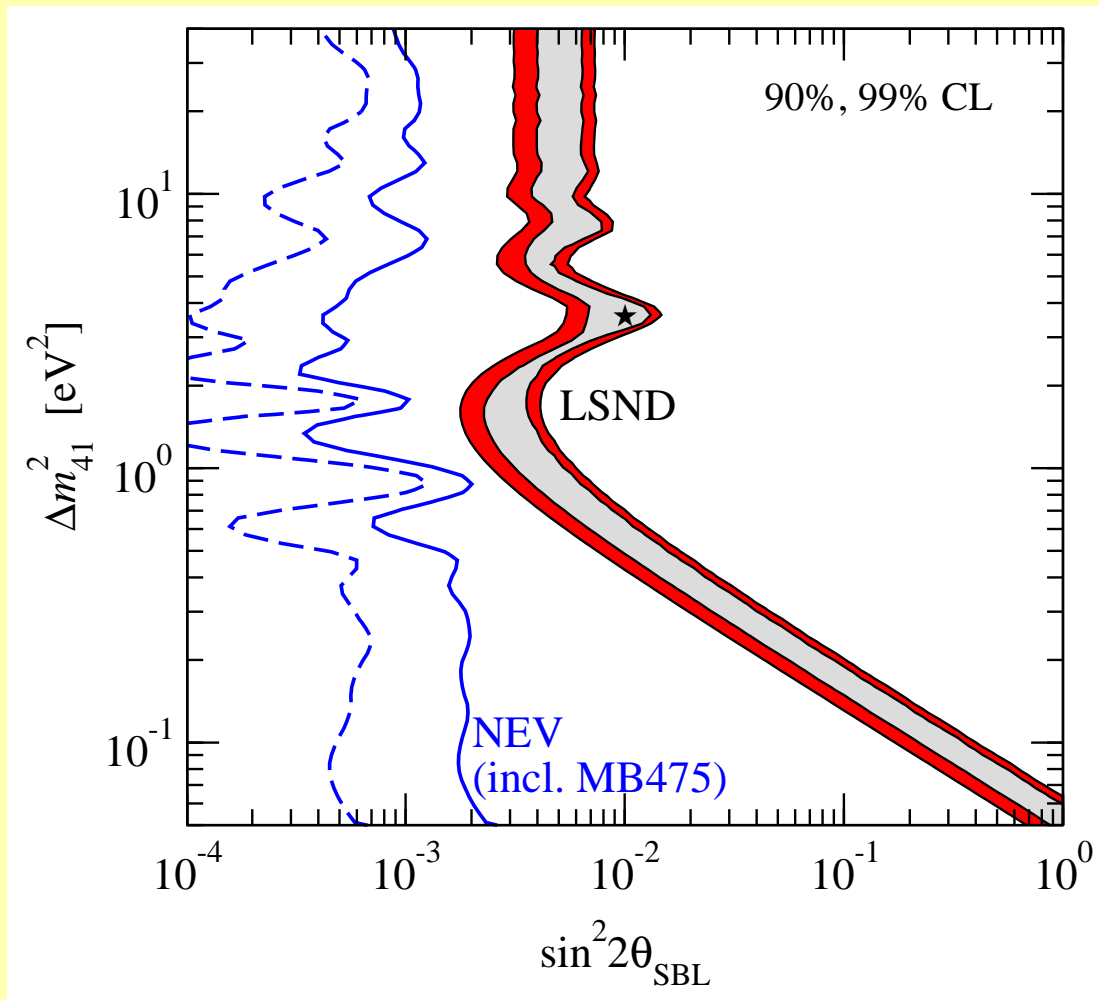
# Appearance vs disappearance in (3+1)

appearance amplitude  $\sin^2 2\theta_{\text{SBL}} = 4|U_{e4}|^2|U_{\mu4}|^2$

disappearance experiments bound  $|U_{e4}|^2$  and  $|U_{\mu4}|^2$



# *(3+1) global*



before MB:

$$\chi_{\text{PG}}^2 = 20.9 \text{ (2 dof)}$$

MB incl.:

