
Neutrino oscillations:

Present status and outlook

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Outline

- Introduction
- Global fit to present oscillation data
impact of 2007 new data
- LSND puzzle in the light of MiniBooNE results
- Future oscillation experiments
prospects for measuring θ_{13}
CP violation, determination of the mass hierarchy

I will not speak about...

Measurements of absolute neutrino masses

- Tritium beta-decay
- neutrinoless double beta-decay
- neutrino mass determination from cosmology

... but focus on neutrino oscillations

Neutrino mixing

$$\mathcal{L}_{\text{CC}} = -\frac{g}{\sqrt{2}} W^\rho \sum_{\alpha=e,\mu,\tau} \bar{\nu}_{\alpha L} \gamma_\rho \ell_{\alpha L} + \text{h.c.}$$

$$\mathcal{L}_{\text{M}} = -\frac{1}{2} \sum_i \nu_{iL}^T C^{-1} \nu_{iL} m_i + \text{h.c.}$$

with $\nu_{\alpha L} = \sum_i U_{\alpha i} \nu_{iL}, \quad (\alpha = e, \mu, \tau)$

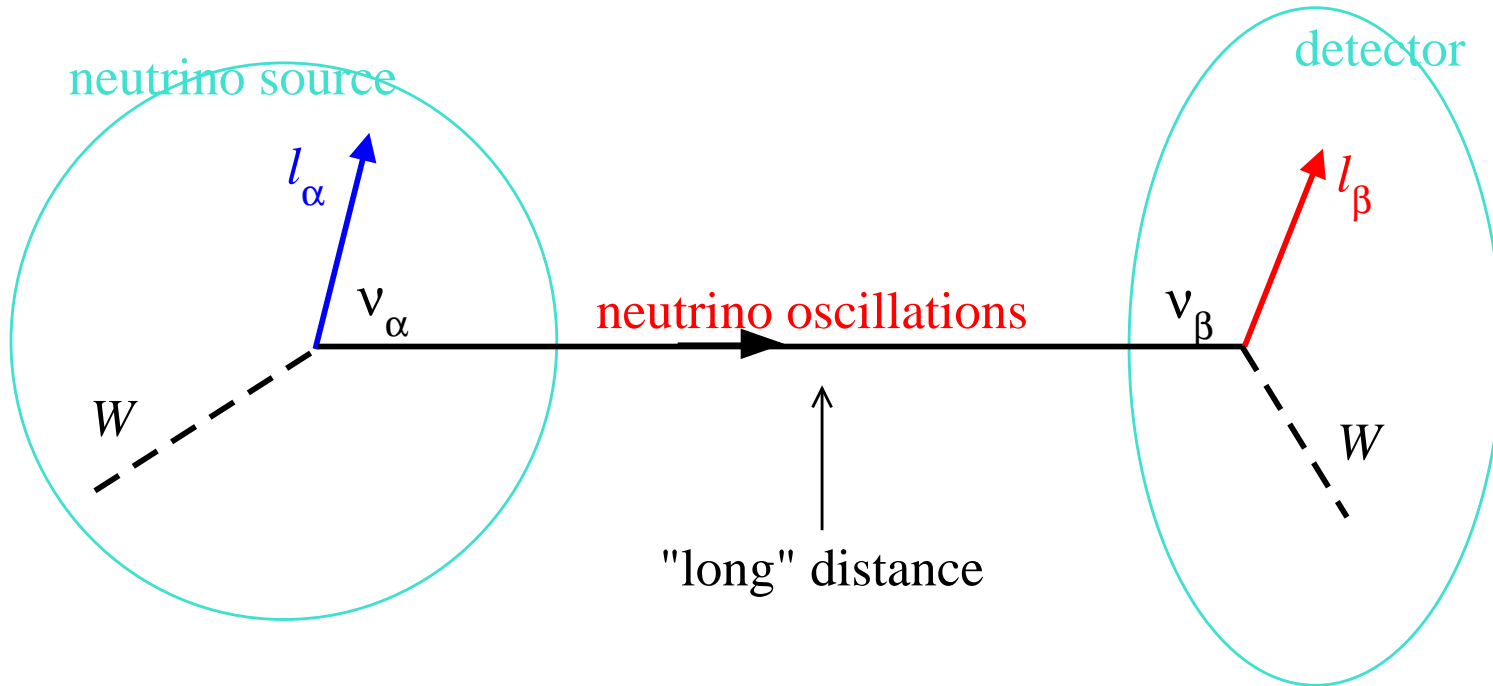
$\nu_{\alpha L}$: neutrinos with CC interaction (“flavour neutrinos”)

ν_{iL} : neutrinos with mass m_i

$U_{\alpha i}$: PMNS lepton mixing matrix

in a basis where the charged lepton mass matrix is diagonal

Neutrino oscillations



$$|\nu_\alpha\rangle = U_{\alpha i}^* |\nu_i\rangle$$

$$e^{-i(Et - p_i x)}$$

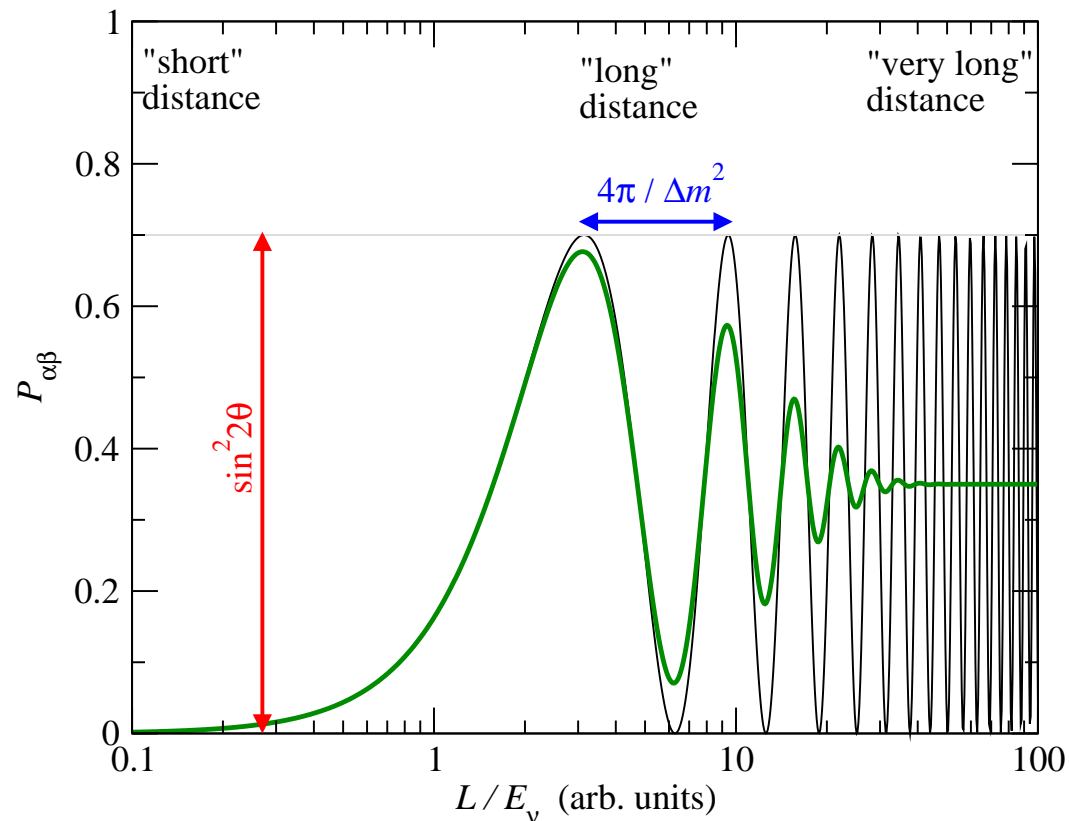
$$|\nu_\beta\rangle = U_{\beta i}^* |\nu_i\rangle$$

osc.prob. (vac):
$$P_{\nu_\alpha \rightarrow \nu_\beta}(L) = \sum_{jk} U_{\alpha j} U_{\beta j}^* U_{\alpha k}^* U_{\beta k} \exp \left[-i \frac{\Delta m_{kj}^2 L}{2 E_\nu} \right]$$

2-neutrino oscillations

Two-flavour limit:

$$U = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}, \quad P = \sin^2 2\theta \sin^2 \frac{\Delta m^2 L}{4E_\nu}$$



Neutrino oscillations in matter

MSW effect (3 flavours):

$$H_{\text{mat}} = \underbrace{U \text{diag} \left(0, \frac{\Delta m_{21}^2}{2E_\nu}, \frac{\Delta m_{31}^2}{2E_\nu} \right) U^\dagger}_{H_{\text{vac}}} \pm \underbrace{\text{diag}(\sqrt{2}G_F N_e, 0, 0)}_{V_{\text{eff}}}$$

$N_e(x)$: electron density along the neutrino path

$$i \frac{d}{dt} \begin{pmatrix} a_e \\ a_\mu \\ a_\tau \end{pmatrix} = H_{\text{mat}}(t) \begin{pmatrix} a_e \\ a_\mu \\ a_\tau \end{pmatrix}$$

Global data and three-neutrino oscillations

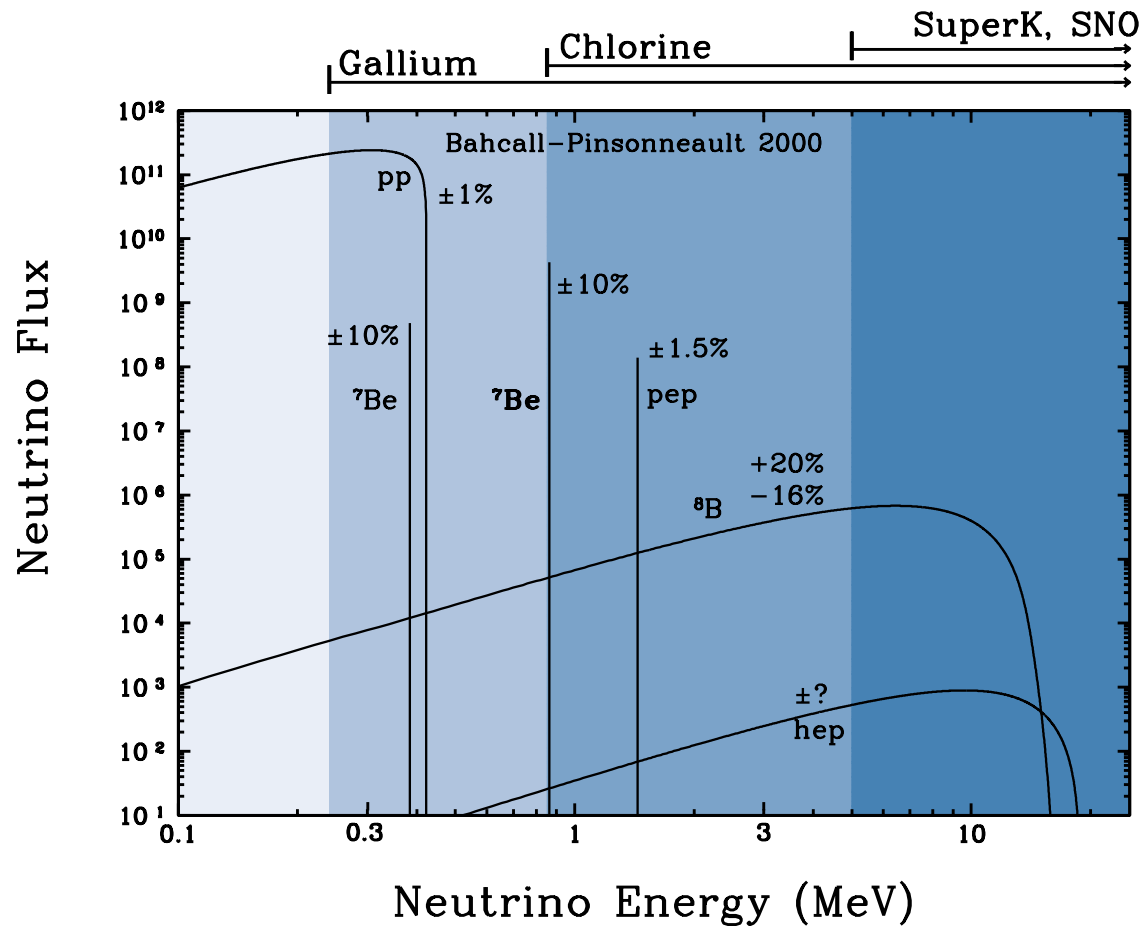
Maltoni, TS, Tortola, Valle, hep-ph/0405172 v6; TS, 0710.5027

Neutrino oscillation experiments

- solar neutrinos
Homestake, SAGE+GNO, Super-Kamiokande, SNO, Borexino
- atmospheric neutrinos
Super-Kamiokande
- reactor neutrinos
Chooz (1 km), KamLAND (180 km)
- long-baseline accelerator experiments
K2K (250 km), MINOS (735 km)

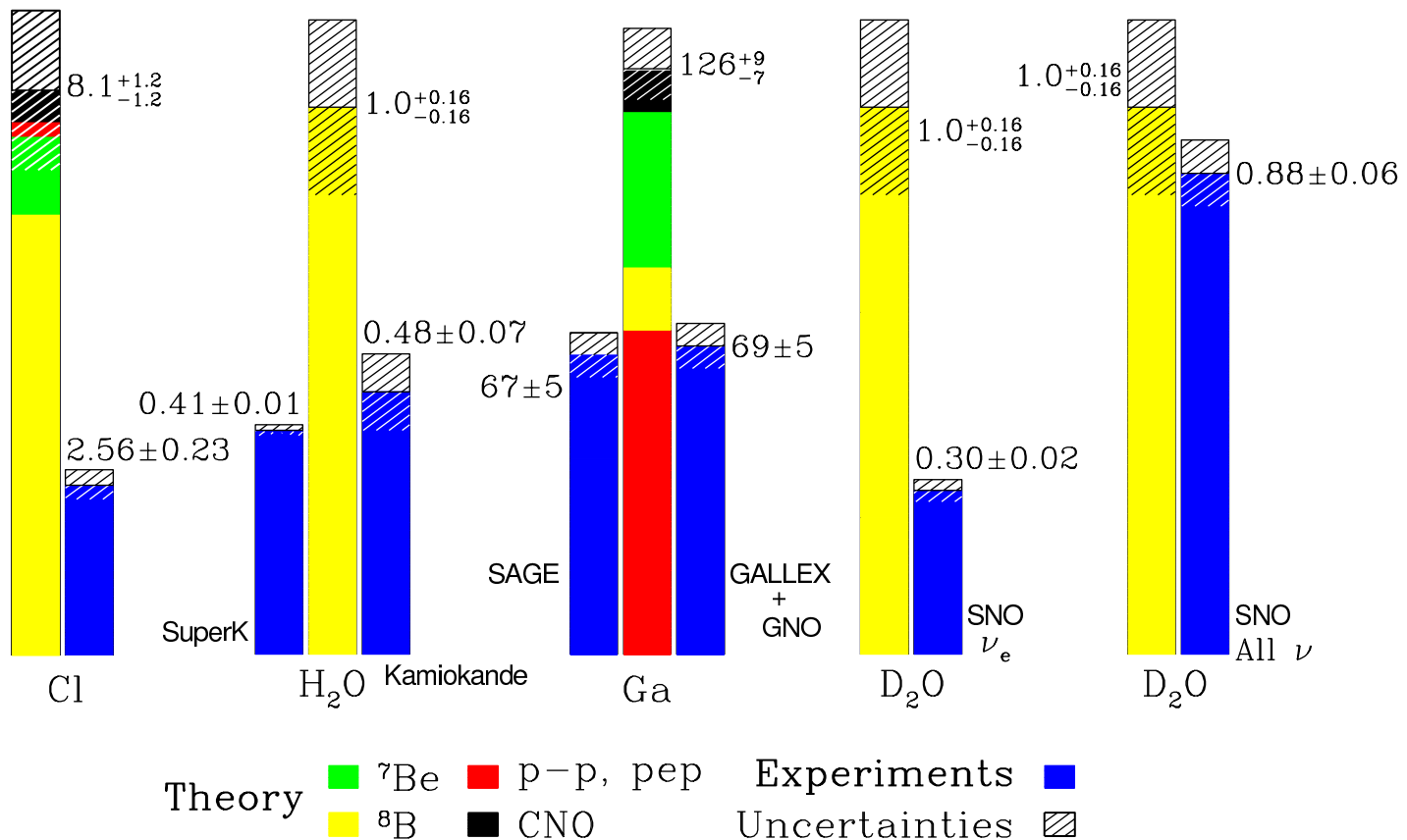
The “solar” parameters $\Delta m_{21}^2, \theta_{12}$

The solar neutrino flux



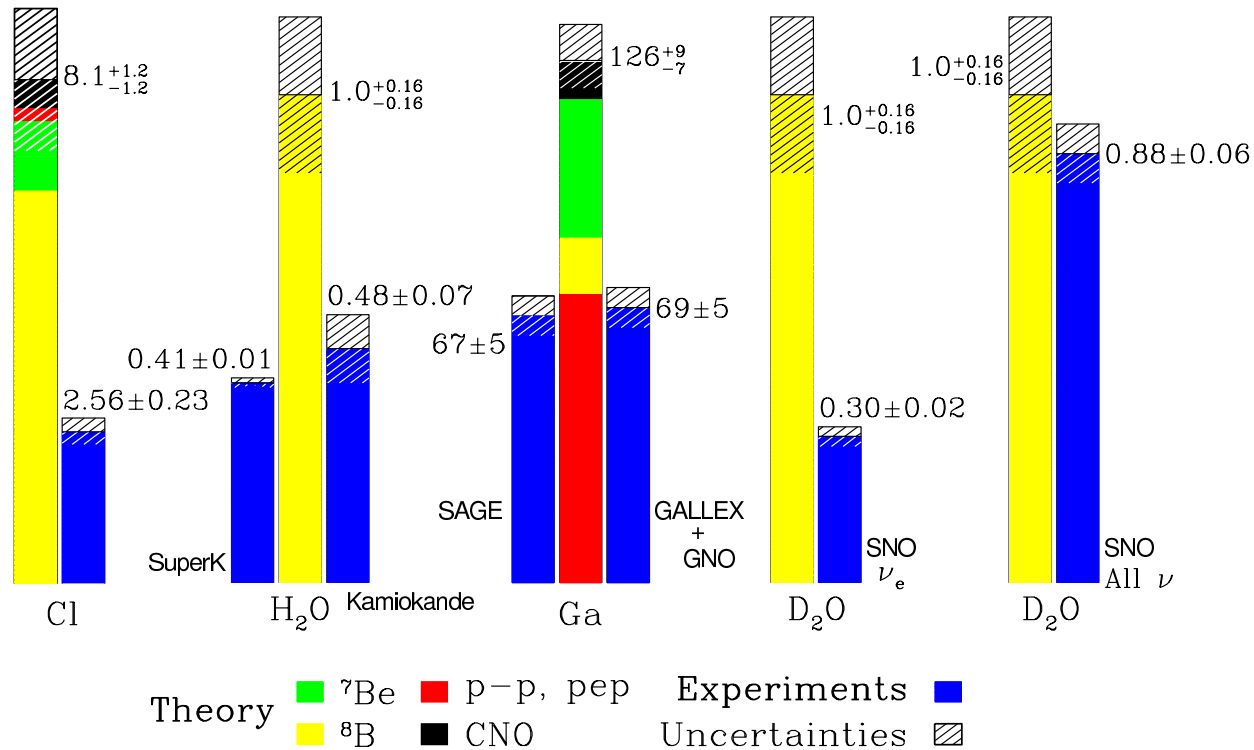
Solar neutrino experiments

Total Rates: Standard Model vs. Experiment
Bahcall–Serenelli 2005 [BS05(OP)]

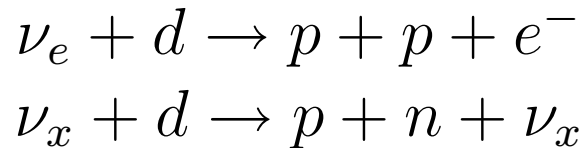


Solar neutrino experiments

Total Rates: Standard Model vs. Experiment
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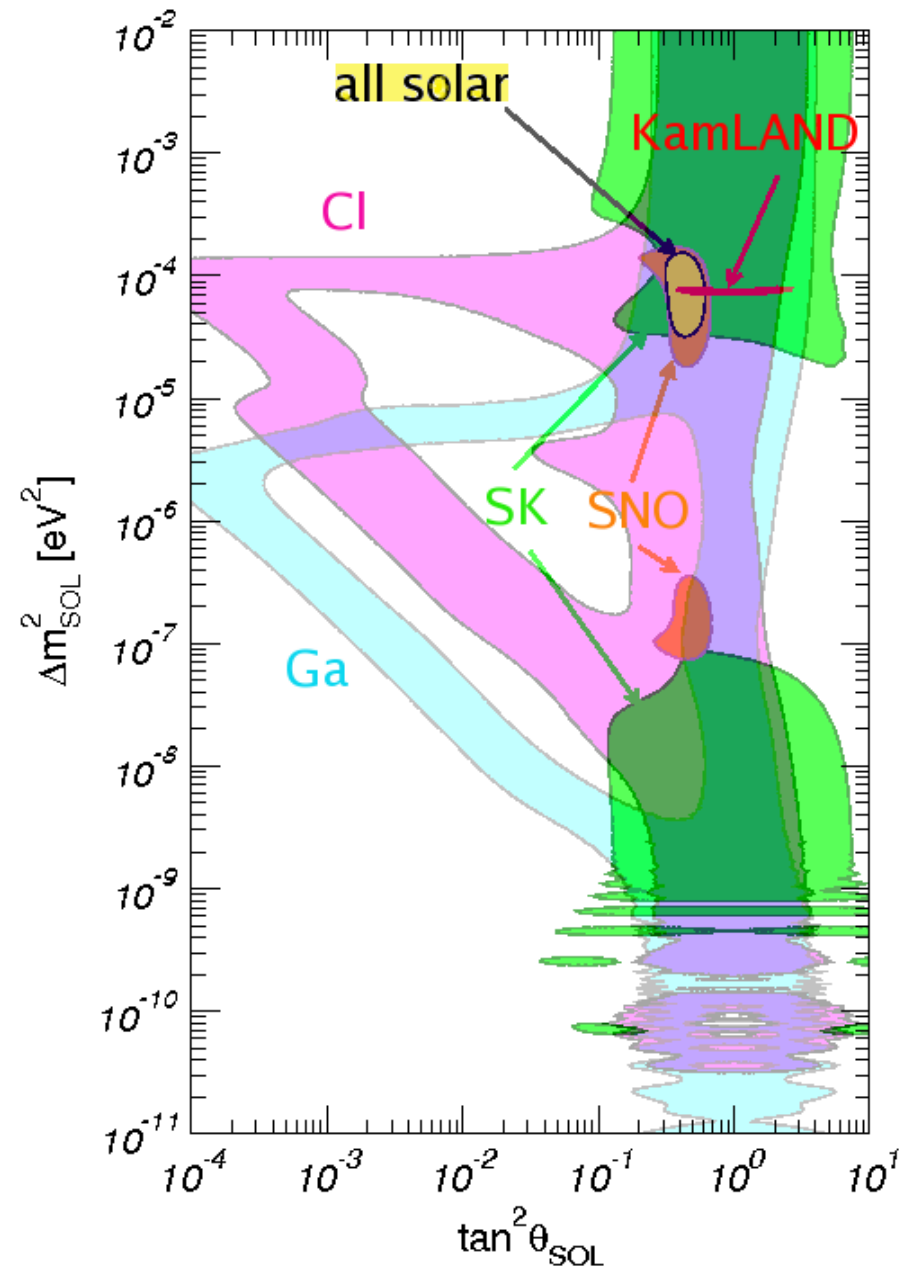
SNO:



$$\frac{\phi_{CC}}{\phi_{NC}} = 0.340 \pm 0.023 \pm 0.030$$

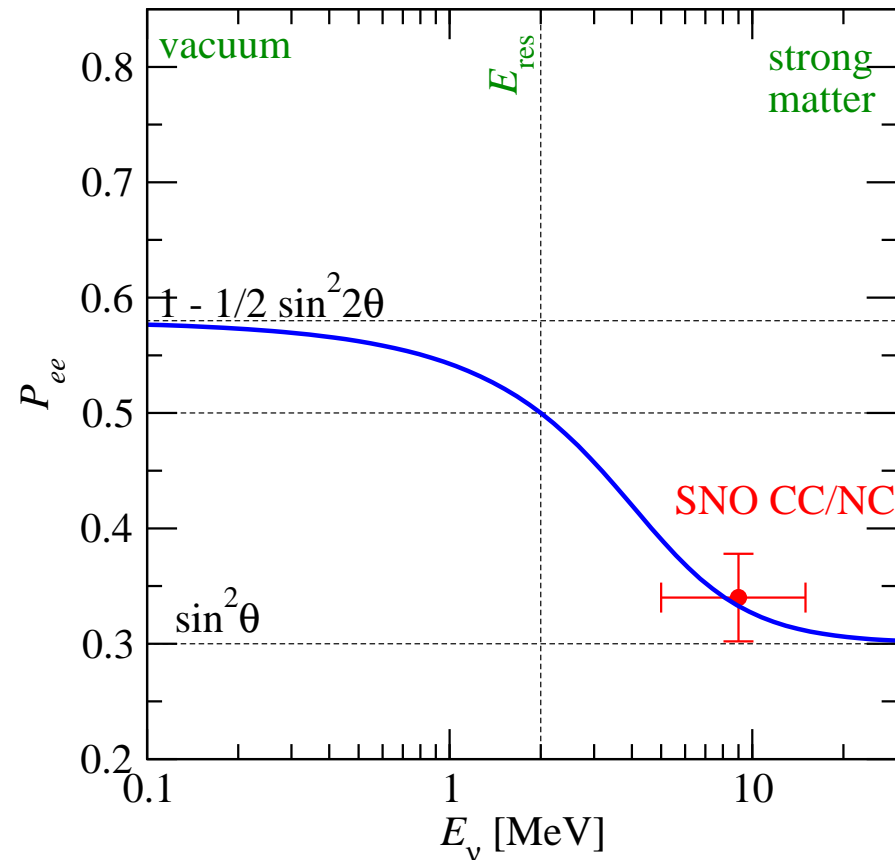
7σ evidence for a non-zero ν_{μ,τ} flux from the sun

'Solar' parameters



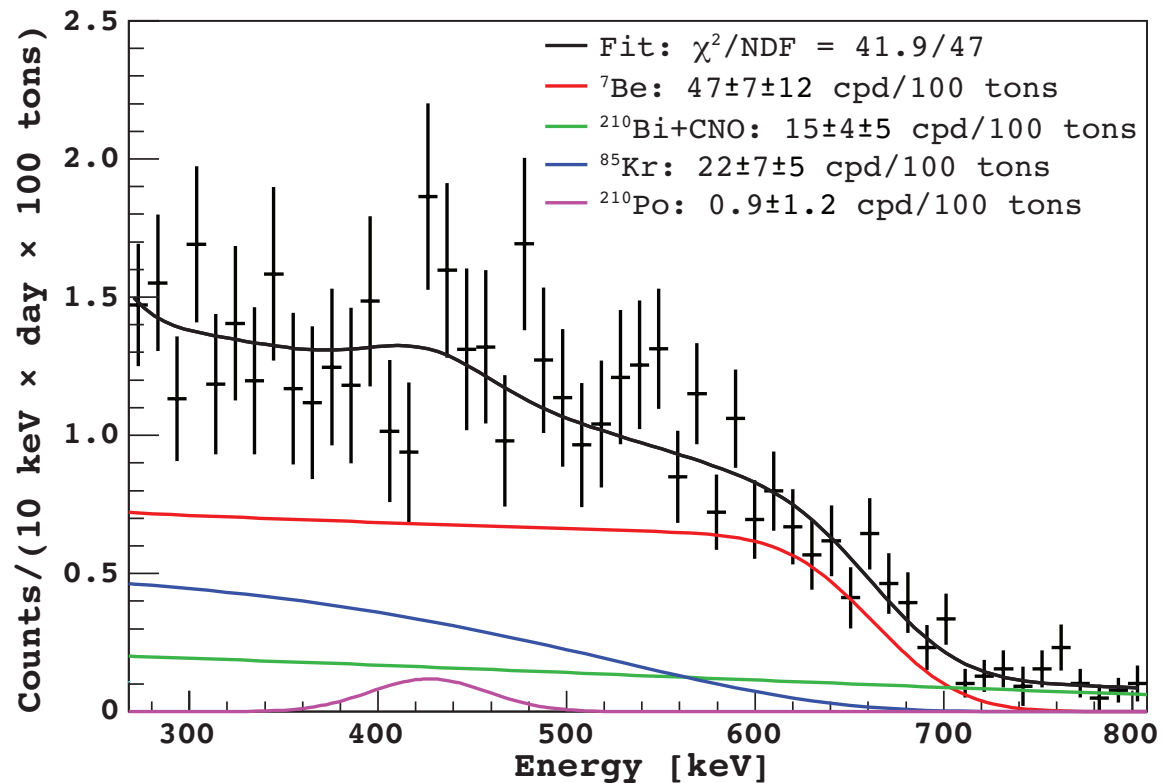
The LMA-MSW solution

adiabatic evolution of the neutrino state from the center of the sun to the surface



First data from Borexino

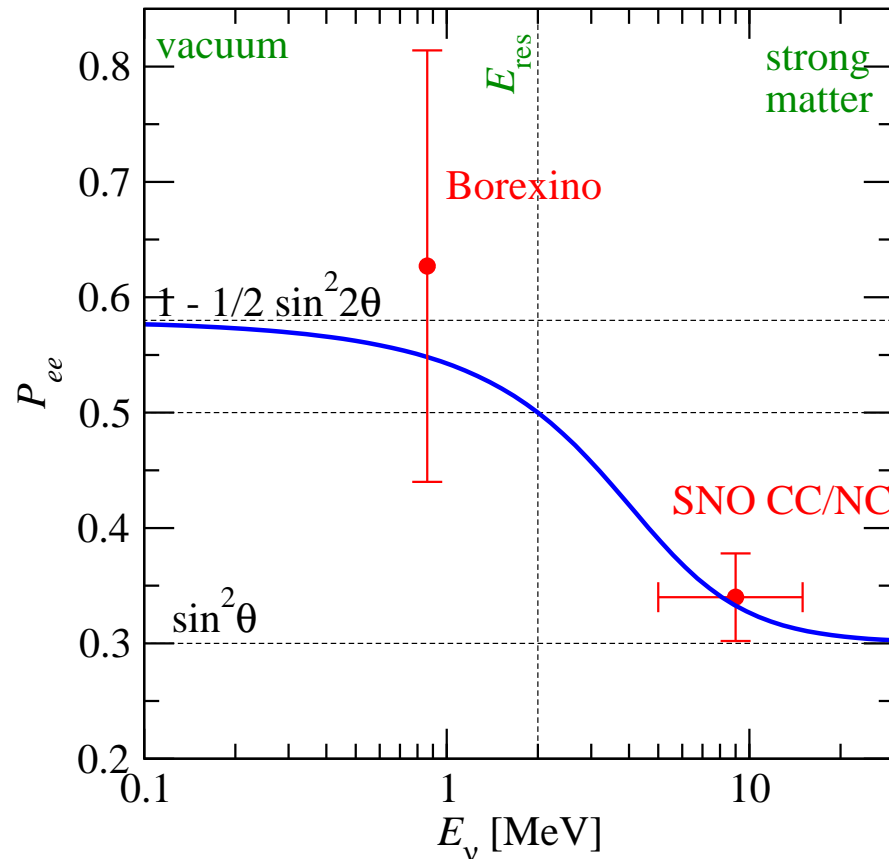
0708.2251 [astro-ph] measurement of the Be7 neutrino line at 0.862 MeV by $e\nu \rightarrow e\nu$ scattering (\Rightarrow)
 $47 \pm 7(\text{stat}) \pm 12(\text{sys}) \text{ ev}/(\text{day} \times 100\text{t})$, without osc.: 75 ± 4



First data from Borexino

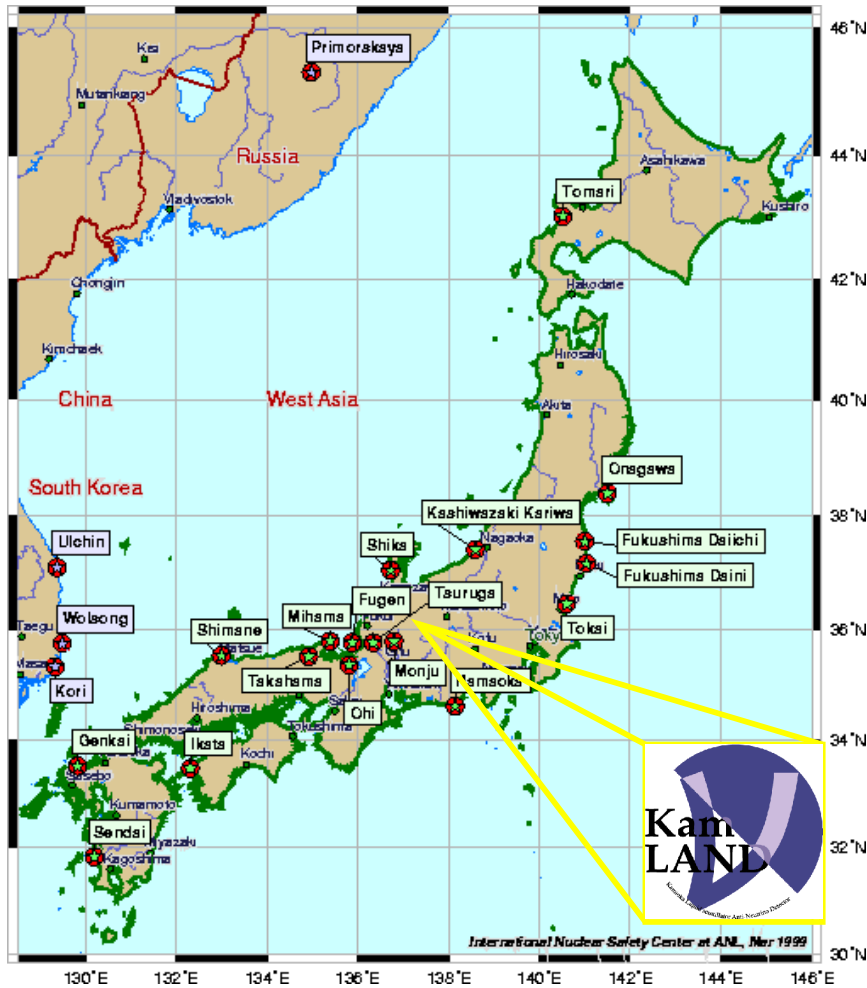
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The KamLAND reactor neutrino experiment

Kamioka Liquid scintillator Anti-Neutrino Detector



detection of $\bar{\nu}_e$ produced in surrounding nuclear power plants

70 GW of nuclear power (7% of world total) is generated at a distance 175 ± 30 km from Kamioka

KamLAND update

New data released this summer:

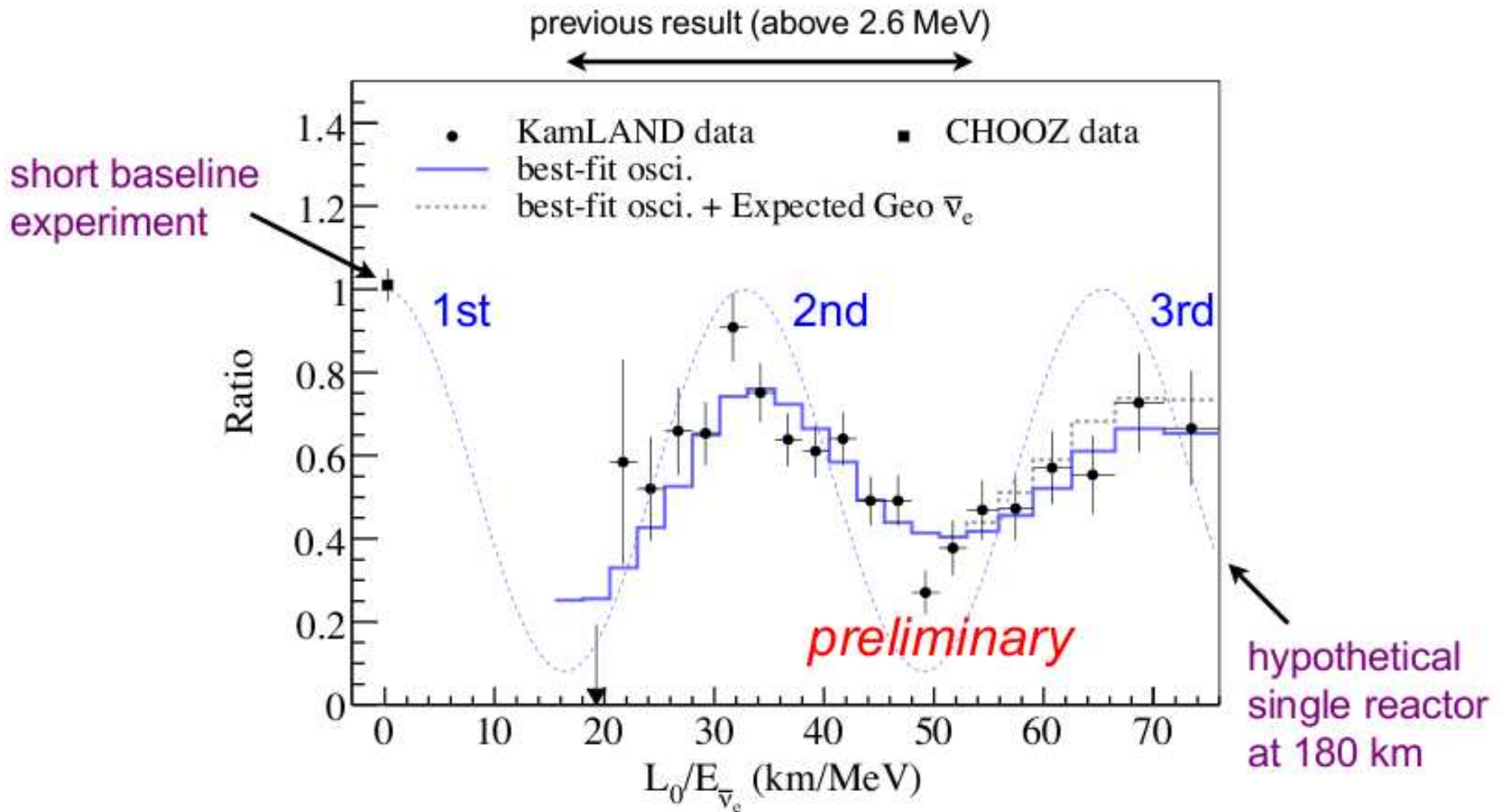
- 2881 ton yr data
4 times more than previous 2004 data
- reduced syst. error due to full volume calibration
from 4.7% to 1.8%
dominating error for Δm^2 determination is now the
uncertainty on the energy scale of 1.5%

observed number of events: 985

expectation without oscillations:

1550 reactor neutrino events + 63 background

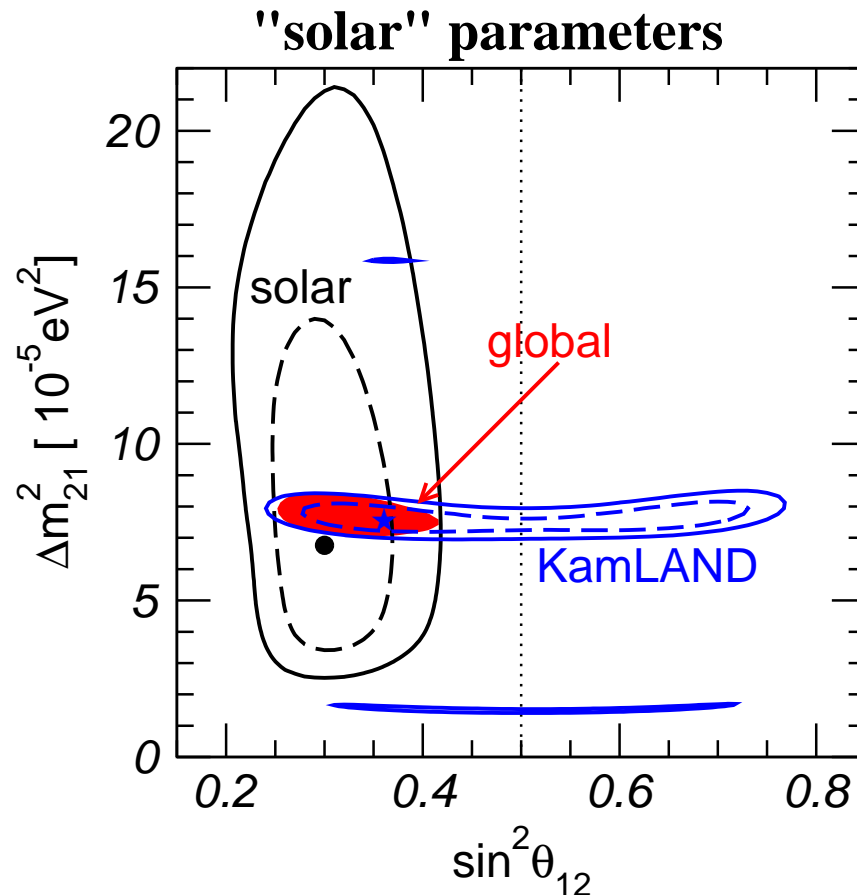
The KamLAND energy spectrum



evidence for oscillations in $1/E_\nu$

KamLAND vs solar data

90% and 99.73% CL contours



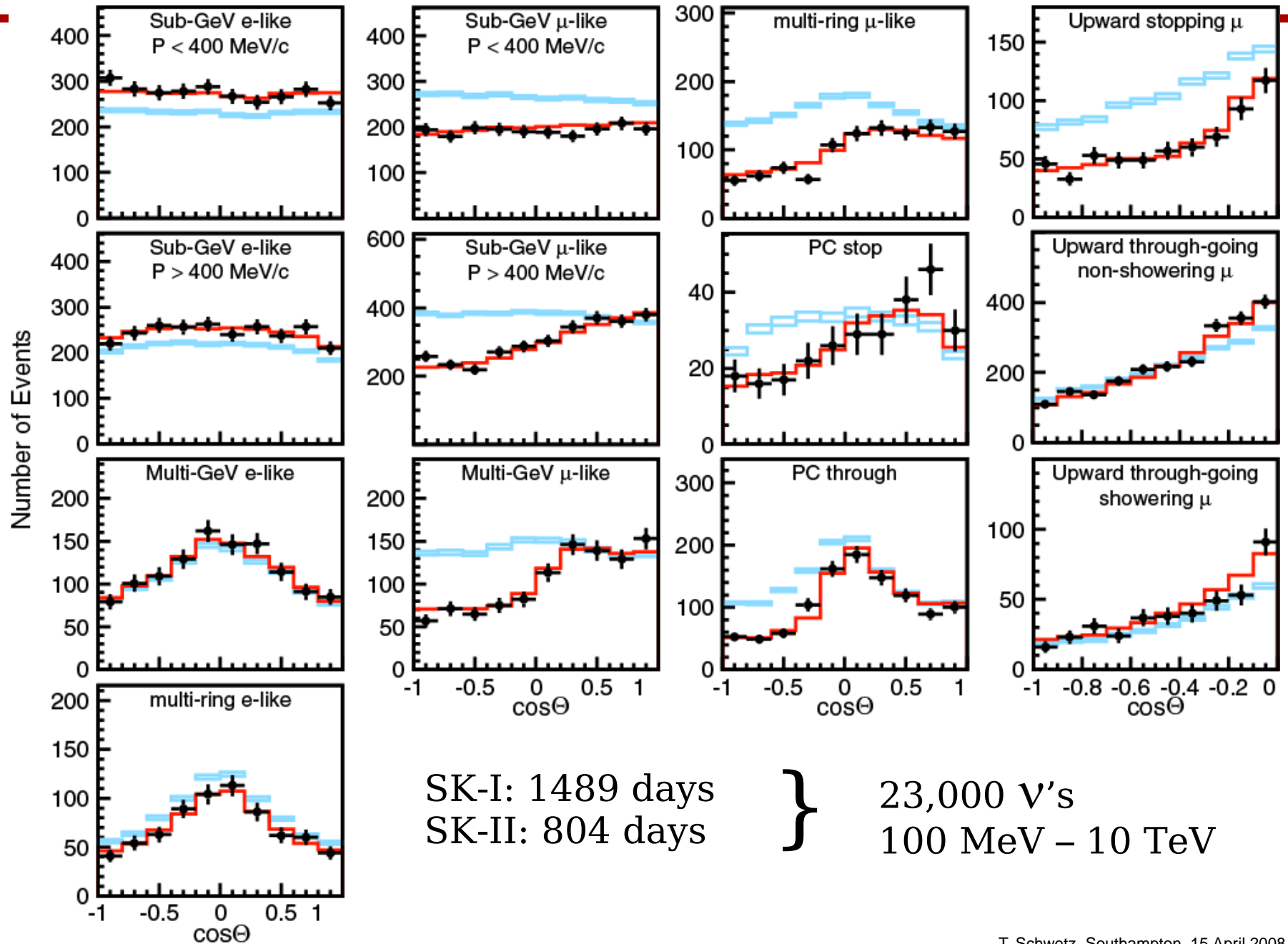
Δm_{21}^2 :
measured by
KamLAND

$\sin^2 \theta_{12}$:
measured by SNO

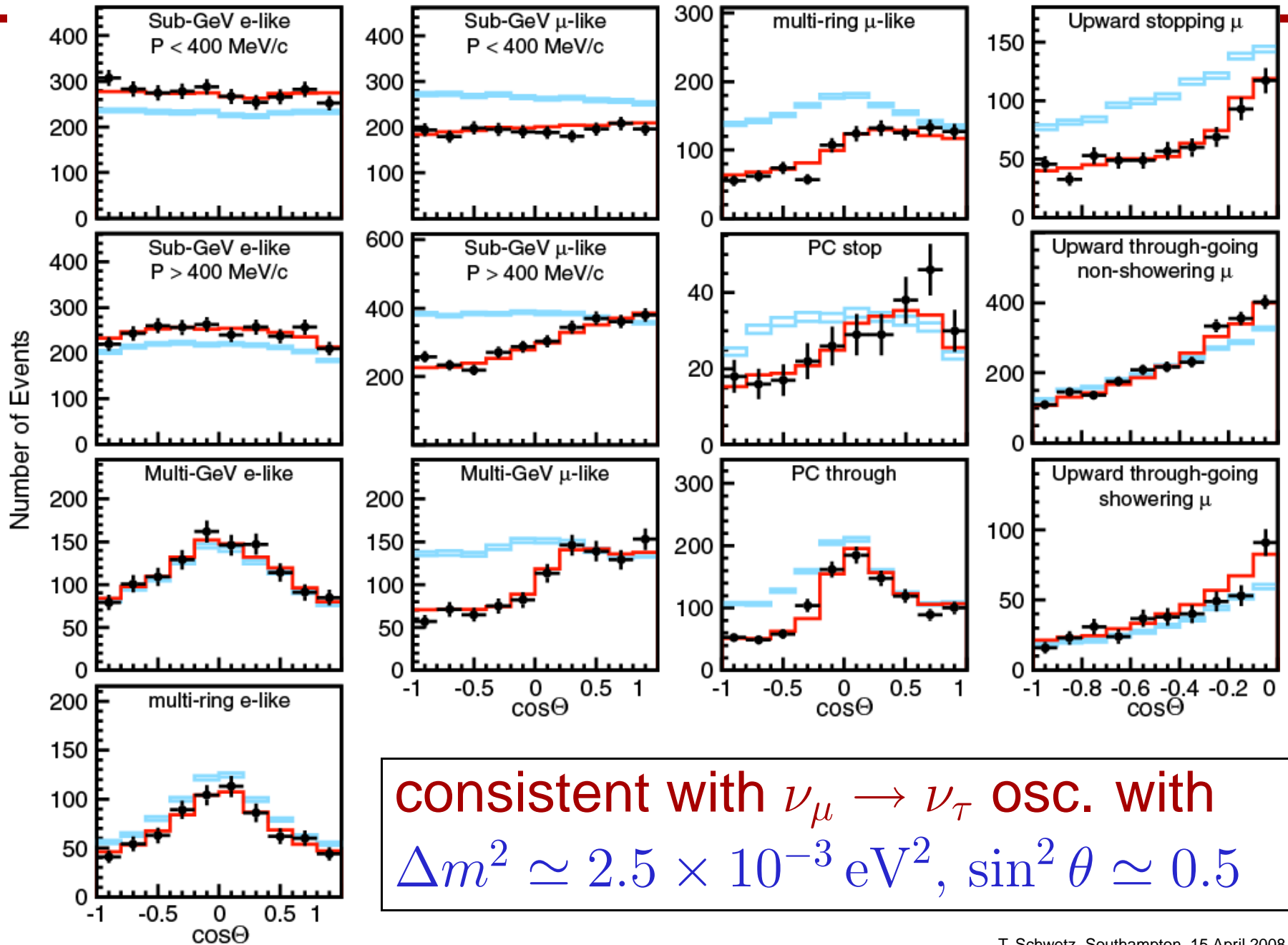
$$\Delta m_{21}^2 = 7.6 \pm 0.20 \times 10^{-5} \text{ eV}^2, \quad \sin^2 \theta_{12} = 0.32 \pm 0.023$$

The “atmospheric” parameters $\Delta m_{31}^2, \theta_{23}$

Super-K atmospheric neutrino data



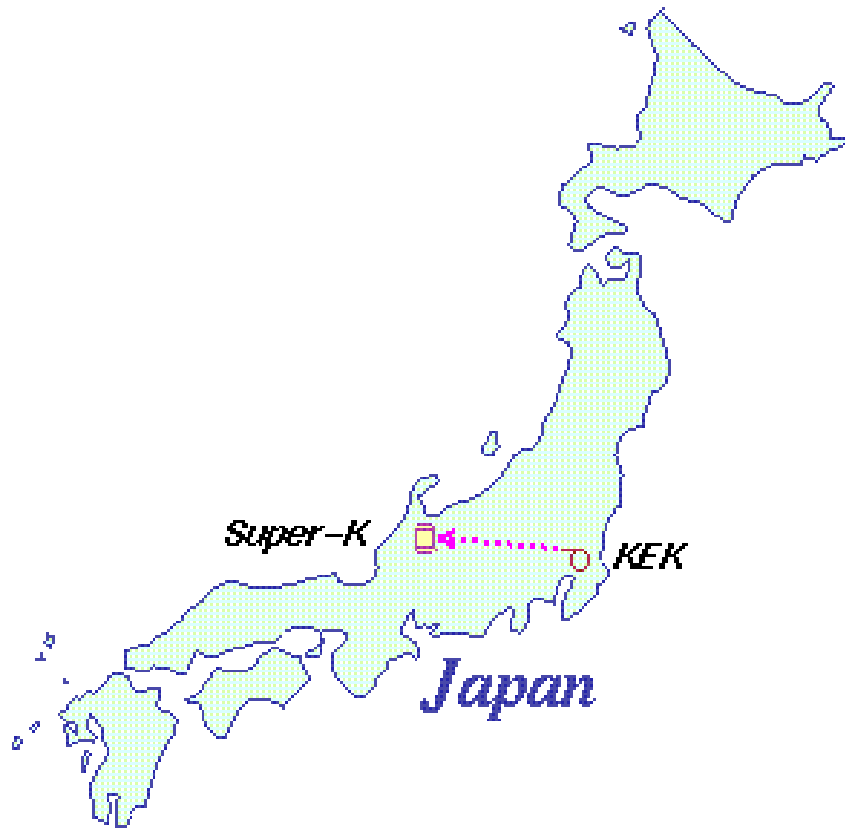
Super-K atmospheric neutrino data



consistent with $\nu_{\mu} \rightarrow \nu_{\tau}$ osc. with
 $\Delta m^2 \simeq 2.5 \times 10^{-3} \text{ eV}^2$, $\sin^2 \theta \simeq 0.5$

Long-baseline experiments

first generation of LBL experiments
(ν_μ -disappearance)

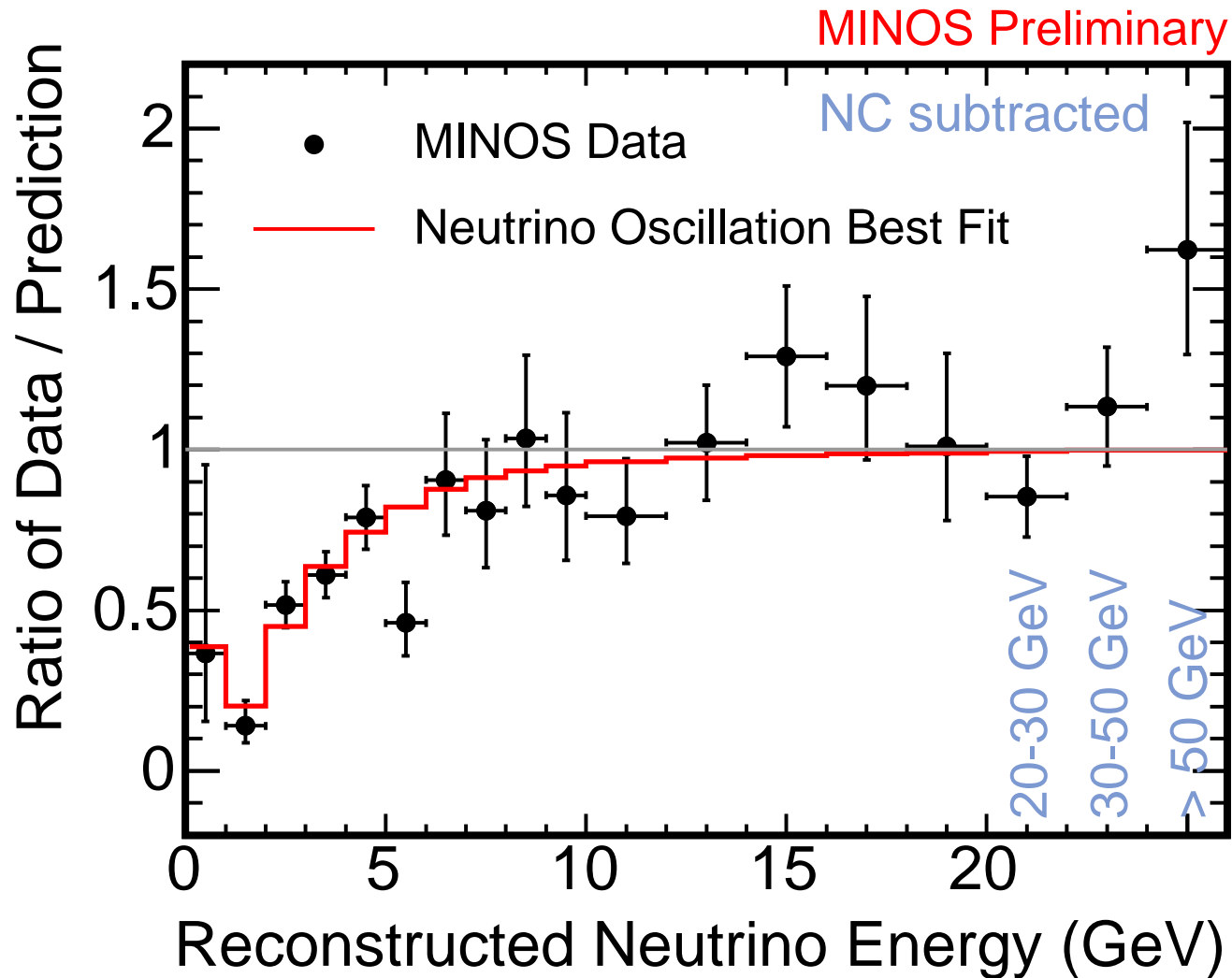


Long-baseline experiments

first generation of LBL experiments
(ν_μ -disappearance)

	K2K	MINOS
source	KEK	Fermilab
detector	Super-K	Soudan
baseline	250 km	735 km
neutrino energy	1.3 GeV	3 GeV
E_ν / L [eV ²]	5.2×10^{-3}	4.1×10^{-3}
obs. events	112	563
expect. w/o osc.	$158.1^{+9.2}_{-8.6}$	738 ± 30

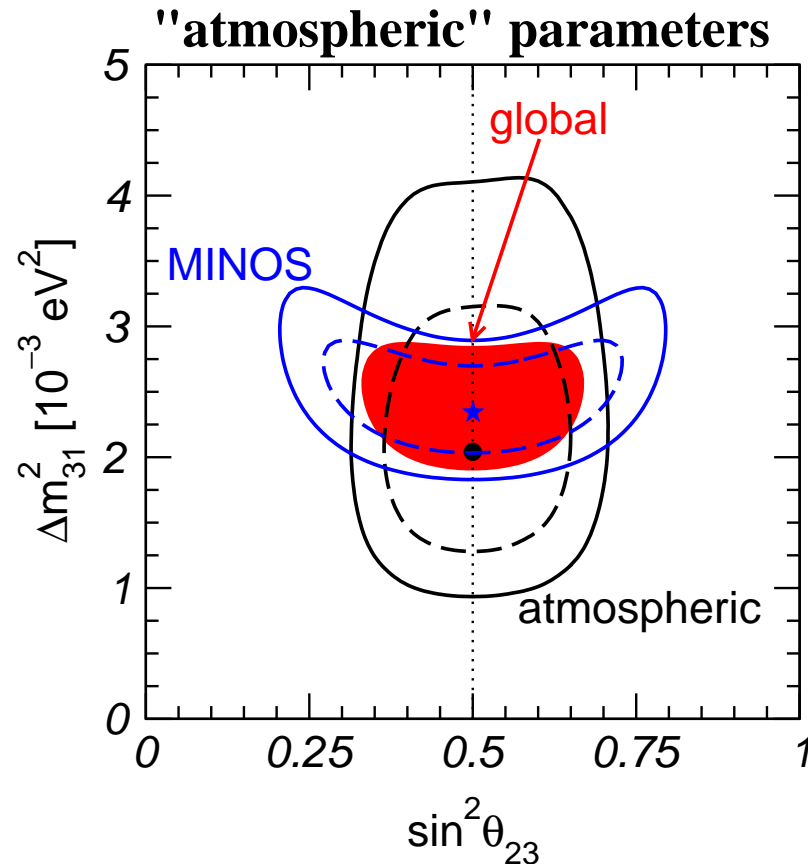
MINOS energy spectrum



arxiv:0708.1495, 2.5×10^{20} pot

Super-K + K2K + MINOS

90%, 99.73% CL regions

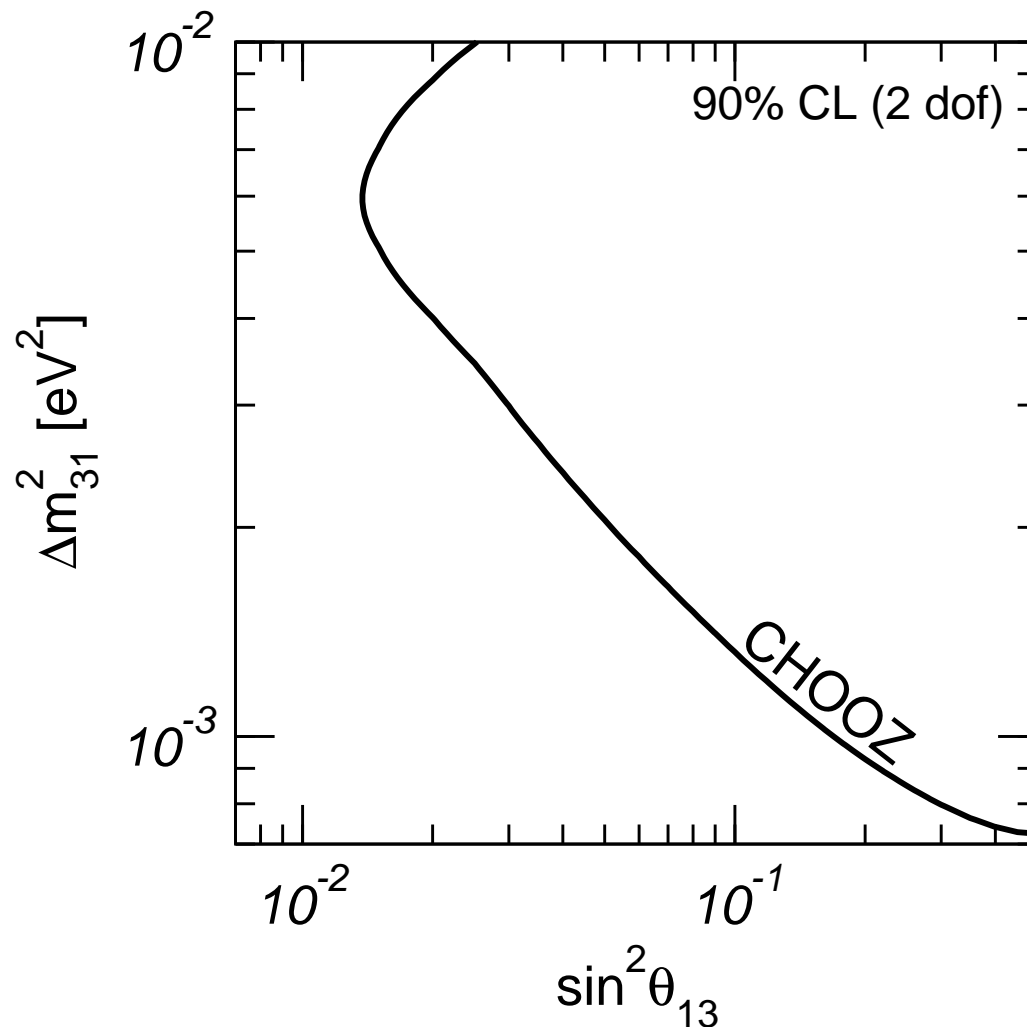


$$\Delta m_{31}^2 = 2.4 \pm 0.15 \times 10^{-3} \text{ eV}^2, \sin^2 \theta_{23} = 0.50 \pm 0.063$$