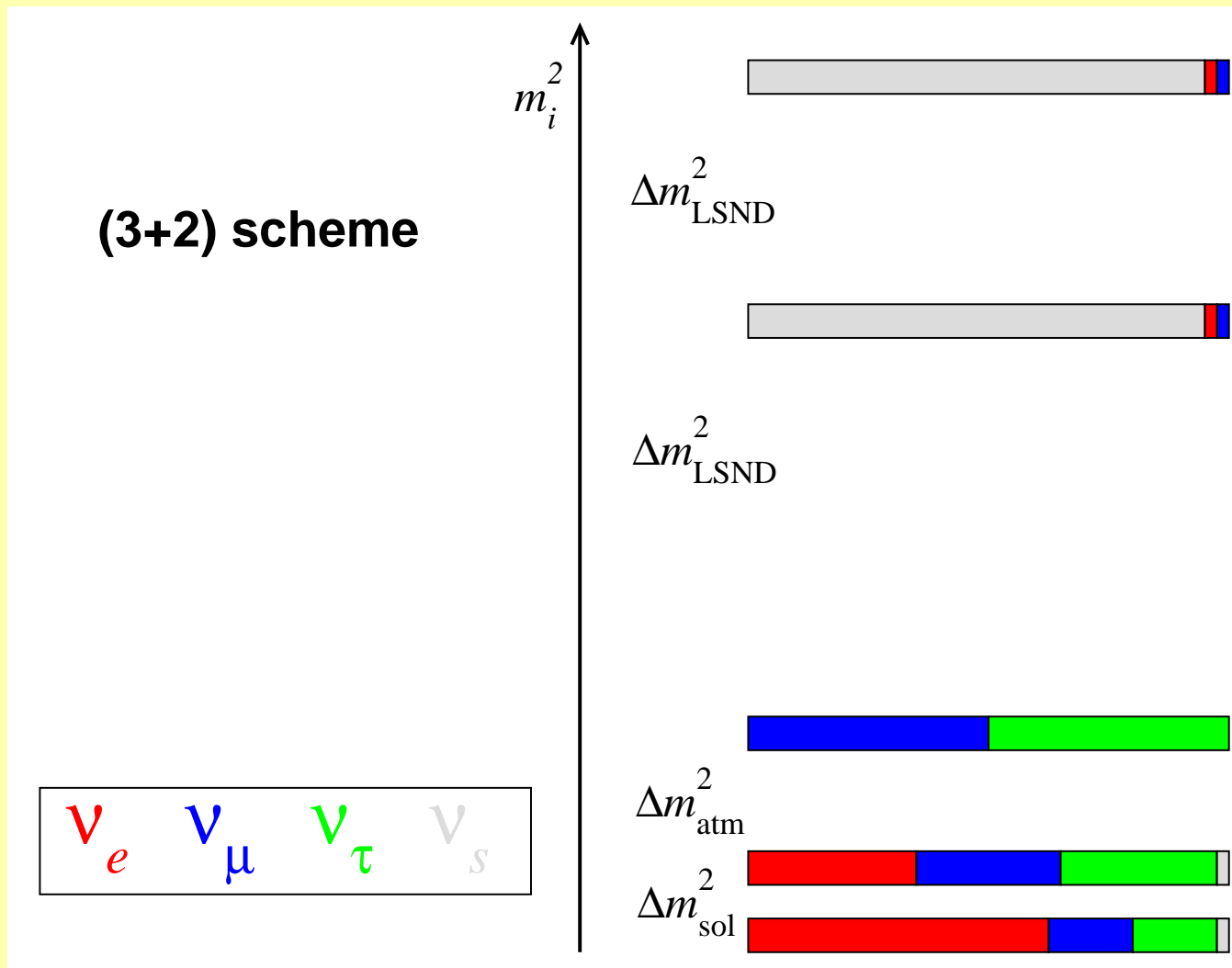
$$\chi_{\text{PG}}^2 = 24.7 \text{ (2 dof)}$$

disagreement at  
about  $4\sigma$

---

# More sterile neutrinos?

# 5-neutrino oscillations



Sorel, Conrad, Shaevitz, hep-ph/0305255

## *(3+2) appearance probability*

---

$$\begin{aligned} P_{\nu_\mu \rightarrow \nu_e} &= 4 |U_{e4}|^2 |U_{\mu4}|^2 \sin^2 \phi_{41} \\ &+ 4 |U_{e5}|^2 |U_{\mu5}|^2 \sin^2 \phi_{51} \\ &+ 8 |U_{e4} U_{\mu4} U_{e5} U_{\mu5}| \sin \phi_{41} \sin \phi_{51} \cos(\phi_{54} - \delta) \end{aligned}$$

with the definitions

$$\phi_{ij} \equiv \frac{\Delta m_{ij}^2 L}{4E}, \quad \delta \equiv \arg(U_{e4}^* U_{\mu4} U_{e5} U_{\mu5}^*) .$$

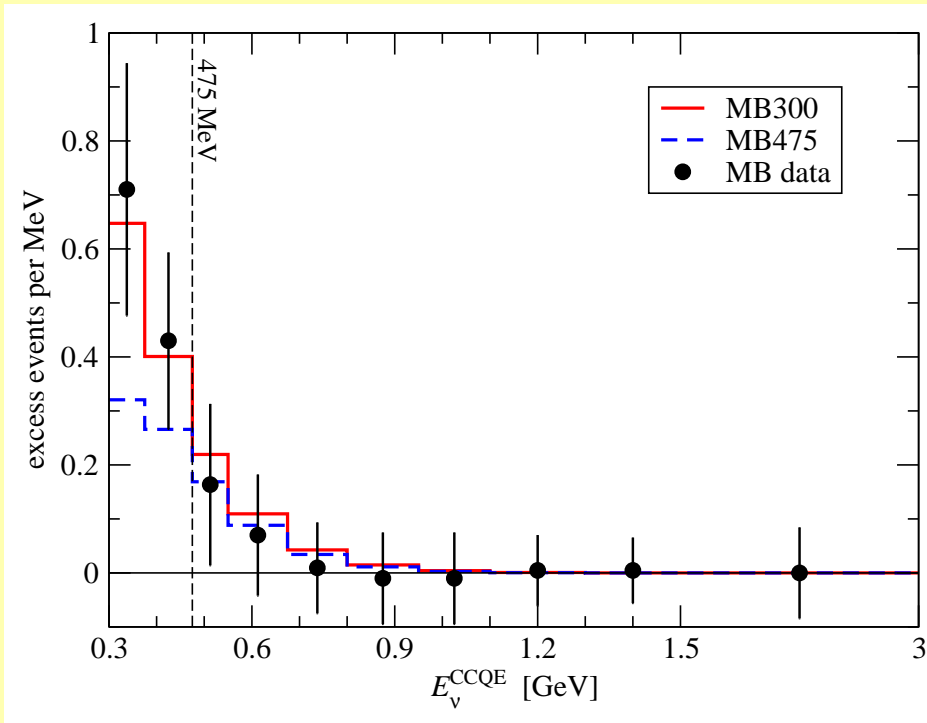
(3+2) osc. include the possibility of **CP violation!**