The bound on θ_{13}

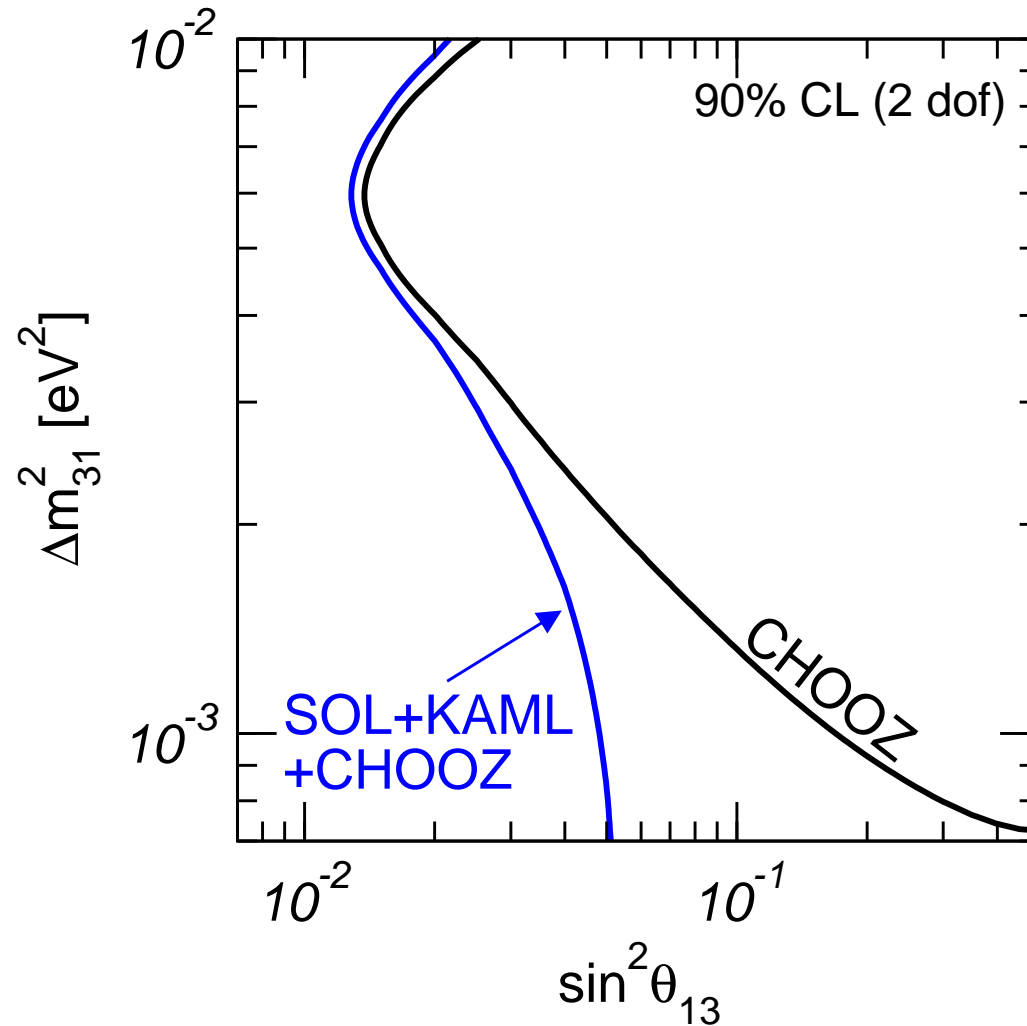
The bound on θ_{13}

The bound on θ_{13} emerges from an interplay of the global data



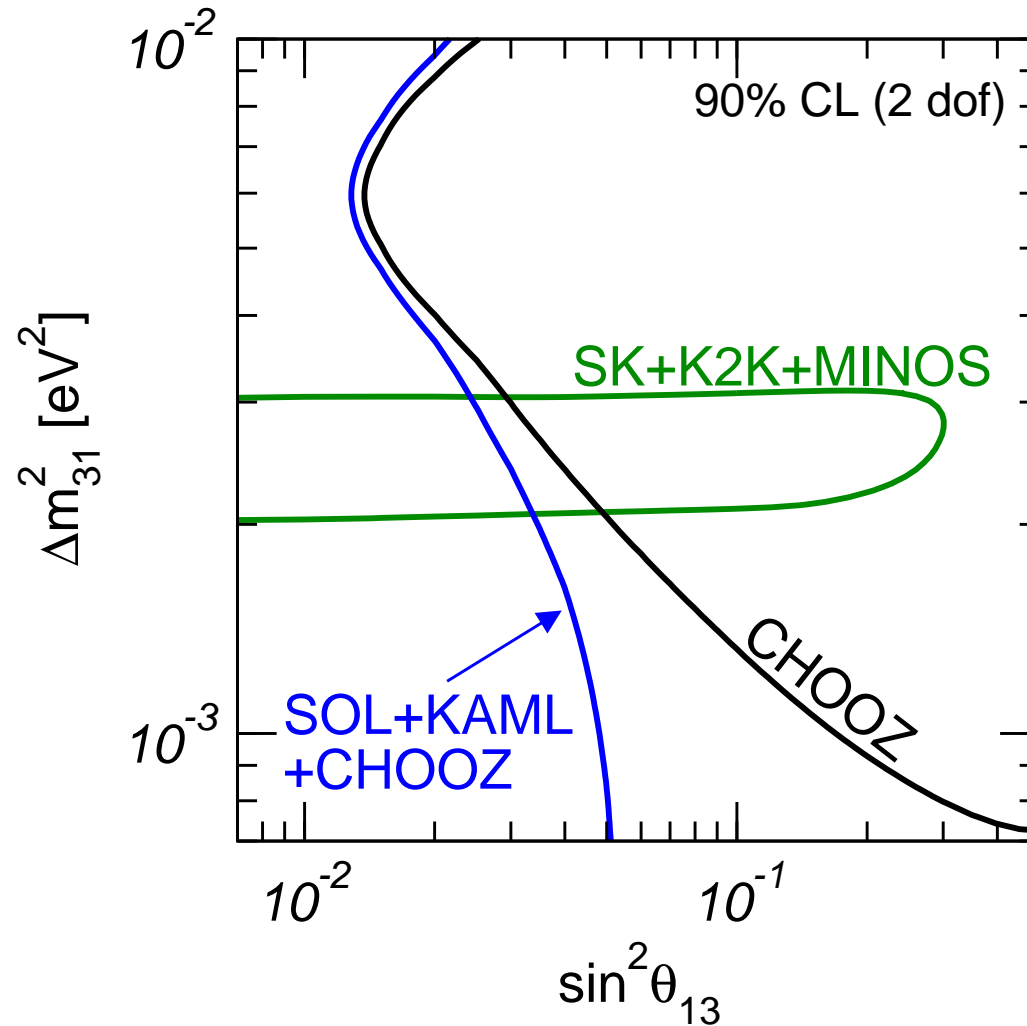
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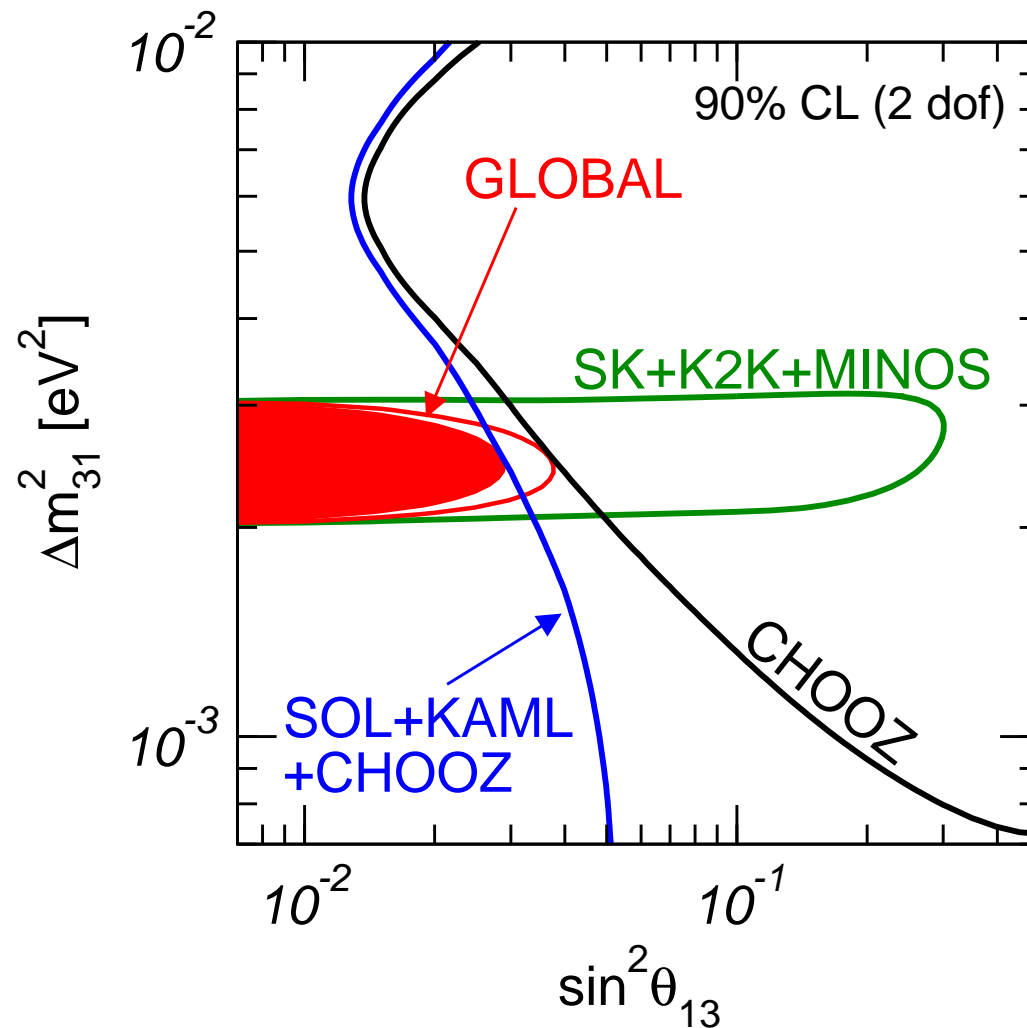
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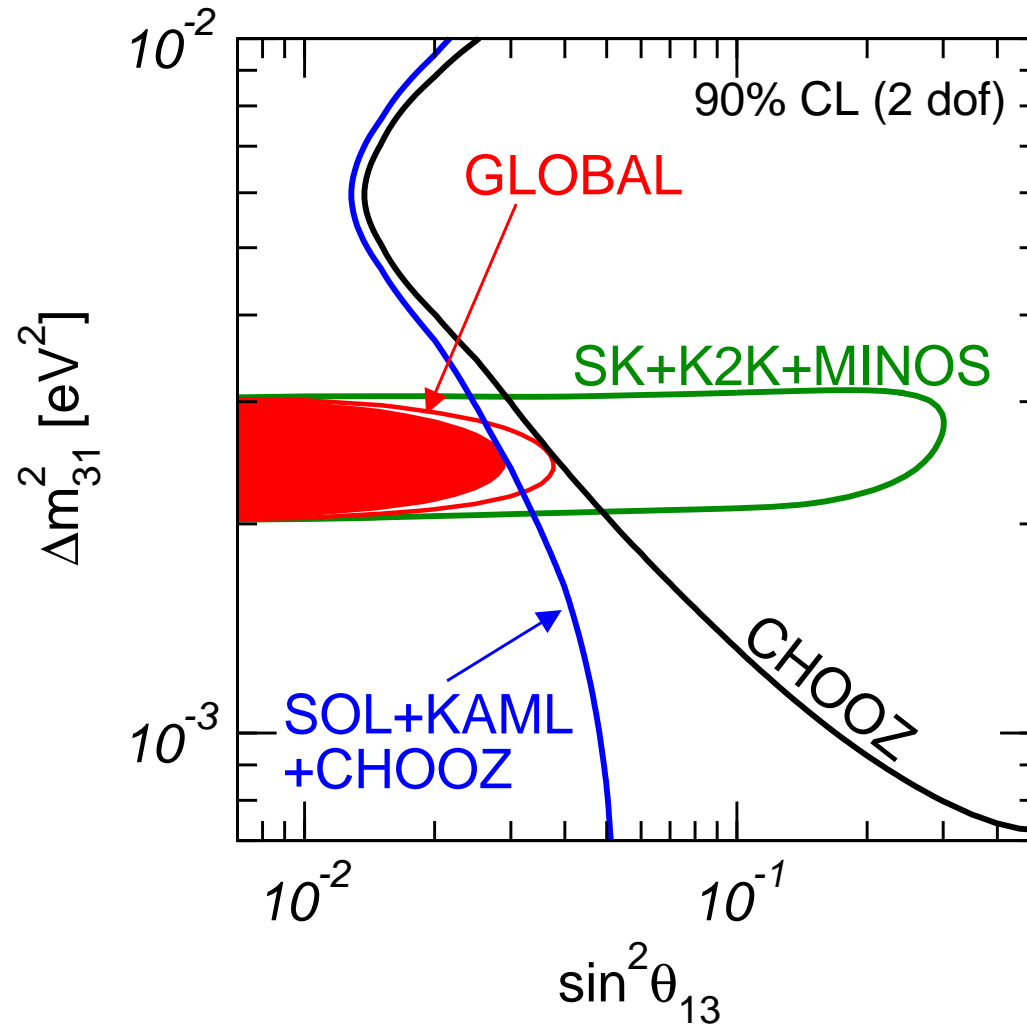
The bound on θ_{13}

global data: $\sin^2 \theta_{13} < 0.05$ at 3σ



The bound on θ_{13}

$$\sin \theta_{13} = |U_{e3}| < 0.224 (3\sigma) \quad \leftrightarrow \quad |V_{us}| = 0.2257 \pm 0.0021$$



Summary 3-flavour oscillation parameters

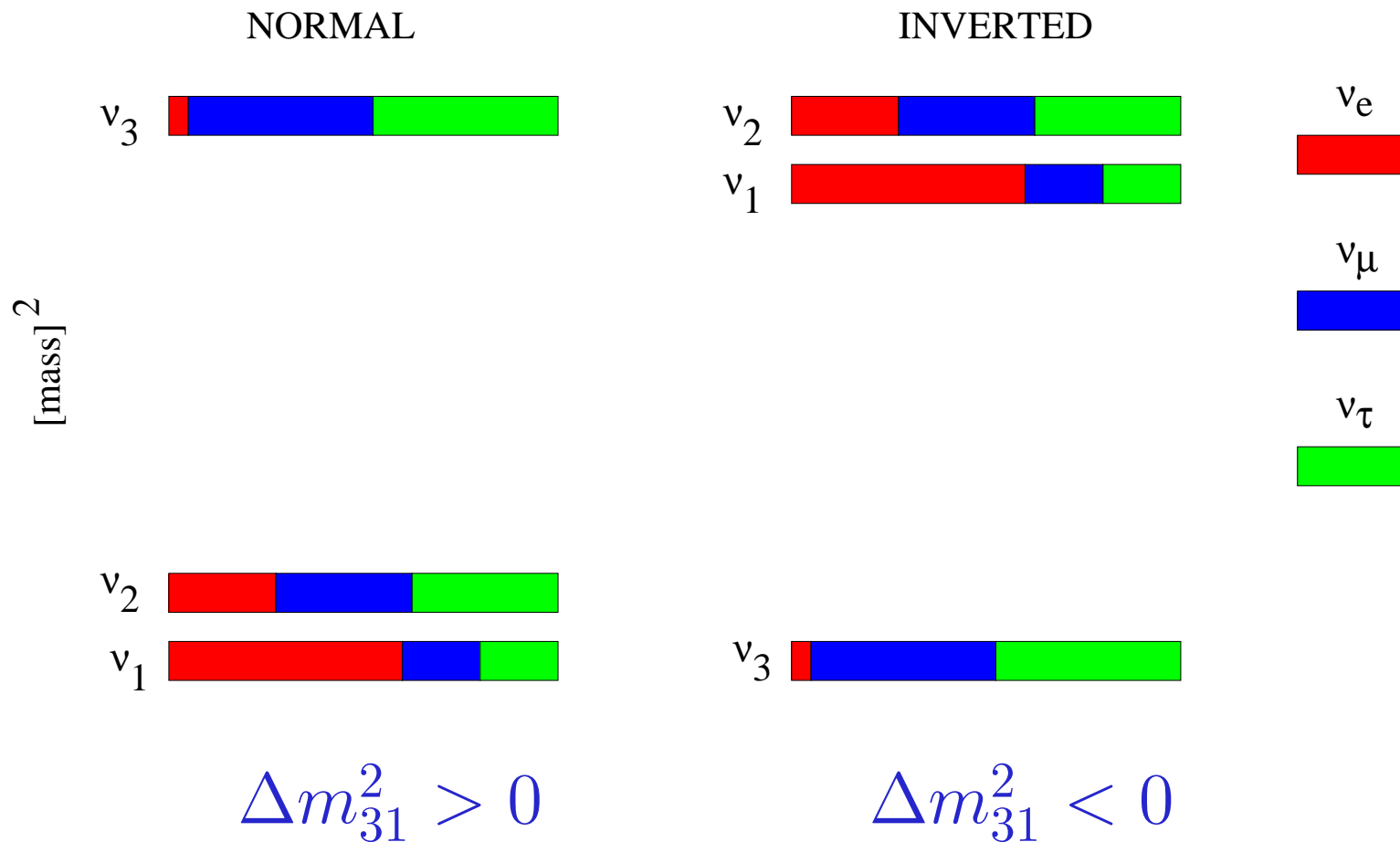
3-flavour oscillation parameters

	bf $\pm 1\sigma$	acc. @ 3σ	
Δm_{21}^2	$(7.6 \pm 0.2) 10^{-5} \text{ eV}^2$	(8%)	KamLAND
$\sin^2 \theta_{12}$	0.32 ± 0.023	(22%)	SNO
$ \Delta m_{31}^2 $	$(2.4 \pm 0.15) 10^{-3} \text{ eV}^2$	(17%)	MINOS
$\sin^2 \theta_{23}$	0.50 ± 0.063	(33%)	SK atm
$\sin^2 \theta_{13} < 0.05$	@ 3σ		CHOOZ

Maltoni, TS, Tortola, Valle, hep-ph/0405172 v6; TS, 0710.5027

Three flavour osc. parameters summary

two possibilities for the neutrino mass spectrum



What do we learn from these numbers?

Do they indicate some structure?

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Do they indicate some structure?

example: **Tri-bimaximal mixing**

Harrison, Perkins, Scott, PLB 2002, hep-ph/0202074

$$\sin^2 \theta_{12} = 1/3, \quad \sin^2 \theta_{23} = 1/2, \quad \sin^2 \theta_{13} = 0 \quad \Rightarrow$$

$$U = \begin{pmatrix} \sqrt{2/3} & 1/\sqrt{3} & 0 \\ -1/\sqrt{6} & 1/\sqrt{3} & 1/\sqrt{2} \\ 1/\sqrt{6} & -1/\sqrt{3} & 1/\sqrt{2} \end{pmatrix}$$

3-flavour oscillations

Open questions:

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- Is this basic picture correct?
LSND hint?
non-standard effects beyond oscillations?

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- Increase the precision on sol and atm params
(e.g. Is θ_{23} exactly 45° ? Tri-bimaximal mixing?)

3-flavour oscillations

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(e.g. Is θ_{23} exactly 45° ? Tri-bimaximal mixing?)
- How small is θ_{13} ?

3-flavour oscillations

Open questions:

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- How small is θ_{13} ?
- What is the value of the CP phase δ ?

3-flavour oscillations

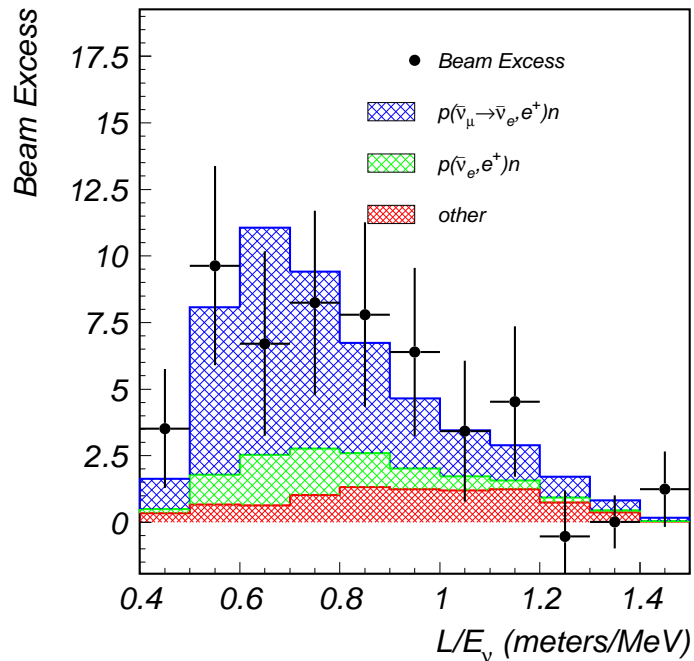
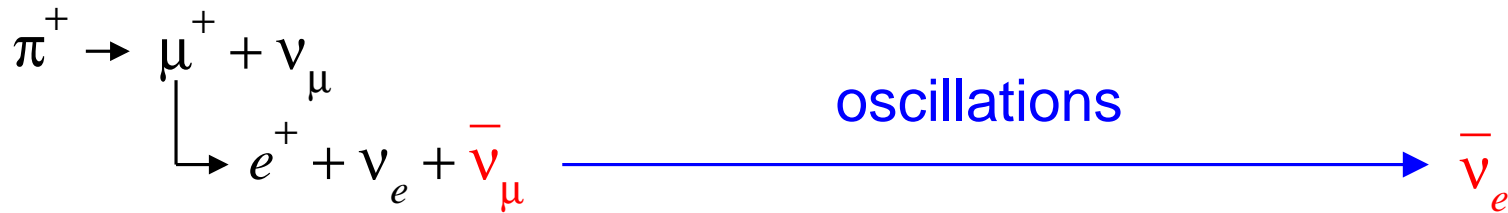
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- Is this basic picture correct?
LSND hint?
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- Increase the precision on sol and atm params
(e.g. Is θ_{23} exactly 45° ? Tri-bimaximal mixing?)
- How small is θ_{13} ?
- What is the value of the CP phase δ ?
- Type of the neutrino mass ordering (sign of Δm_{31}^2)

The LSND puzzle and MiniBooNE results

Maltoni, TS, 0705.0107

The LSND signal



$$L \simeq 35 \text{ m}$$

evidence for $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ oscillations

A. Aguilar *et al.*, PRD 64 (2001) 112007

$87.9 \pm 22.4 \pm 6.0$ excess events

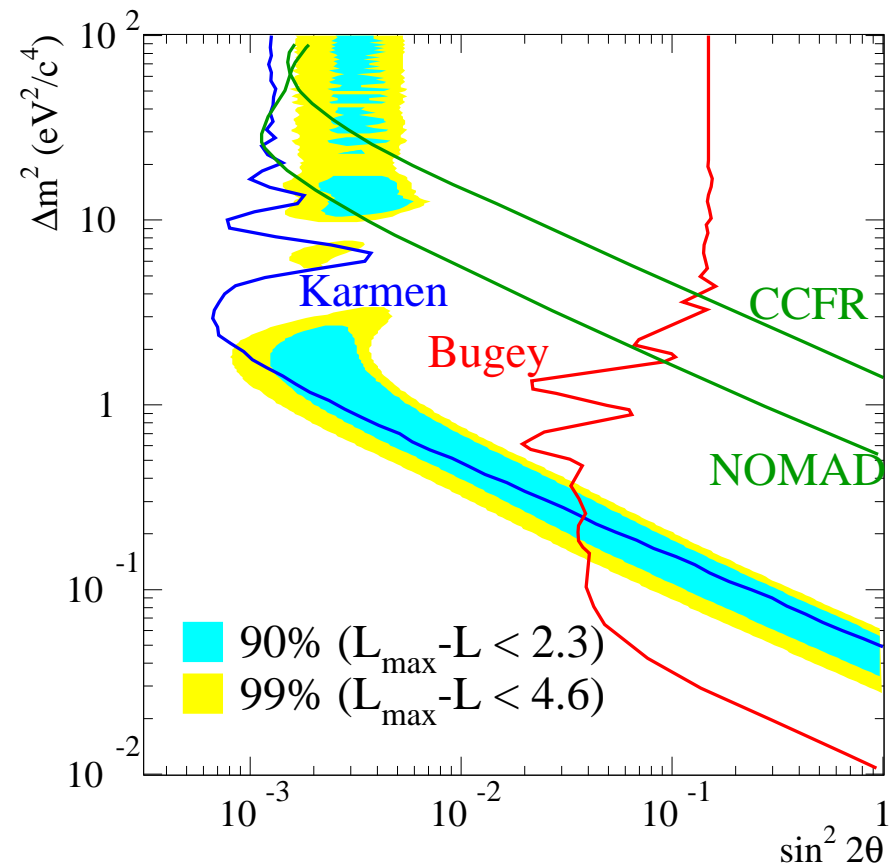
$P = (0.264 \pm 0.067 \pm 0.045)\%$

$\sim 3.3\sigma$ away from zero

Oscillation interpretation of LSND

the problem:

$\Delta m^2 \sim \text{eV}^2$ not consistent
with solar (8×10^{-5}) and
atmospheric (3×10^{-3})
mass splittings for three
neutrinos!



Check LSND with MiniBooNE

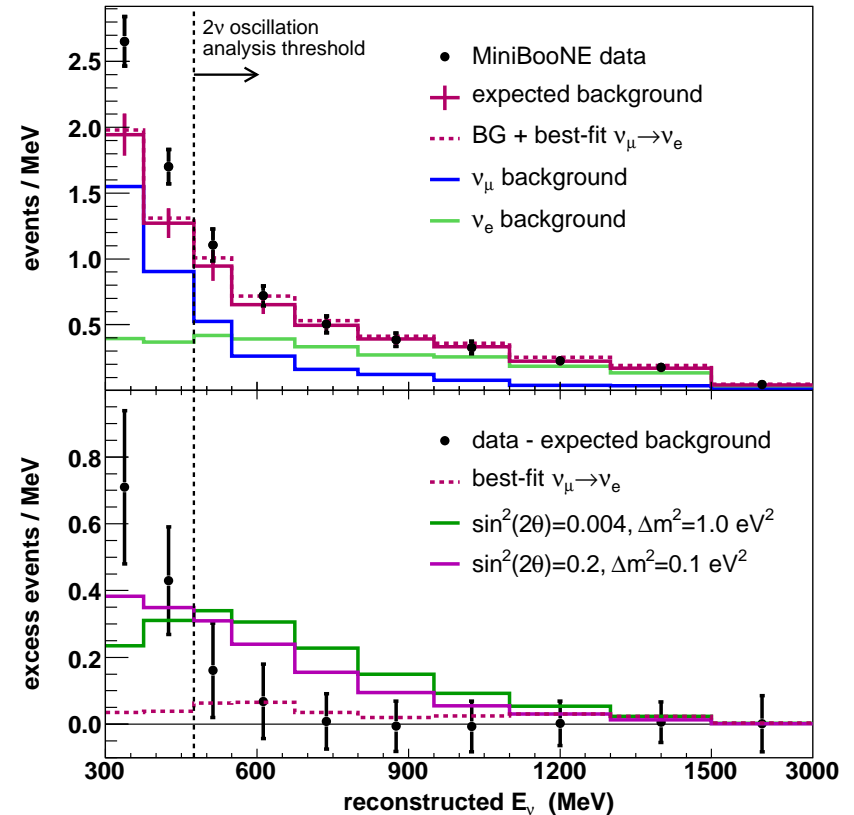
	LSND	MiniBooNE
energy	30 MeV	500 MeV
baseline	30 m	500 m
	same L/E_ν value	
channel	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$	$\nu_\mu \rightarrow \nu_e$

MiniBooNE results, April 2007

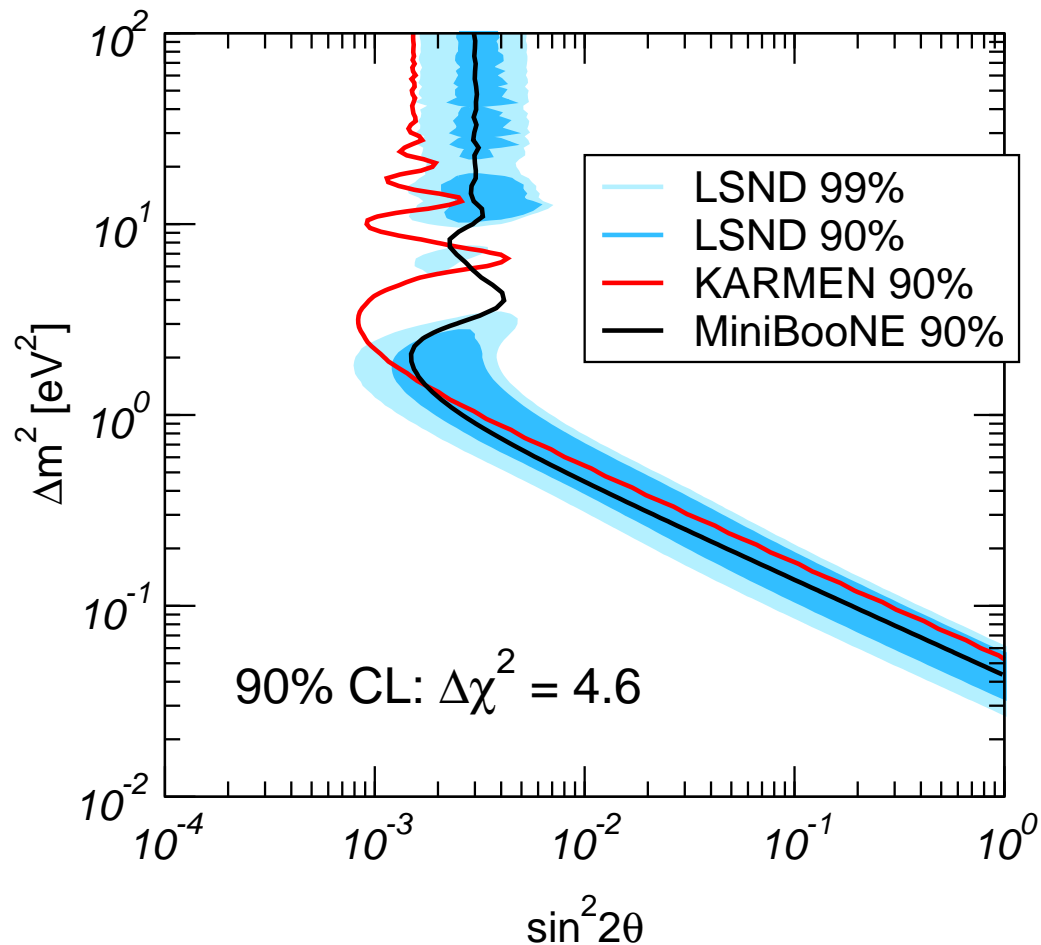
obs. events minus
background:

$475 < E_{\nu}^{\text{QE}} < 1250 \text{ MeV}$:
 $22 \pm 19 \pm 35$ events
(consistent with zero)

$300 < E_{\nu}^{\text{QE}} < 475 \text{ MeV}$:
 $96 \pm 17 \pm 20$ events
(excess at 3.6σ)



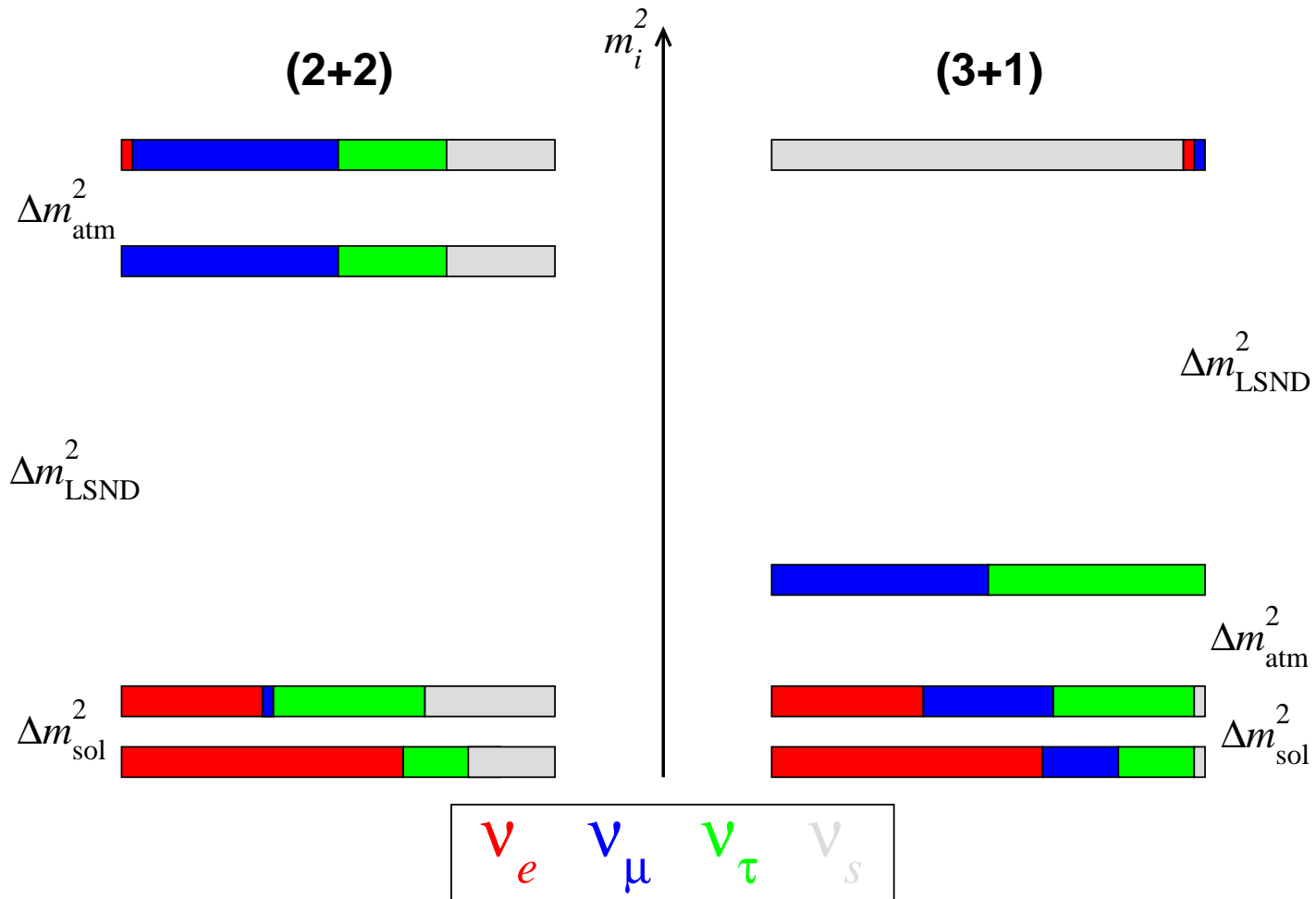
The MiniBooNE 2-neutrino limit



In the 2-neutrino framework MiniBooNE and LSND are incompatible at the 98% CL Aguilar-Arevalo et al., PRL08

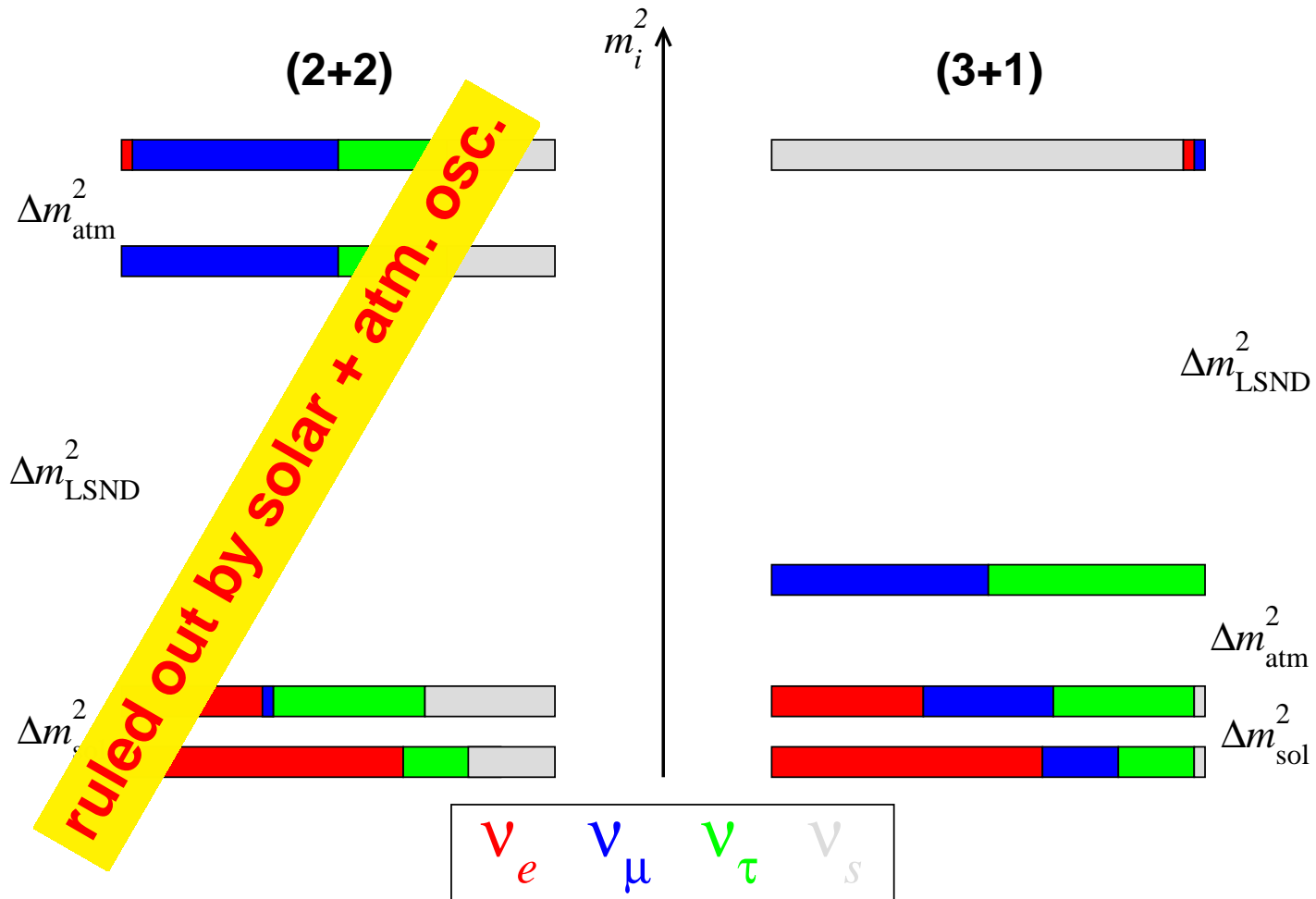
Adding a sterile neutrino

4-neutrino mass schemes:



Adding a sterile neutrino

4-neutrino mass schemes:



MB vs LSND in (3+1)

In (3+1) schemes the SBL appearance probability is effectively 2- ν oscillations:

$$P_{\mu e} = \sin^2 2\theta_{\text{SBL}} \sin^2 \frac{\Delta m_{41}^2 L}{4E}$$

with

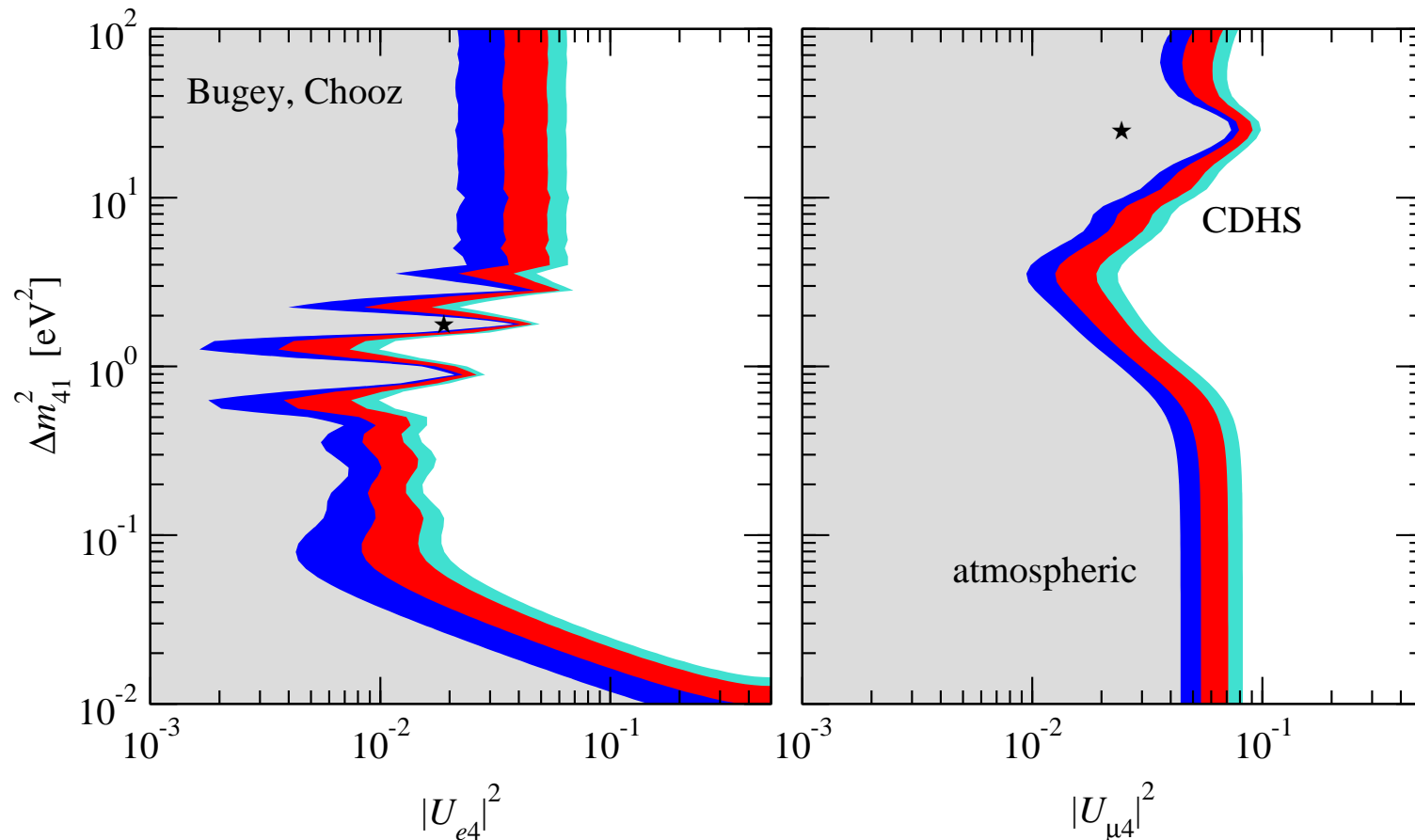
$$\sin^2 2\theta_{\text{SBL}} = 4|U_{e4}|^2|U_{\mu4}|^2$$