remember: MiniBooNE: neutrinos, LSND: anti-neutrinos

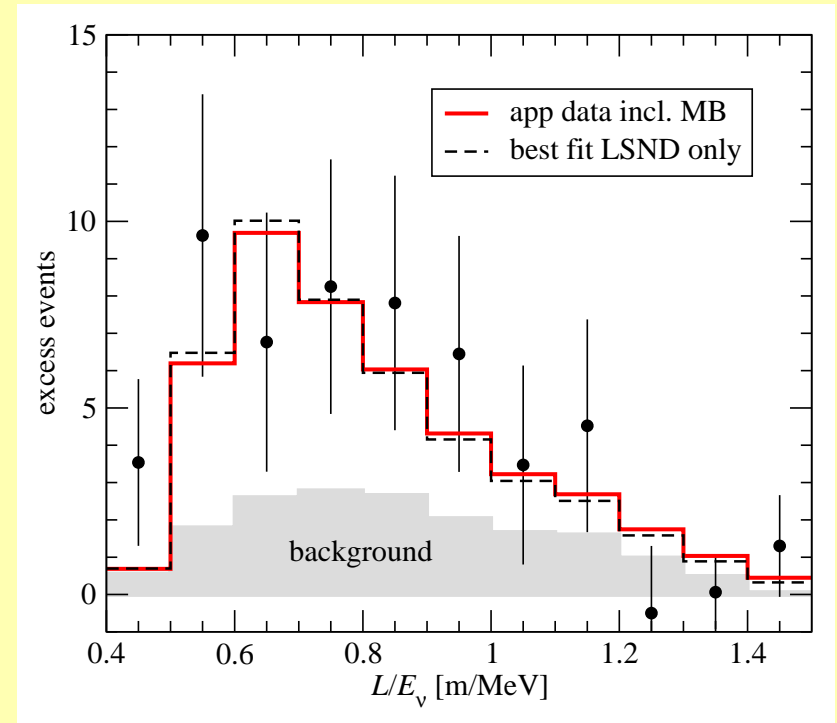
# *(3+2) appearance data*

best fit point spectra:

## MiniBooNE



## LSND



Perfect fit to appearance data:

w/o MB low energy excess:  $\chi_{\min}^2 = 16.9/(29 - 5)$

with MB low energy excess:  $\chi_{\min}^2 = 18.5/(31 - 5)$

## *(3+2) disappearance data*

---

what about the disappearance data?

$$P_{\nu_\alpha \rightarrow \nu_\alpha} = 1 - 4 \left( 1 - \sum_{i=4,5} |U_{\alpha i}|^2 \right) \sum_{i=4,5} |U_{\alpha i}|^2 \sin^2 \phi_{i1} - 4 |U_{\alpha 4}|^2 |U_{\alpha 5}|^2 \sin^2 \phi_{54}$$

$\Rightarrow$  bound  $|U_{ei}|$  and  $|U_{\mu i}|$  ( $i = 4, 5$ ), similar as in (3+1)