LSND / MiniBooNE inconsistency is the same as in the 2-flavour analysis presented by the MiniBooNE collaboration (98% CL)

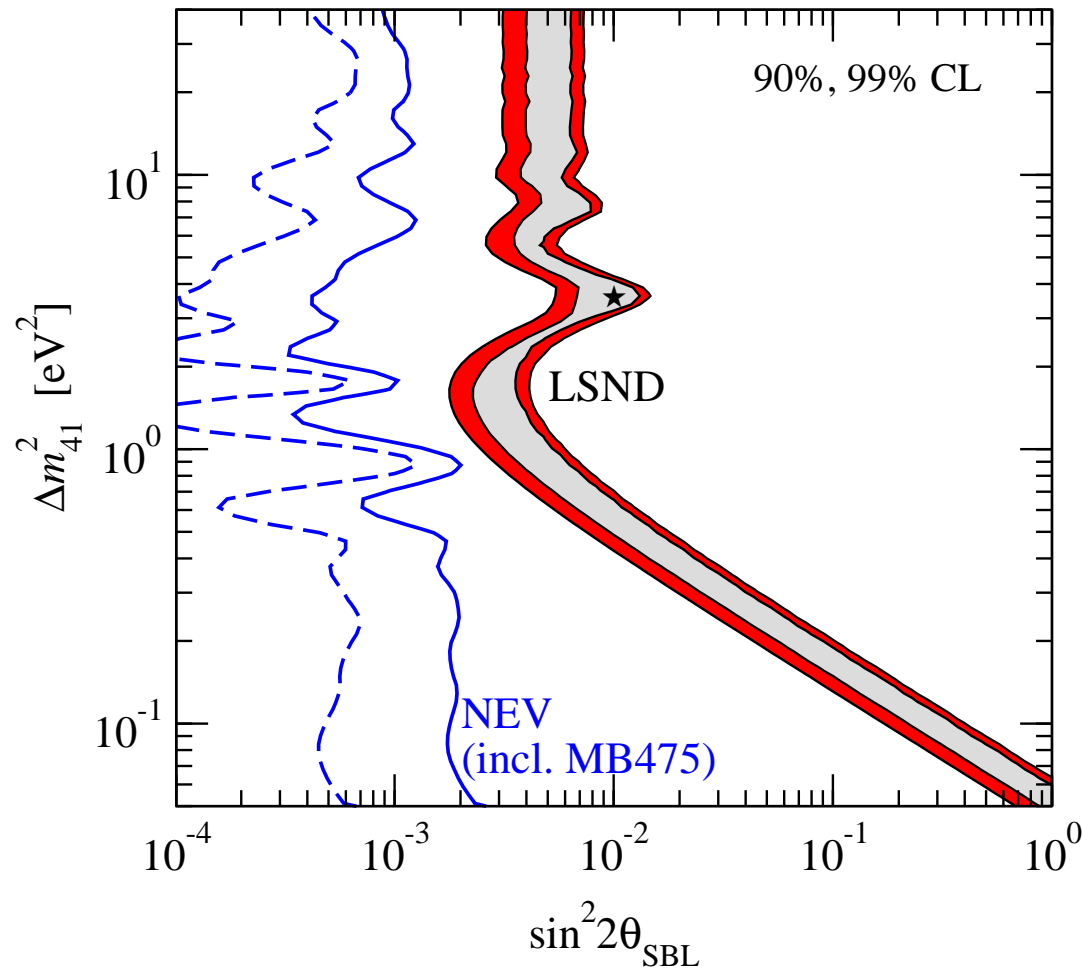
Appearance vs disappearance in (3+1)

appearance amplitude $\sin^2 2\theta_{\text{SBL}} = 4|U_{e4}|^2|U_{\mu4}|^2$

disappearance experiments bound $|U_{e4}|^2$ and $|U_{\mu4}|^2$



(3+1) global



before MB:

$$\chi_{\text{PG}}^2 = 20.9 \text{ (2 dof)}$$

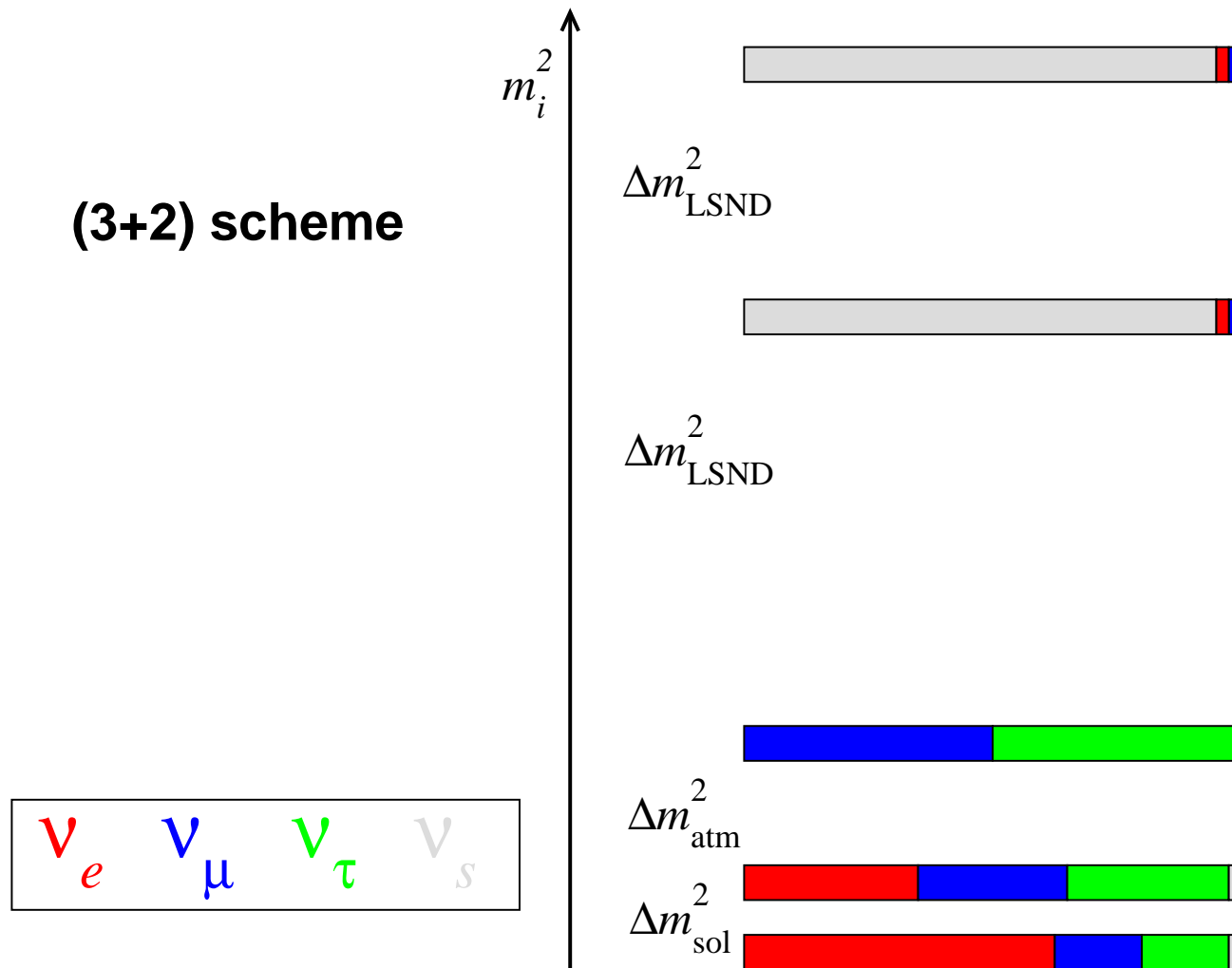
MB incl.:

$$\chi_{\text{PG}}^2 = 24.7 \text{ (2 dof)}$$

disagreement at
about 4σ

More sterile neutrinos?

5-neutrino oscillations



Sorel, Conrad, Shaevitz, hep-ph/0305255

(3+2) appearance probability

$$\begin{aligned} P_{\nu_\mu \rightarrow \nu_e} &= 4 |U_{e4}|^2 |U_{\mu4}|^2 \sin^2 \phi_{41} \\ &+ 4 |U_{e5}|^2 |U_{\mu5}|^2 \sin^2 \phi_{51} \\ &+ 8 |U_{e4} U_{\mu4} U_{e5} U_{\mu5}| \sin \phi_{41} \sin \phi_{51} \cos(\phi_{54} - \delta) \end{aligned}$$

with the definitions

$$\phi_{ij} \equiv \frac{\Delta m_{ij}^2 L}{4E}, \quad \delta \equiv \arg(U_{e4}^* U_{\mu4} U_{e5} U_{\mu5}^*) .$$

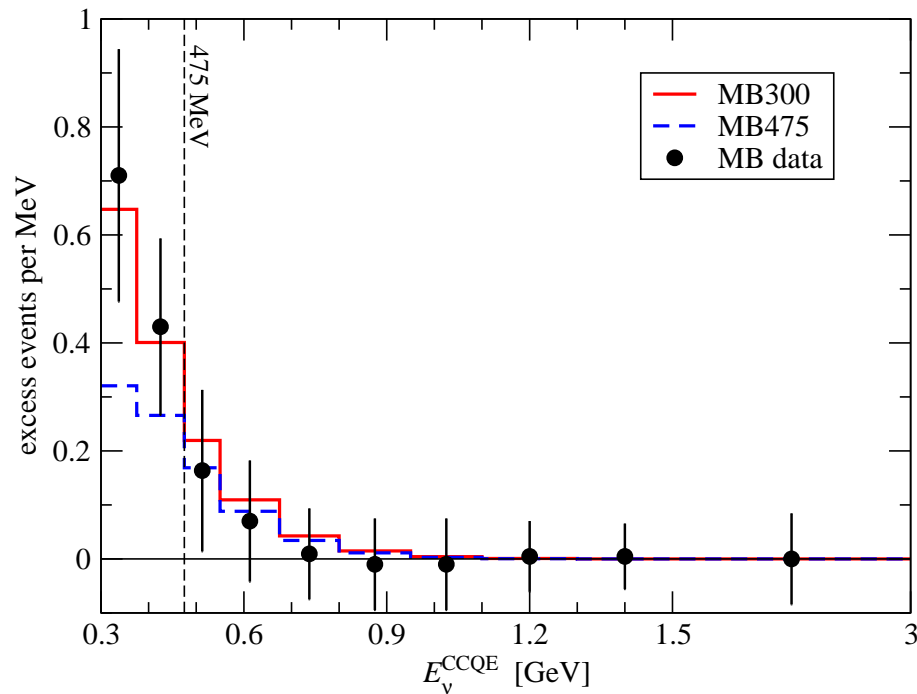
(3+2) osc. include the possibility of **CP violation!**

remember: MiniBooNE: neutrinos, LSND: anti-neutrinos

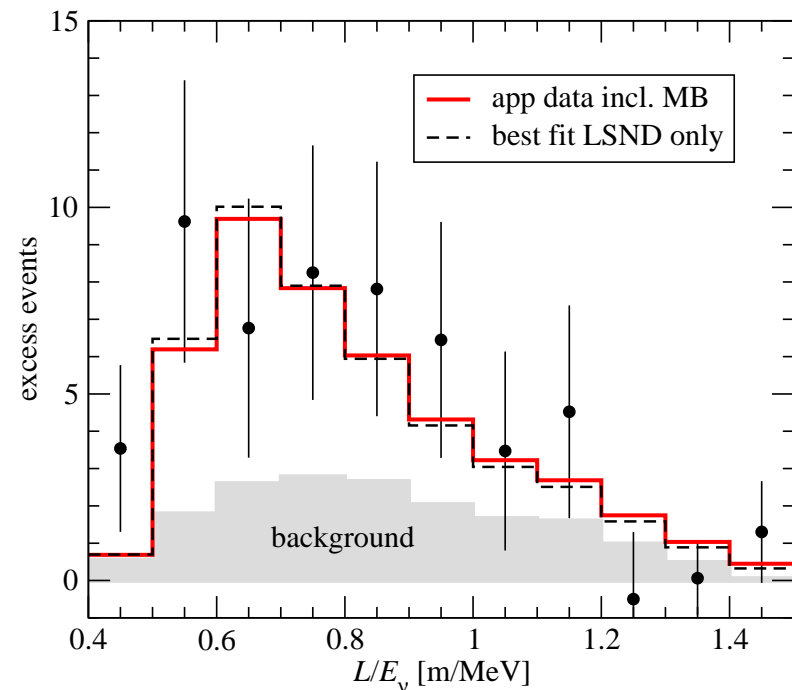
(3+2) appearance data

best fit point spectra:

MiniBooNE



LSND



Perfect fit to appearance data:

w/o MB low energy excess: $\chi_{\min}^2 = 16.9/(29 - 5)$

with MB low energy excess: $\chi_{\min}^2 = 18.5/(31 - 5)$

(3+2) disappearance data

what about the disappearance data?

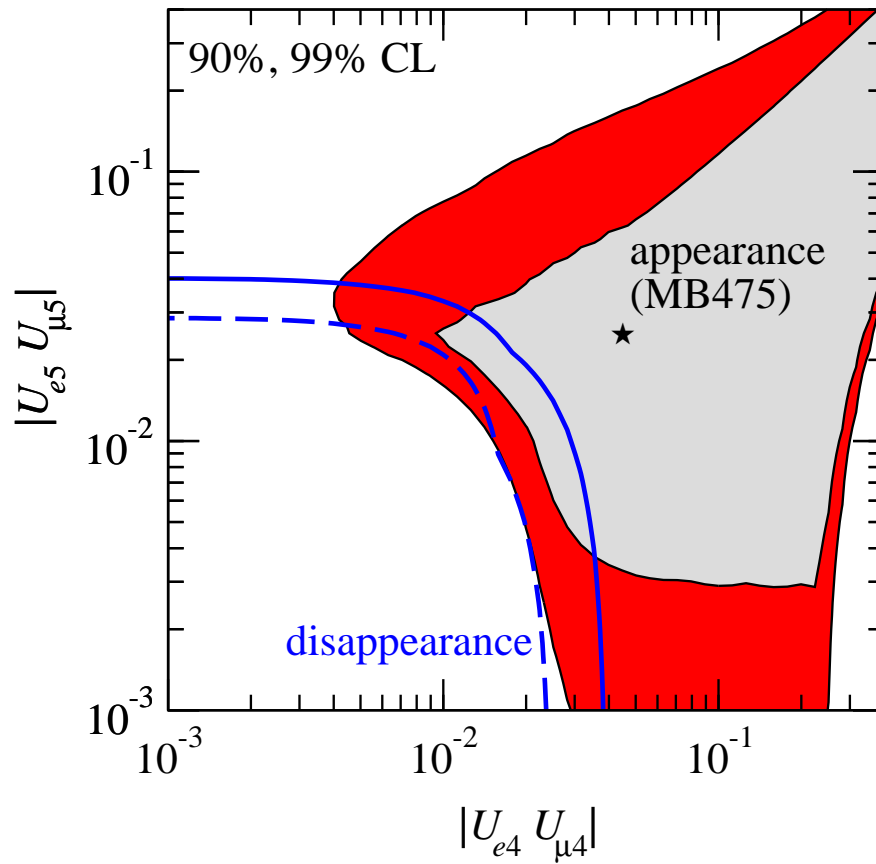
$$P_{\nu_\alpha \rightarrow \nu_\alpha} = 1 - 4 \left(1 - \sum_{i=4,5} |U_{\alpha i}|^2 \right) \sum_{i=4,5} |U_{\alpha i}|^2 \sin^2 \phi_{i1} \\ - 4 |U_{\alpha 4}|^2 |U_{\alpha 5}|^2 \sin^2 \phi_{54}$$

\Rightarrow bound $|U_{ei}|$ and $|U_{\mu i}|$ ($i = 4, 5$), similar as in (3+1)

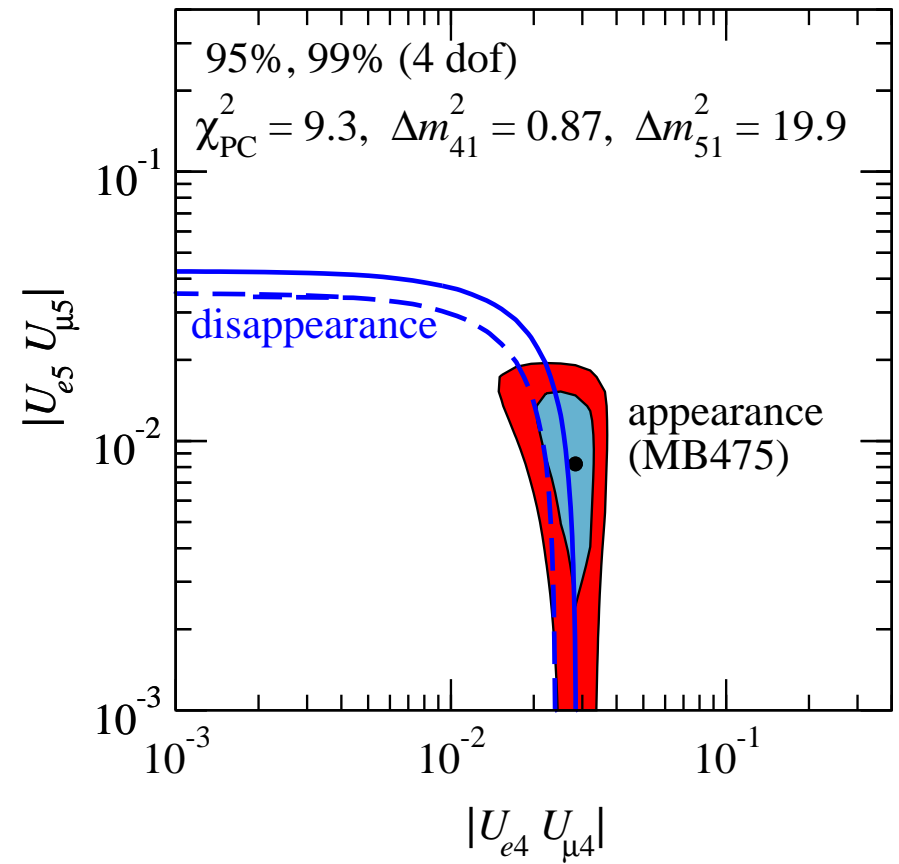
to be reconciled with appearance amplitudes $|U_{ei}U_{\mu i}|$

(3+2) app vs disap

projection



section



(3+2) global

testing consistency of disappearance and appearance data:

$$\chi_{\text{PG}}^2 = 17.2 \text{ (4 dof)} \quad \text{PG} = 0.18\%$$

(without MB: $\chi_{\text{PG}}^2 = 17.5$)

inconsistency at about 3.1σ

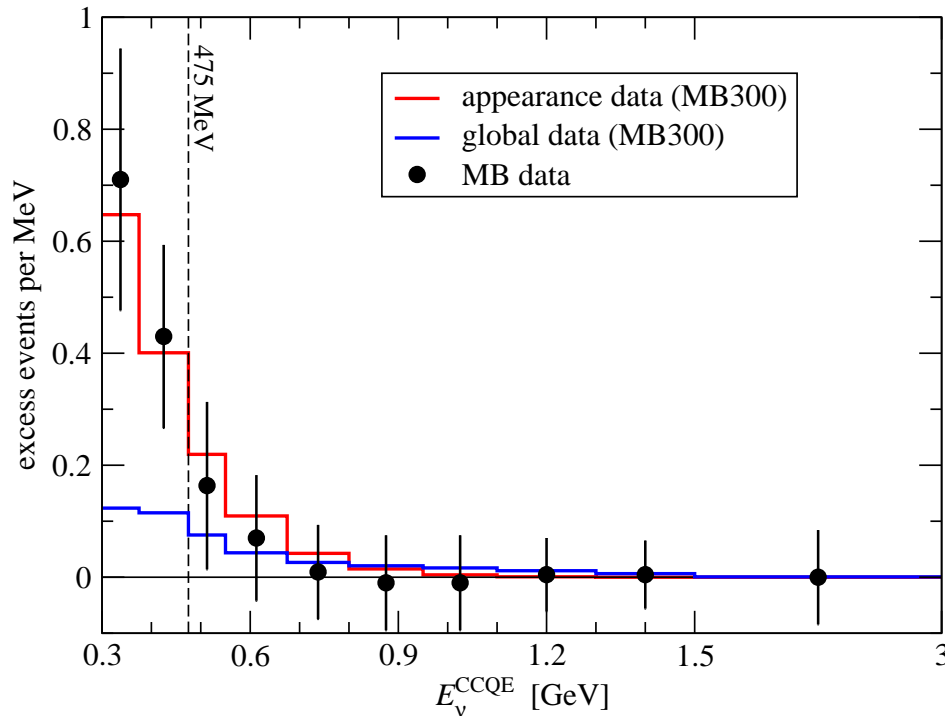
parameters in common $|U_{e4}U_{\mu4}|, |U_{e5}U_{\mu5}|, \Delta m_{41}^2, \Delta m_{51}^2$

best fit: $\Delta m_{41}^2 = 0.9 \text{ eV}^2, \Delta m_{51}^2 = 6.5 \text{ eV}^2, \chi_{\text{min}}^2 = 94.5/(107 - 7)$

$$\chi_{\text{min, global (3+1)}}^2 - \chi_{\text{min, global (3+2)}}^2 = 6.1/4 \text{ dof} \quad (81\% \text{ CL})$$

the low energy MB excess in the (3+2) fit

the MB low energy excess is not reproduced at the global best fit point:



$$\chi_{\text{MB300}}^2 = 104.4 / (109 - 7)$$

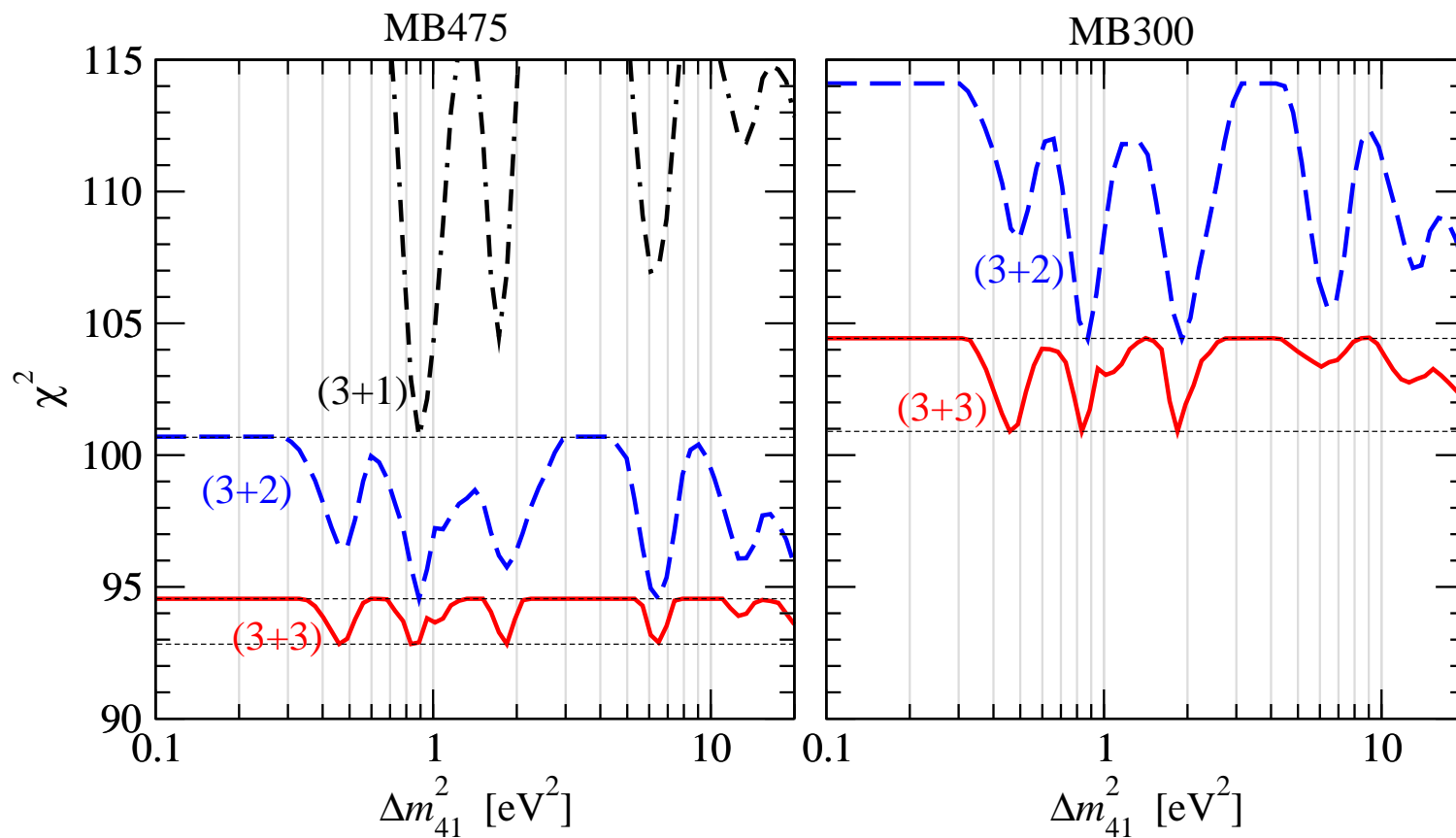
$$\chi_{\text{MB475}}^2 = 94.5 / (107 - 7)$$

$$\chi_{\text{PG}}^2 = 25.1 / 4$$

$$\text{PG} = 4.8 \times 10^{-5} \quad (4\sigma)$$

adding another sterile: (3+3)

(3+3) global fit



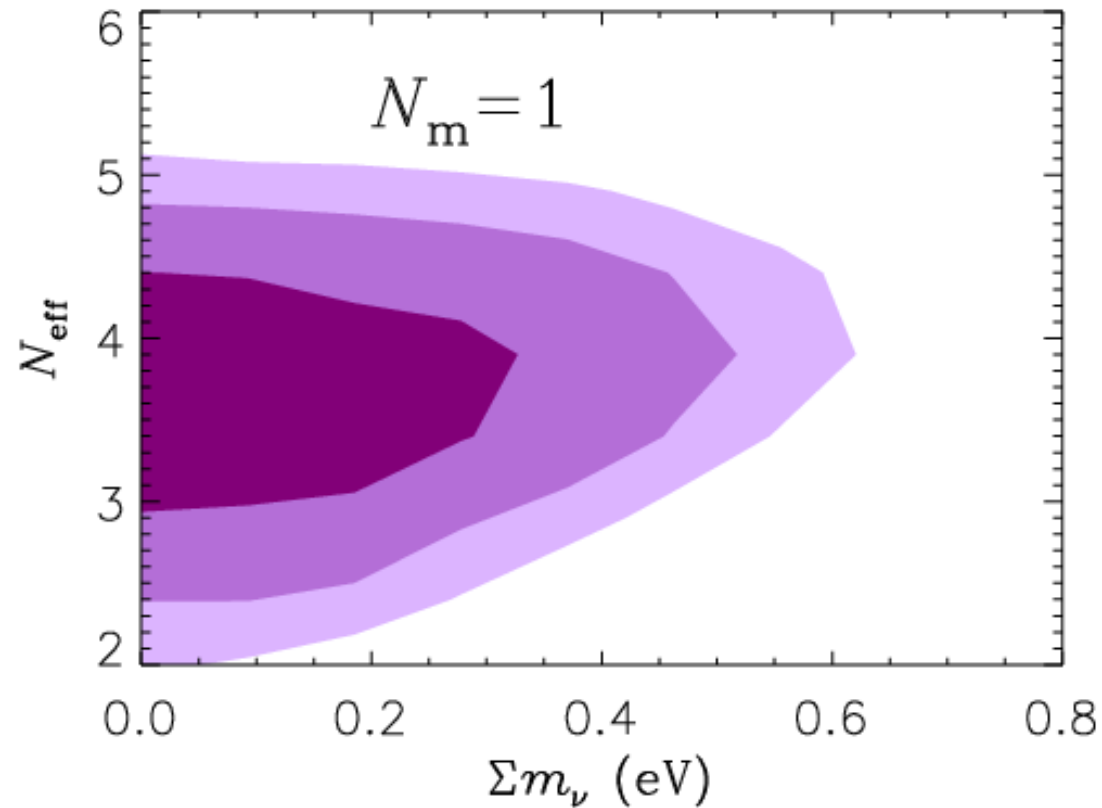
	Δm_{41}^2	Δm_{51}^2	Δm_{61}^2	χ_{\min}^2	$\chi_{(3+2)}^2 - \chi_{(3+3)}^2$	CL
MB475	0.46	0.83	1.84	92.8	1.7/4	20%
MB300	0.46	0.83	1.84	100.9	3.5/4	52%

All these sterile neutrino schemes have problems with cosmology

- sterile states contribute to the relativistic degrees of freedom (CMB, BBN)
- conflict with bound on the sum of neutrino masses from various cosmological data sets (LSS)

Cosmology

SN Ia, LSS (2dF, SDSS), BAO, CMB (WMAP, BOOMERANG)



68%, 95%, 99% CL

Hannestad, Raffelt, astro-ph/0607101

More 'exotic' proposals

- **3-neutrinos and CPT violation** Murayama, Yanagida 01; Barenboim, Borisso, Lykken 02; Gonzalez-Garcia, Maltoni, Schwetz 03

- **4-neutrinos and CPT violation** Barger, Marfatia, Whisnant 03
- **Exotic muon-decay** Babu, Pakvasa 02
- **CPT viol. quantum decoherence** Barenboim, Mavromatos 04
- **Lorentz violation**
Kostelecky, Mews, 04; Gouvea, Grossman, 06; Katori, Kostelecky, Tayloe, 06
- **mass varying neutrinos**
Kaplan, Nelson, Weiner 04; Zurek 04; Barger, Marfatia, Whisnant 05
- **shortcuts of sterile neutrinos in extra dimensions**
Paes, Pakvasa, Weiler 05
- **1 decaying sterile neutrino** Palomares-Riuz, Pascoli, Schwetz 05
- **2 decaying sterile neutrinos with CPV**
- **sterile neutrinos and new gauge boson** Nelson, Walsh 07

- **3-neutrinos and CPT** KamLAND+atmospheric antineutrino data
Barenboim, B... , Gonzalez-Garcia, Maltoni, Schwetz 03

- **4-neutrinos and CPT violation** Barger, Marfatia, Whisnant 03
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An exotic sterile neutrino with energy dependent mass or mixing

TS, 0710.2985

Energy dependent sterile neutrino

Experiment	Channel	$\langle E_\nu \rangle$
Bugey	$\bar{\nu}_e \rightarrow \bar{\nu}_e$	4 MeV
Chooz	$\bar{\nu}_e \rightarrow \bar{\nu}_e$	4 MeV
Palo Verde	$\bar{\nu}_e \rightarrow \bar{\nu}_e$	4 MeV
LSND	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$	40 MeV
KARMEN	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$	40 MeV
MiniBooNE	$\nu_\mu \rightarrow \nu_e$	700 MeV
CDHS	$\nu_\mu \rightarrow \nu_\mu$	1 GeV
NOMAD	$\nu_\mu \rightarrow \nu_e$	50 GeV

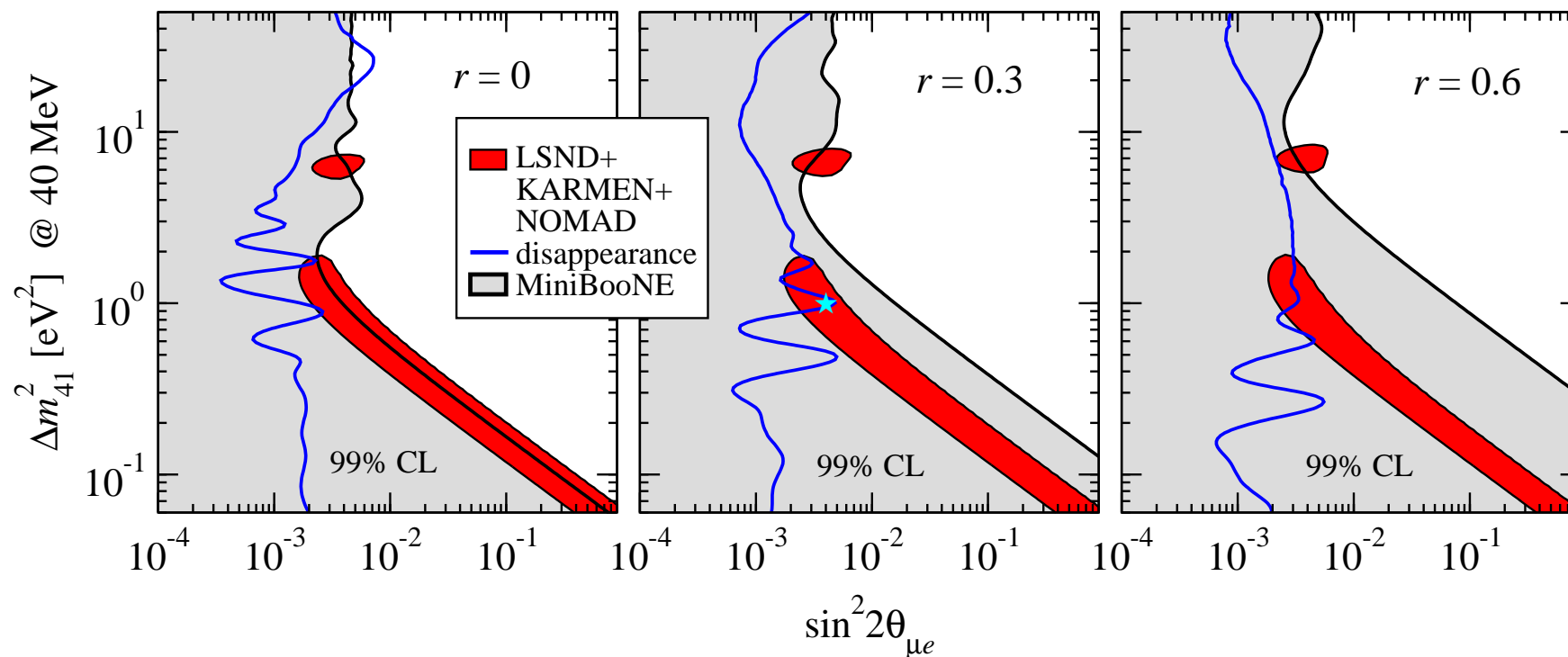
e.g., assume a 4th neutrino with an energy dependent mass:

$$m_4^2 = m_*^2 \left(\frac{E_*}{E_\nu} \right)^r$$

$$(r \geq 0)$$

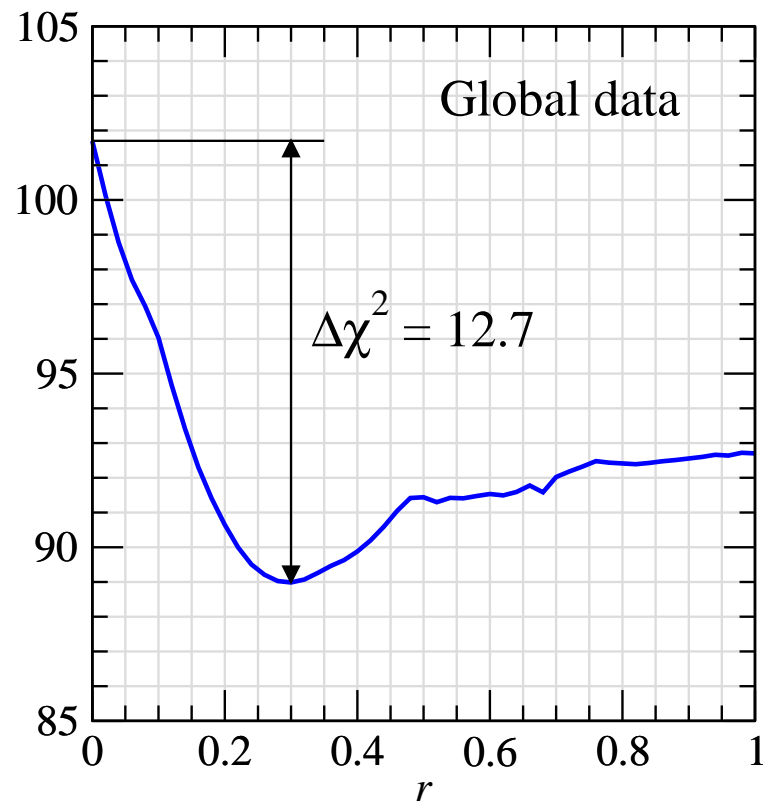
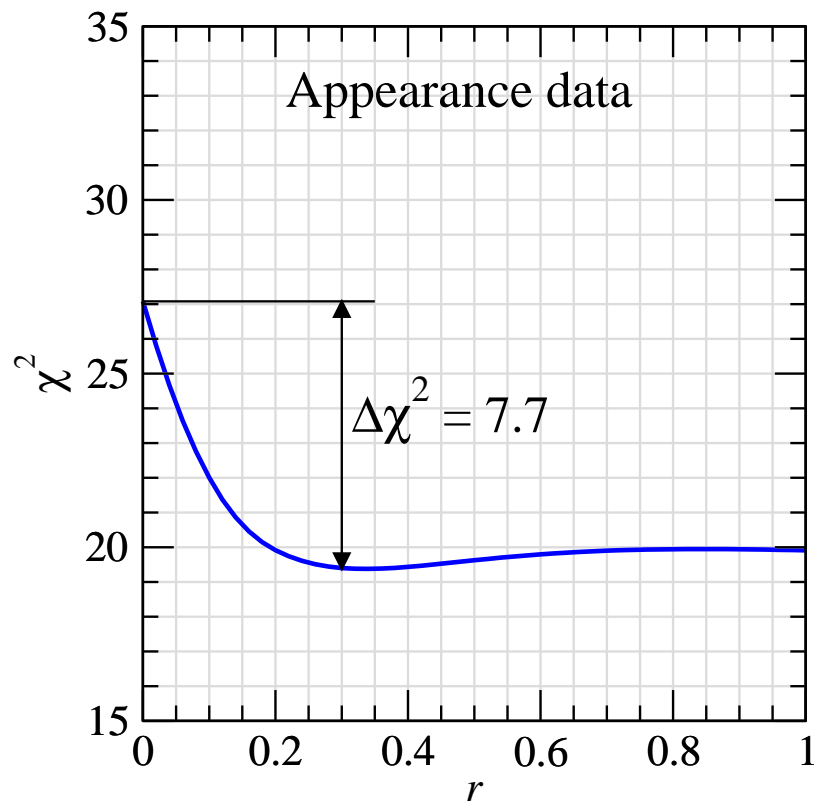
Energy dependent sterile neutrino

A sterile neutrino with an energy dependent mass



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Summary LSND

- **(3+1)**: strongly disfavoured
- **(3+2)**: LSND and MiniBooNE are consistent
but: severe tension in the global fit
- many exotic “solutions” fail

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For the rest of this talk I will assume a non-oscillation explanation for the LSND signal and the low-energy MiniBooNE excess, and stick to the three-neutrino oscillation framework.