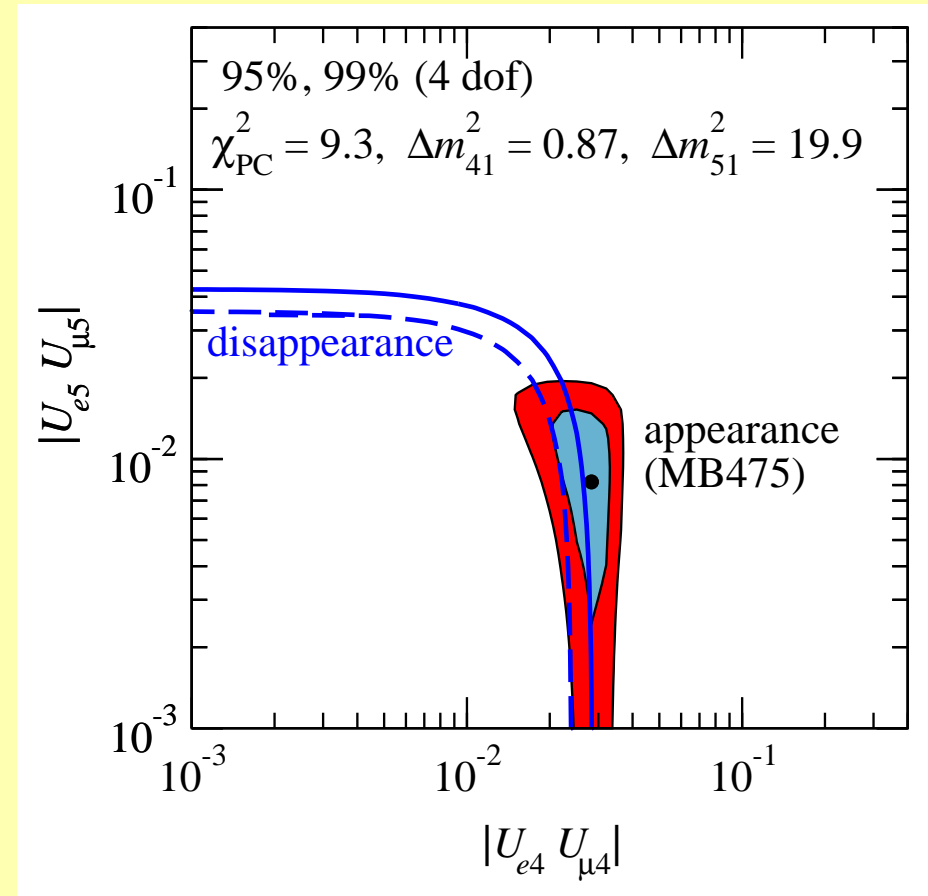
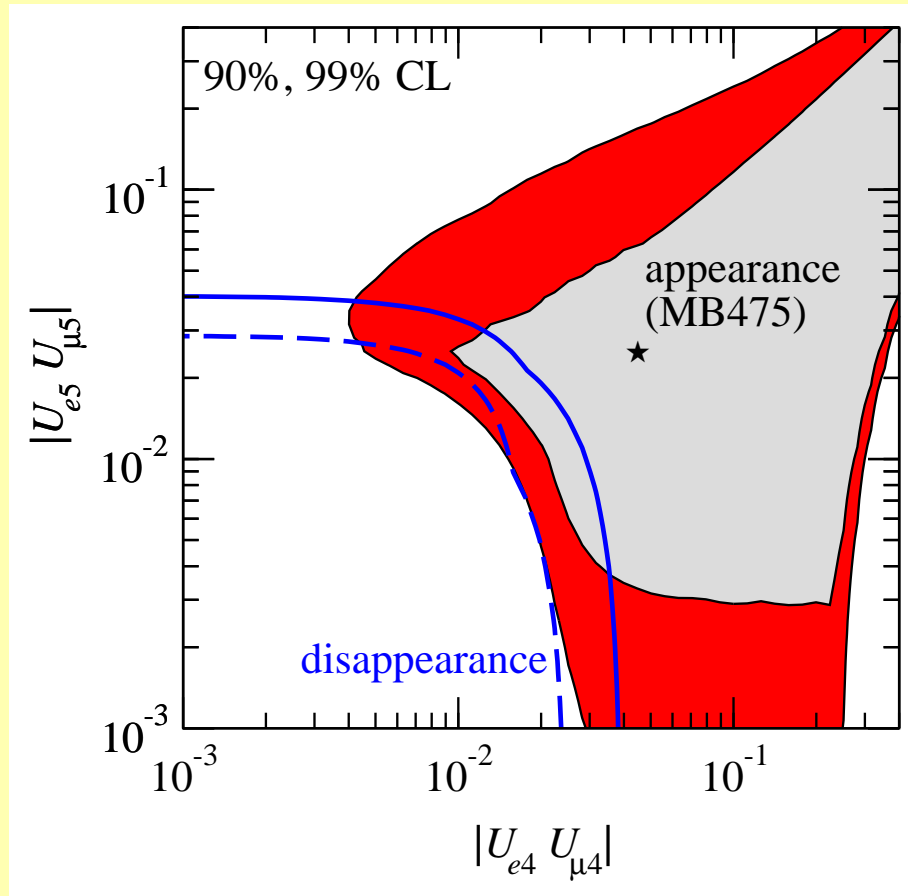
to be reconciled with appearance amplitudes  $|U_{ei}U_{\mu i}|$



# *(3+2) app vs disap*

projection

section



## *(3+2) global*

---

testing consistency of disappearance and appearance data:

$$\chi_{\text{PG}}^2 = 17.2 \text{ (4 dof)} \quad \text{PG} = 0.18\%$$

(without MB:  $\chi_{\text{PG}}^2 = 17.5$ )

**inconsistency at about  $3.1\sigma$**

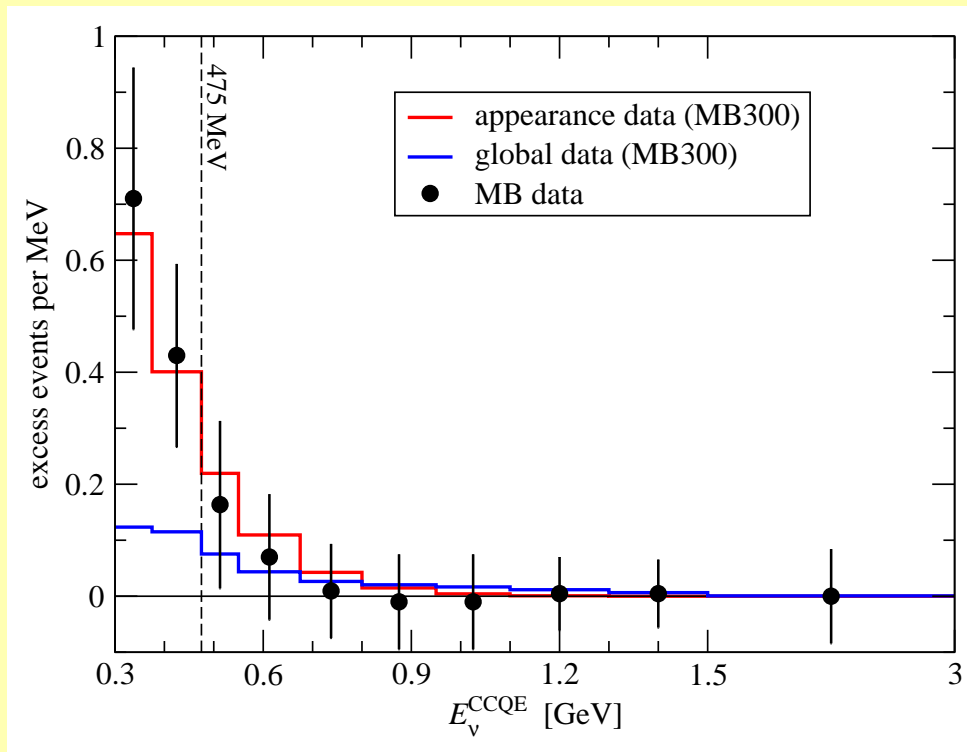
parameters in common  $|U_{e4}U_{\mu4}|, |U_{e5}U_{\mu5}|, \Delta m_{41}^2, \Delta m_{51}^2$

best fit:  $\Delta m_{41}^2 = 0.9 \text{ eV}^2, \Delta m_{51}^2 = 6.5 \text{ eV}^2, \chi_{\text{min}}^2 = 94.5/(107 - 7)$

$$\chi_{\text{min, global (3+1)}}^2 - \chi_{\text{min, global (3+2)}}^2 = 6.1/4 \text{ dof} \quad (81\% \text{ CL})$$

# *the low energy MB excess in the (3+2) fit*

the MB low energy excess is not reproduced at the global best fit point:



$$\chi_{\text{MB300}}^2 = 104.4 / (109 - 7)$$

$$\chi_{\text{MB475}}^2 = 94.5 / (107 - 7)$$

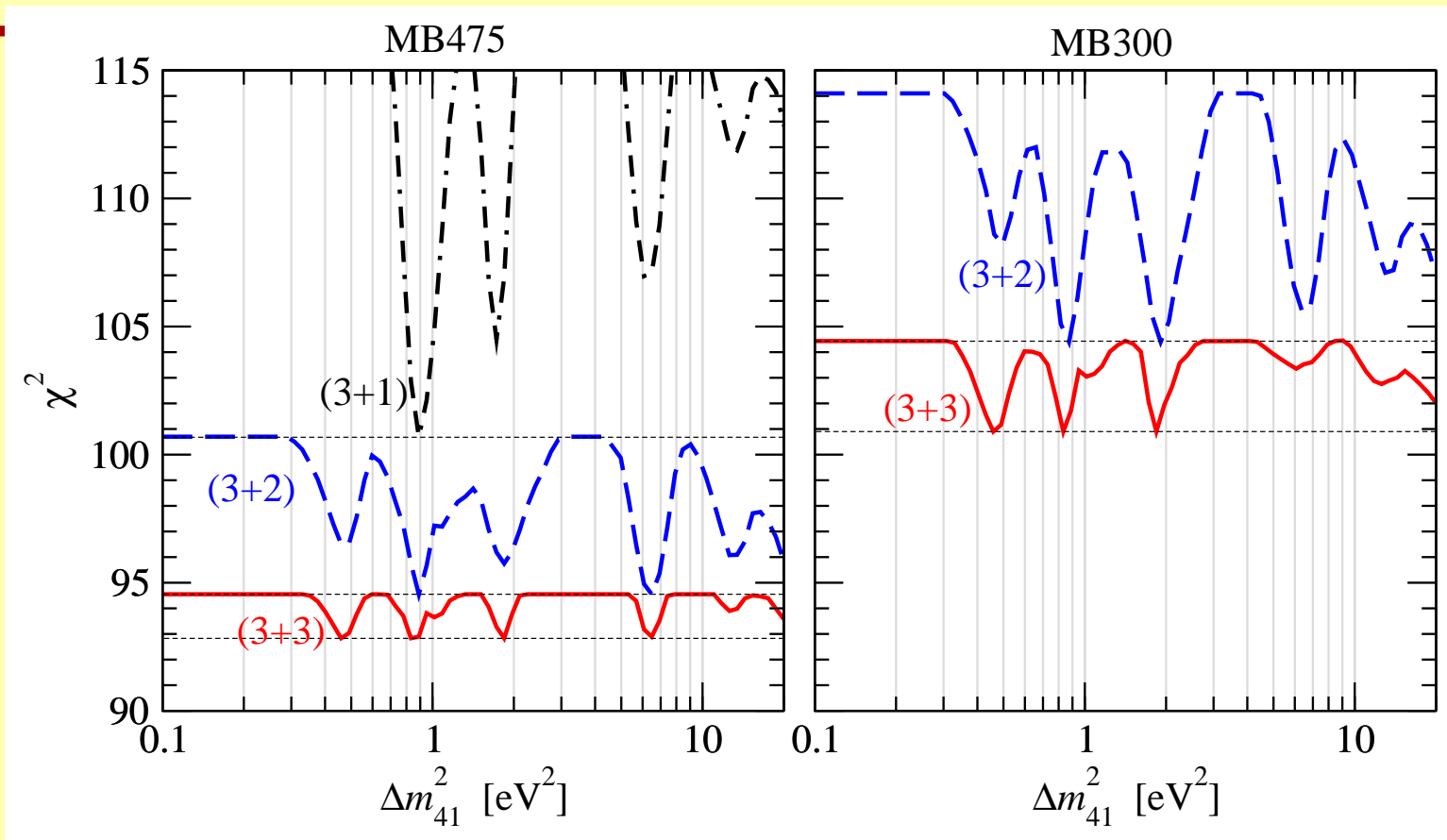
$$\chi_{\text{PG}}^2 = 25.1 / 4$$

$$\text{PG} = 4.8 \times 10^{-5} \quad (4\sigma)$$

---

**adding another sterile: (3+3)**

# *(3+3) global fit*



	$\Delta m_{41}^2$	$\Delta m_{51}^2$	$\Delta m_{61}^2$	$\chi_{\min}^2$	$\chi_{(3+2)}^2 - \chi_{(3+3)}^2$	CL
MB475	0.46	0.83	1.84	92.8	1.7/4	20%
MB300	0.46	0.83	1.84	100.9	3.5/4	52%

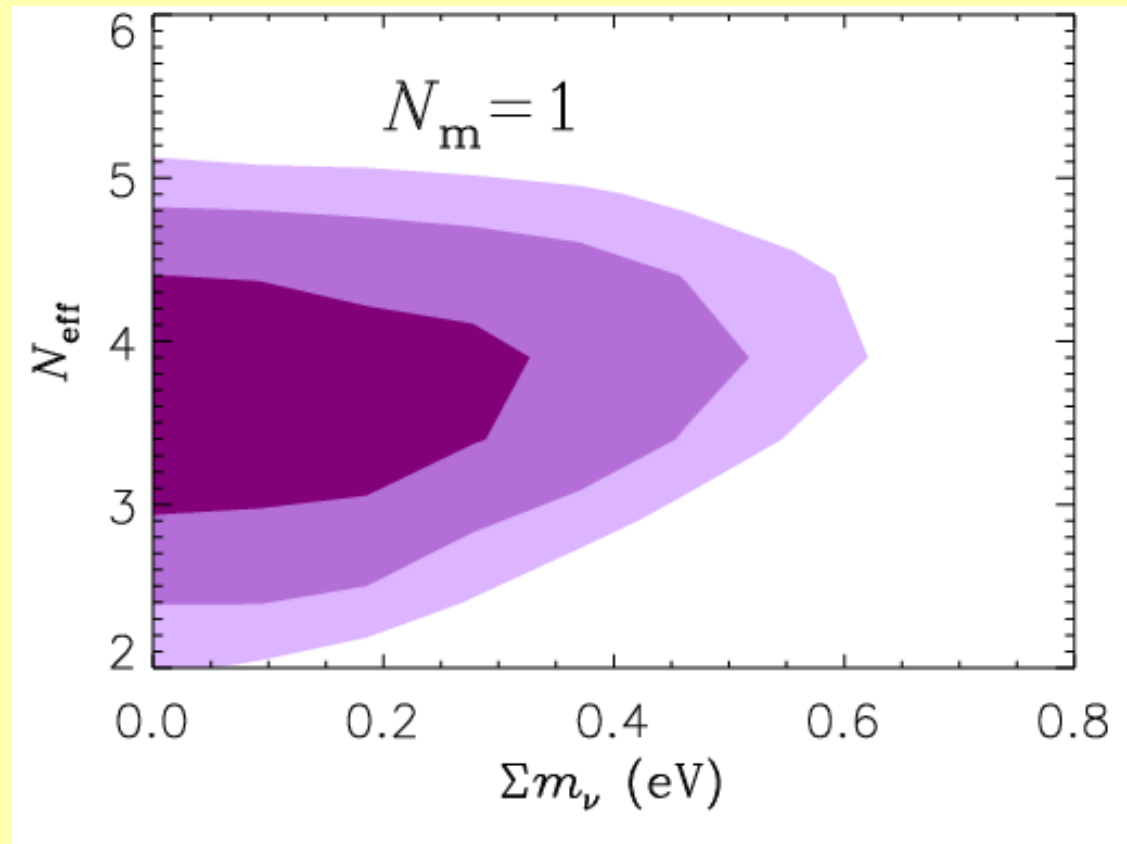
---

## All these sterile neutrino schemes have problems with cosmology

- sterile states contribute to the relativistic degrees of freedom (CMB, BBN)
- conflict with bound on the sum of neutrino masses from various cosmological data sets (LSS)

# Cosmology

SN Ia, LSS (2dF, SDSS), BAO, CMB (WMAP, BOOMERANG)



68%, 95%, 99% CL

Hannestad, Raffelt, astro-ph/0607101

---

## More 'exotic' proposals



- **3-neutrinos and CPT violation** Murayama, Yanagida 01;  
Barenboim, Borissov, Lykken 02; Gonzalez-Garcia, Maltoni, Schwetz 03
- **4-neutrinos and CPT violation** Barger, Marfatia, Whisnant 03
- **Exotic muon-decay** Babu, Pakvasa 02
- **CPT viol. quantum decoherence** Barenboim, Mavromatos 04
- **Lorentz violation**  
Kostelecky, Mews, 04; Gouvea, Grossman, 06; Katori, Kostelecky, Tayloe, 06
- **mass varying neutrinos**  
Kaplan, Nelson, Weiner 04; Zurek 04; Barger, Marfatia, Whisnant 05
- **shortcuts of sterile neutrinos in extra dimensions**  
Paes, Pakvasa, Weiler 05
- **1 decaying sterile neutrino** Palomares-Riuz, Pascoli, Schwetz 05
- **2 decaying sterile neutrinos with CPV**
- **sterile neutrinos and new gauge boson** Nelson, Walsh 07
- **sterile neutrino with exotic energy dependence** Schwetz 07
- **quantum decoherence with special energy dependence**  
Farzan, Schwetz, Smirnov, 08

- 3-neutrinos and CPT violation **KamLAND+atmospheric antineutrino data**  
Barenboim, Berezin, Lykken 02; Gonzalez-Garcia, Maltoni, Schwetz 03
- 4-neutrinos and CPT violation Barger, Marfatia, Whisnant 03
- Exotic muon-decay Babu, Pakvasa 02
- CPT viol. quantum decoherence Barenboim, Mavromatos 04
- Lorentz violation  
Kostelecky, Mews, 04; Gouvea, Grossman, 06; Katori, Kostelecky, Tayloe, 06
- mass varying neutrinos  
Kaplan, Nelson, Weiner 04; Zurek 04; Barger, Marfatia, Whisnant 05
- shortcuts of sterile neutrinos in extra dimensions  
Paes, Pakvasa, Weiler 05
- 1 decaying sterile neutrino Palomares-Riuz, Pascoli, Schwetz 05
- 2 decaying sterile neutrinos with CPV
- sterile neutrinos and new gauge boson Nelson, Walsh 07
- sterile neutrino with exotic energy dependence Schwetz 07
- quantum decoherence with special energy dependence  
Farzan, Schwetz, Smirnov, 08

- 3-neutrinos and CPT violation **KamLAND+atmospheric antineutrino data**  
Barenboim, Borner, Lykken 02; Gonzalez-Garcia, Maltoni, Schwetz 03
- 4-neutrinos and CPT violation Barger, Marfatia, Whisnant 03
- Exotic muon-decay **KARMEN, TWIST**
- CPT viol. quantum decoherence Barenboim, Mavromatos 04
- Lorentz violation  
Kostelecky, Mews, 04; Gouvea, Grossman, 06; Katori, Kostelecky, Tayloe, 06
- mass varying neutrinos  
Kaplan, Nelson, Weiner 04; Zurek 04; Barger, Marfatia, Whisnant 05
- shortcuts of sterile neutrinos in extra dimensions  
Paes, Pakvasa, Weiler 05
- 1 decaying sterile neutrino Palomares-Riuz, Pascoli, Schwetz 05
- 2 decaying sterile neutrinos with CPV
- sterile neutrinos and new gauge boson Nelson, Walsh 07
- sterile neutrino with exotic energy dependence Schwetz 07
- quantum decoherence with special energy dependence  
Farzan, Schwetz, Smirnov, 08

- 3-neutrinos and CPT violation **KamLAND+atmospheric antineutrino data**  
Barenboim, Borjan, Lykken 02; Gonzalez-Garcia, Maltoni, Schwetz 03
- 4-neutrinos and CPT violation Barger, Marfatia, Whisnant 03
- Exotic muon-decay **KARMEN, TWIST**
- CPT viol. quant **KamL spectrum, NuTeV**  
Barenboim, Mavromatos 04
- Lorentz violation  
Kostelecky, Mews, 04; Gouvea, Grossman, 06; Katori, Kostelecky, Tayloe, 06
- mass varying neutrinos  
Kaplan, Nelson, Weiner 04; Zurek 04; Barger, Marfatia, Whisnant 05
- shortcuts of sterile neutrinos in extra dimensions  
Paes, Pakvasa, Weiler 05
- 1 decaying sterile neutrino Palomares-Riuz, Pascoli, Schwetz 05
- 2 decaying sterile neutrinos with CPV
- sterile neutrinos and new gauge boson Nelson, Walsh 07
- sterile neutrino with exotic energy dependence Schwetz 07
- quantum decoherence with special energy dependence  
Farzan, Schwetz, Smirnov, 08

- 3-neutrinos and CPT violation **KamLAND+atmospheric antineutrino data**  
Barenboim, Borner, Lykken 02; Gonzalez-Garcia, Maltoni, Schwetz 03
- 4-neutrinos and CPT violation Barger, Marfatia, Whisnant 03
- Exotic muon-decay **KARMEN, TWIST**
- CPT viol. quant. **KamL spectrum, NuTeV**  
Barenboim, Mavromatos 04
- Lorentz violation **energy dependence, MiniBooNE?**  
Kostelecky, Lykken, Crossman, 06; Katori, Kostelecky, Tayloe, 06
- mass varying neutrinos  
Kaplan, Nelson, Weiner 04; Zurek 04; Barger, Marfatia, Whisnant 05
- shortcuts of sterile neutrinos in extra dimensions  
Paes, Pakvasa, Weiler 05
- 1 decaying sterile neutrino Palomares-Riuz, Pascoli, Schwetz 05
- 2 decaying sterile neutrinos with CPV
- sterile neutrinos and new gauge boson Nelson, Walsh 07
- sterile neutrino with exotic energy dependence Schwetz 07
- quantum decoherence with special energy dependence  
Farzan, Schwetz, Smirnov, 08

- 3-neutrinos and CPT violation **KamLAND+atmospheric antineutrino data**  
Barenboim, Borjan, Lykken 02; Gonzalez-Garcia, Maltoni, Schwetz 03
- 4-neutrinos and CPT violation Barger, Marfatia, Whisnant 03
- Exotic muon-decay **KARMEN, TWIST**
- CPT viol. quant. **KamL spectrum, NuTeV**  
Barenboim, Mavromatos 04
- Lorentz violation **energy dependence, MiniBooNE?**  
Kostelecky, Crossman, 06; Katori, Kostelecky, Tayloe, 06
- mass varying neutrinos **CDHS+atmospheric data?**  
Kaplan, Nelson, Weiler, Barger, Marfatia, Whisnant 05
- shortcuts of sterile neutrinos in extra dimensions  
Paes, Pakvasa, Weiler 05
- 1 decaying sterile neutrino Palomares-Riuz, Pascoli, Schwetz 05
- 2 decaying sterile neutrinos with CPV
- sterile neutrinos and new gauge boson Nelson, Walsh 07
- sterile neutrino with exotic energy dependence Schwetz 07
- quantum decoherence with special energy dependence  
Farzan, Schwetz, Smirnov, 08

- 3-neutrinos and CPT violation **KamLAND+atmospheric antineutrino data**  
Barenboim, Barger, Marfatia, Whisnant 01; Gonzalez-Garcia, Maltoni, Schwetz 03
- 4-neutrinos and CPT violation Barger, Marfatia, Whisnant 03
- Exotic muon-decay **KARMEN, TWIST**
- CPT viol. quant. **KamL spectrum, NuTeV**  
Barenboim, Mavromatos 04
- Lorentz violation **energy dependence, MiniBooNE?**  
Kostelecky, Crossman, 06; Katori, Kostelecky, Tayloe, 06
- mass varying neutrinos **CDHS+atmospheric data?**  
Kaplan, Nelson, Whisnant, Barger, Marfatia, Whisnant 05
- shortcuts of sterile neutrino **MiniB+KamL+atmospheric?** dimensions
- 1 decaying sterile neutrino Palomares-Riuz, Pascoli, Schwetz 05
- 2 decaying sterile neutrinos with CPV
- sterile neutrinos and new gauge boson Nelson, Walsh 07
- sterile neutrino with exotic energy dependence Schwetz 07
- quantum decoherence with special energy dependence  
Farzan, Schwetz, Smirnov, 08

- 3-neutrinos and CPT violation **KamLAND+atmospheric antineutrino data**  
Barenboim, Borjan, Lykken 02; Gonzalez-Garcia, Maltoni, Schwetz 03
- 4-neutrinos and CPT violation Barger, Marfatia, Whisnant 03
- Exotic muon-decay **KARMEN, TWIST**
- CPT viol. quant **KamL spectrum, NuTeV**  
Barenboim, Mavromatos 04
- Lorentz violation **energy dependence, MiniBooNE?**  
Kostelecky, Crossman, 06; Katori, Kostelecky, Tayloe, 06
- mass varying neutrinos **CDHS+atmospheric data?**  
Kaplan, Nelson, Wei, Barger, Marfatia, Whisnant 05
- shortcuts of sterile neutrinos **MiniB+KamL+atmospheric? dimensions**  
Paes, Pakvasa, Wei
- 1 decaying sterile neutrino **MiniBooNE**  
Mores-Riuz, Pascoli, Schwetz 05
- 2 decaying sterile neutrinos with CPV
- sterile neutrinos and new gauge boson Nelson, Walsh 07
- sterile neutrino with exotic energy dependence Schwetz 07
- quantum decoherence with special energy dependence  
Farzan, Schwetz, Smirnov, 08



- 3-neutrinos and CPT violation **KamLAND+atmospheric antineutrino data**  
Barenboim, B... Lykken 02; Gonzalez-Garcia, Maltoni, Schwetz 03
- 4-neutrinos and CPT violation Barger, Marfatia, Whisnant 03
- Exotic muon-decay **KARMEN, TWIST**
- CPT viol. quant **KamL spectrum, NuTeV**  
Barenboim, Mavromatos 04
- Lorentz violation **energy dependence, MiniBooNE?**  
Kostelecky, ... Crossman, 06; Katori, Kostelecky, Tayloe, 06
- mass varying neutrinos **CDHS+atmospheric data?**  
Kaplan, Nelson, Wei ... Barger, Marfatia, Whisnant 05
- shortcuts of sterile neutrinos **MiniB+KamL+atmospheric?** dimensions  
Paes, Pakvasa, Wei ...
- 1 decaying sterile neutrino **MiniBooNE** ... Mares-Riuz, Pascoli, Schwetz 05
- 2 decaying sterile neutrinos with CPV
- sterile neutrinos **MINOS+atmospheric?** ... Nelson, Walsh 07
- sterile neutrino with exotic energy dependence Schwetz 07
- quantum decoherence with special energy dependence  
Farzan, Schwetz, Smirnov, 08

# *Sterile neutrino oscillations - outlook*

---

- CPV is being tested by MiniBooNE anti-neutrino data (problem of statistics?)
- MB low- $E$  excess is a real puzzle for pheno

# *Sterile neutrino oscillations - outlook*

---

- CPV is being tested by MiniBooNE anti-neutrino data (problem of statistics?)
- MB low- $E$  excess is a real puzzle for pheno
- the problem of  $(3+s)$  schemes heavily relies on SBL disappearance experiments  
Bugey ( $\bar{\nu}_e$  reactor) and CDHS ( $\nu_\mu$  accelerator)
- could be worth to look for disappearance at the  $\Delta m^2 \sim 1 \text{ eV}^2$  scale at future reactor or LBL experiments (near detectors)

# *Sterile neutrino oscillations - outlook*

---

- CPV is being tested by MiniBooNE anti-neutrino data (problem of statistics?)
- MB low- $E$  excess is a real puzzle for pheno
- the problem of  $(3+s)$  schemes heavily relies on SBL disappearance experiments  
Bugey ( $\bar{\nu}_e$  reactor) and CDHS ( $\nu_\mu$  accelerator)
- could be worth to look for disappearance at the  $\Delta m^2 \sim 1 \text{ eV}^2$  scale at future reactor or LBL experiments (near detectors)
- sterile neutrinos with  $\Delta m^2 \sim 1 \text{ eV}^2$  might lead to large effects for high energy atmospheric neutrinos in IceCube S. Choubey, 0709.1937