Future oscillation experiments

Upcoming experiments

Conventional beam experiments:

Reactor experiments with near and far detectors:

Off-axis superbeams:

Upcoming experiments

Label	L	$\langle E_\nu \rangle$	mass	channel
Conventional beam experiments:				
MINOS	735 km	3 GeV	5.4 kt	$\nu_\mu \rightarrow \nu_\mu, \nu_e$
Reactor experiments with near and far detectors:				
Off-axis superbeams:				

MINOS:

Fermilab to Soudan mine, 5.4 kt magnetized iron calorimeter

Upcoming experiments

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MINOS	735 km	3 GeV	5.4 kt	$\nu_\mu \rightarrow \nu_\mu, \nu_e$
OPERA	732 km	17 GeV	1.65 kt	$\nu_\mu \rightarrow \nu_e, \nu_\mu, \nu_\tau$
Reactor experiments with near and far detectors:				
Off-axis superbeams:				

CNGS: CERN to Gran Sasso, ν_τ appearance

OPERA: 1.65 kt emulsion cloud chamber

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Reactor experiments with near and far detectors:				
D-Chooz	1.05 km	~ 4 MeV	~ 10 t	$\bar{\nu}_e \rightarrow \bar{\nu}_e$
Daya Bay	2./1.6 km	~ 4 MeV	~ 80 t	$\bar{\nu}_e \rightarrow \bar{\nu}_e$
Off-axis superbeams:				

D-Chooz: new experiment at Chooz site (50 000 events)

Daya Bay: “big” reactor experiment in China (500 000 ev)

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Off-axis superbeams:				
T2K	295 km	0.76 GeV	22.5 kt	$\nu_\mu \rightarrow \nu_e, \nu_\mu$
NOνA	812 km	2.22 GeV	20 kt	$\nu_\mu \rightarrow \nu_e, \nu_\mu$

T2K: Tokai (JPARC) to Kamioka (SK) 22.5 kt water Cherenkov

NO ν A: T ASD detector, off-axis angle of 0.72°

LBL experiments beyond ten years

- superbeam upgrades $(\nu_\mu \rightarrow \nu_e, \nu_\mu) + (\bar{\nu}_\mu \rightarrow \bar{\nu}_e, \bar{\nu}_\mu)$
 - T2HK**: beam 0.77 \rightarrow 4 MW, SK (22.5 kt) \rightarrow HK (500 kt)
 - T2KK**: second detector in Korea
 - NO ν A**: proton driver, second detector
 - WBB**: wideband beam, $E_\nu \sim \text{GeV}$, $L \gtrsim 1000 \text{ km}$
 - CNGS**-upgrades (beam upgrade, liquid Ar detector)
 - SPL**: CERN to \sim Mt water Cerenkov at Frejus (130 km)

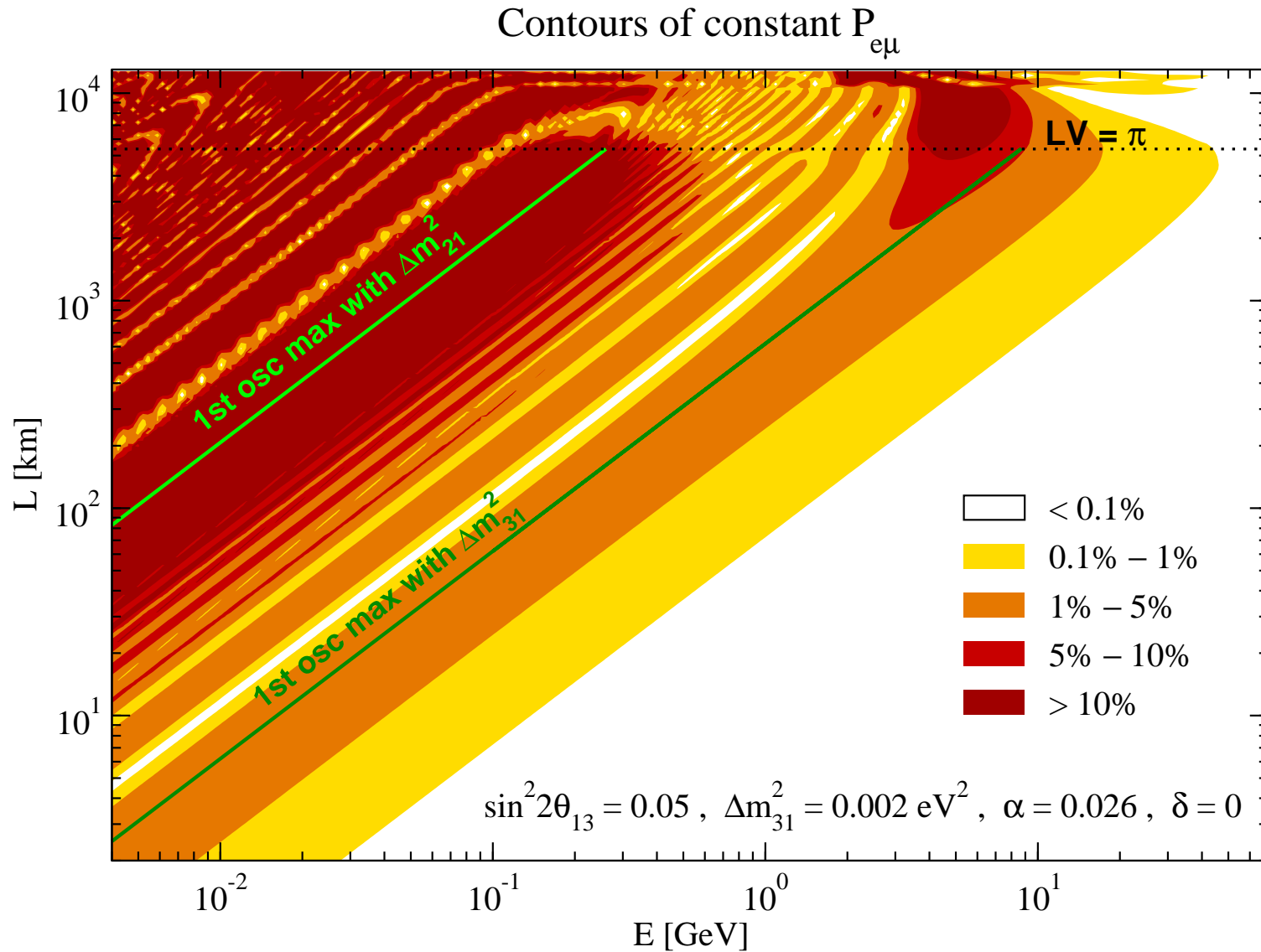
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 - low γ $\beta\mathbf{B}$ z.B. CERN-Frejus ($E_\nu \sim 0.4 \text{ GeV}$) or
 - high γ $\beta\mathbf{B}$ (longer BL), mono-energetic $\beta\mathbf{B}$

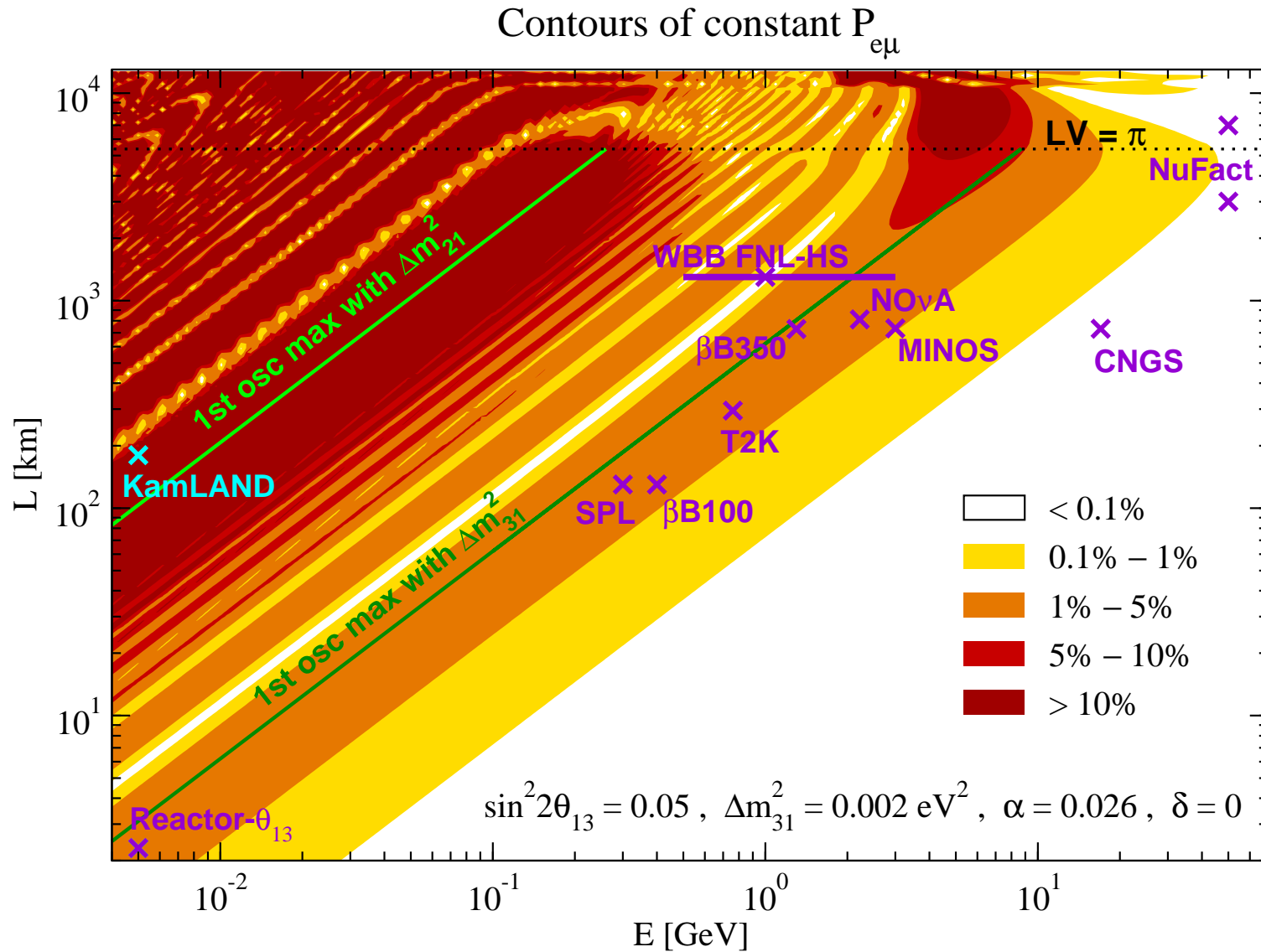
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high γ **β B** (longer BL), mono-energetic **β B**
- **neutrino factory** (**NuFact**) $(\nu_e, \nu_\mu \rightarrow \nu_\mu) + (\bar{\nu}_e, \bar{\nu}_\mu \rightarrow \bar{\nu}_\mu)$
 $E_\nu \sim 20 - 50 \text{ GeV}$, $1000 \text{ km} \lesssim L \lesssim 7000 \text{ km}$

LBL oscillation probability



LBL oscillation probability



What is the value of θ_{13} ?

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- naively one would expect $\theta_{12} \sim \theta_{23} \sim \theta_{13}$
 $\rightarrow \theta_{13}$ around the corner
- $\theta_{13} \ll 1$ hint for some symmetry

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- naively one would expect $\theta_{12} \sim \theta_{23} \sim \theta_{13}$
 $\rightarrow \theta_{13}$ around the corner
- $\theta_{13} \ll 1$ hint for some symmetry
- relatively large θ_{13} opens the possibility to observe generic 3-flavour effects (CP-violation)

Measuring θ_{13}

- $\bar{\nu}_e \rightarrow \bar{\nu}_e$ disappearance reactor experiments with near and far detectors: **D-Chooz, Daya Bay**
- LBL $\nu_\mu \rightarrow \nu_e$ appearance experiments
(MINOS, CNGS) T2K, NO ν A

Measuring θ_{13} by $\nu_{\mu} \rightarrow \nu_e$ at beams

The measurement of θ_{13} with the $\nu_{\mu} \rightarrow \nu_e$ appearance channel suffers from **correlations** and **degeneracies**:

G.L. Fogli, E. Lisi, Phys. Rev. D54 (1996) 3667

J. Burguet-Castell et al., Nucl. Phys. B608 (2001) 301

H. Minakata, H. Nunokawa, JHEP 10 (2001) 001

V.Barger, D.Marfatia, K.Whisnant, Phys. Rev. D65 (2002) 073023; D66 (2002) 053007

P.Huber, M.Lindner, W.Winter, Nucl. Phys. B645 (2002) 3; Nucl. Phys. B654 (2003) 3

and many more

Not $\sin^2 2\theta_{13}$, but only a specific **parameter combination** is measured very accurately

The LBL appearance oscillation probability

$$P_{\mu e} \simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \frac{\sin^2(1-A)\Delta}{(1-A)^2} \\ + \sin 2\theta_{13} \hat{\alpha} \sin 2\theta_{23} \frac{\sin(1-A)\Delta}{1-A} \frac{\sin A\Delta}{A} \cos(\Delta + \delta_{\text{CP}}) \\ + \hat{\alpha}^2 \cos^2 \theta_{23} \frac{\sin^2 A\Delta}{A^2}$$

with

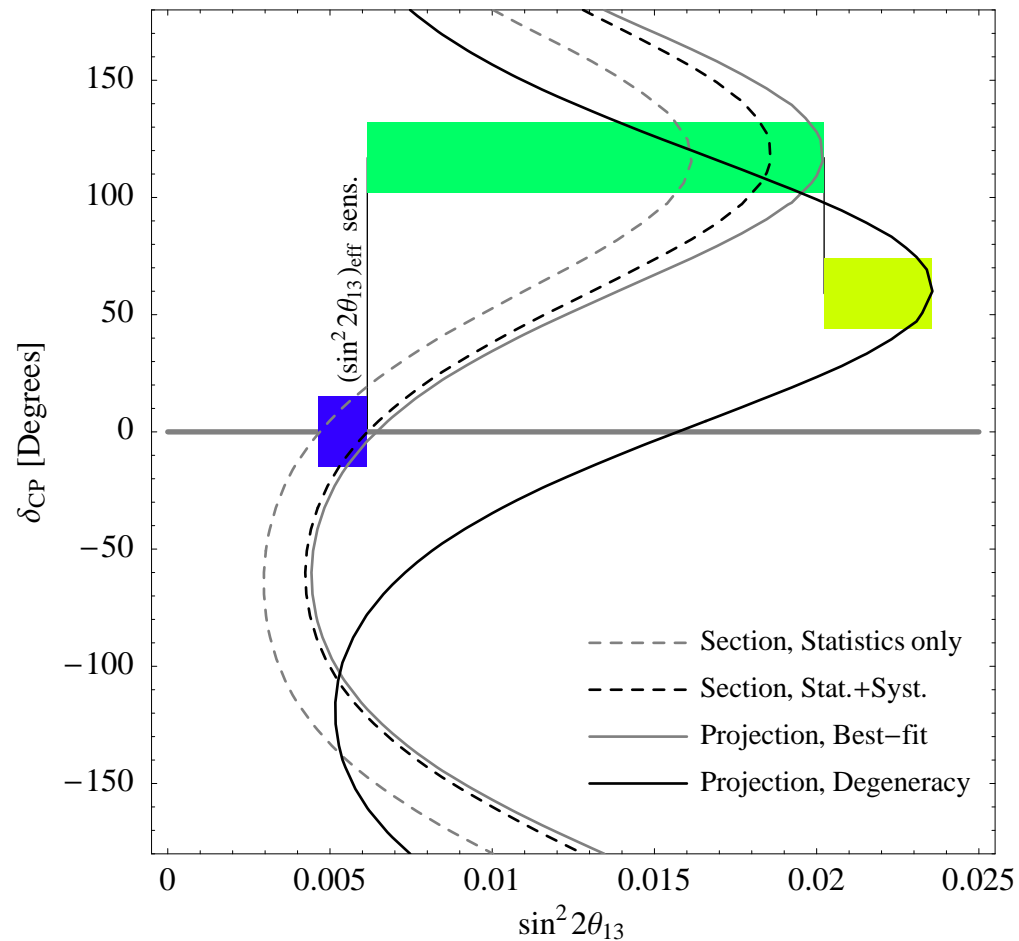
$$\Delta \equiv \frac{\Delta m_{31}^2 L}{4E_\nu}, \quad \hat{\alpha} \equiv \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \sin 2\theta_{12}, \quad A \equiv \frac{2E_\nu V}{\Delta m_{31}^2}$$

anti- ν : $\delta_{\text{CP}} \rightarrow -\delta_{\text{CP}}, A \rightarrow -A, \quad P_{e\mu}: \delta_{\text{CP}} \rightarrow -\delta_{\text{CP}}$

other hierarchy: $\Delta \rightarrow -\Delta, A \rightarrow -A, \hat{\alpha} \rightarrow -\hat{\alpha}$

Measuring θ_{13} by $\nu_{\mu} \rightarrow \nu_e$ at beams

T2K: $\delta - \theta_{13}$ correlation:



Huber, Lindner, Rolinec, TS, Winter, 2004

Measuring $\sin^2 2\theta_{13}$ at reactors

“Clean” measurement of $\sin^2 2\theta_{13}$:

$$P_{ee} \approx 1 - \sin^2 2\theta_{13} \sin^2 \frac{\Delta m_{31}^2 L}{4E_\nu} + \left(\frac{\Delta m_{21}^2 L}{4E_\nu} \right)^2 \cos^4 \theta_{13} \sin^2 2\theta_{12}$$

last term negligible for $\frac{\Delta m_{31}^2 L}{4E_\nu} \sim \pi/2$ and $\sin^2 2\theta_{13} \gtrsim 10^{-3}$

determination of θ_{13} is free of correlations and degeneracies

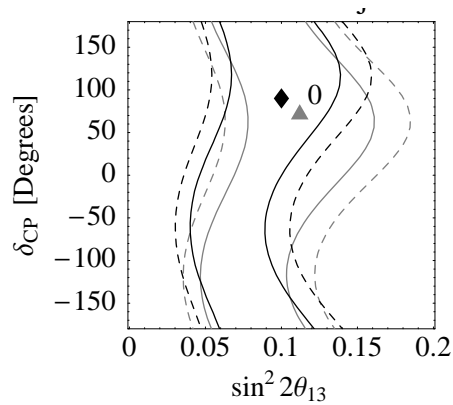
Minakata, Sugiyama, Yasuda, Inoue, Suekane, hep-ph/0211111

Huber, Lindner, TS, Winter, hep-ph/0303232

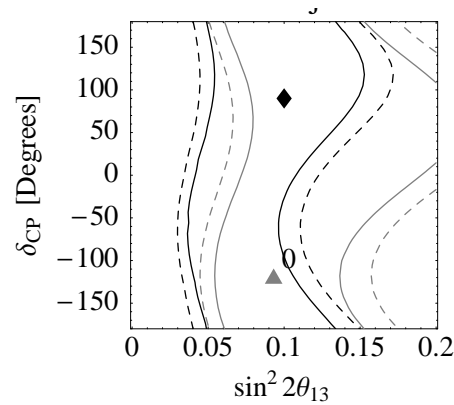
Measuring $\sin^2 2\theta_{13}$ at beams or reactors

assume $\sin^2 2\theta_{13} = 0.1$

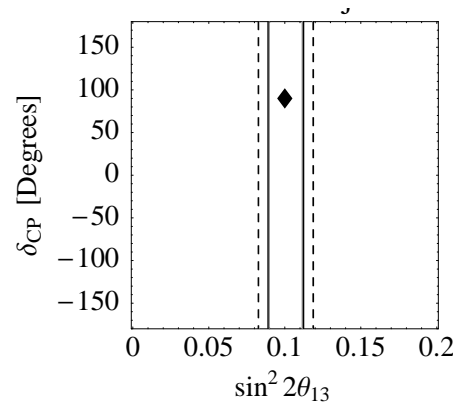
T2K



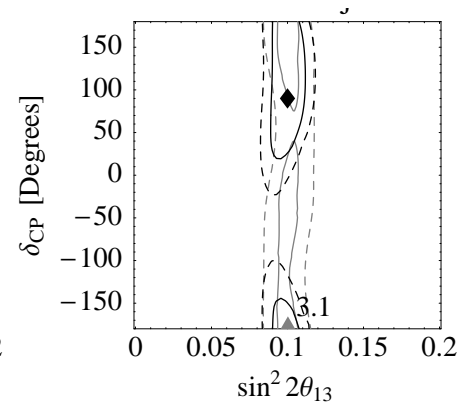
NO ν A



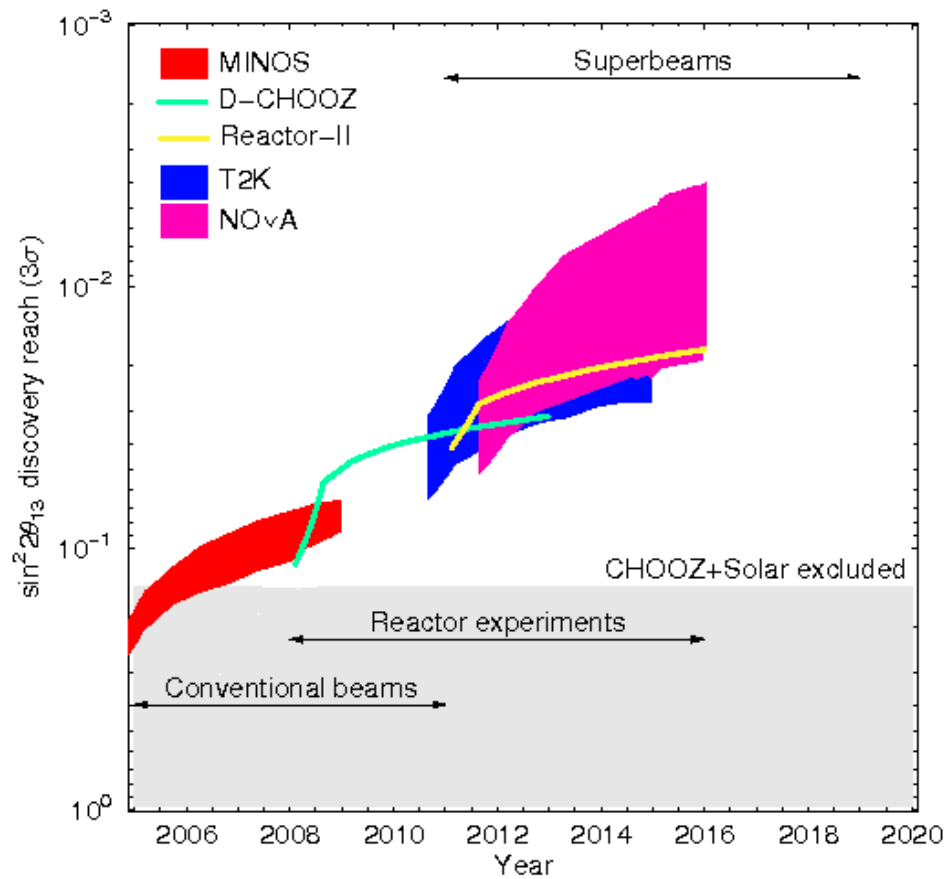
Daya Bay



combined



$\sin^2 2\theta_{13}$ discovery reach evolution

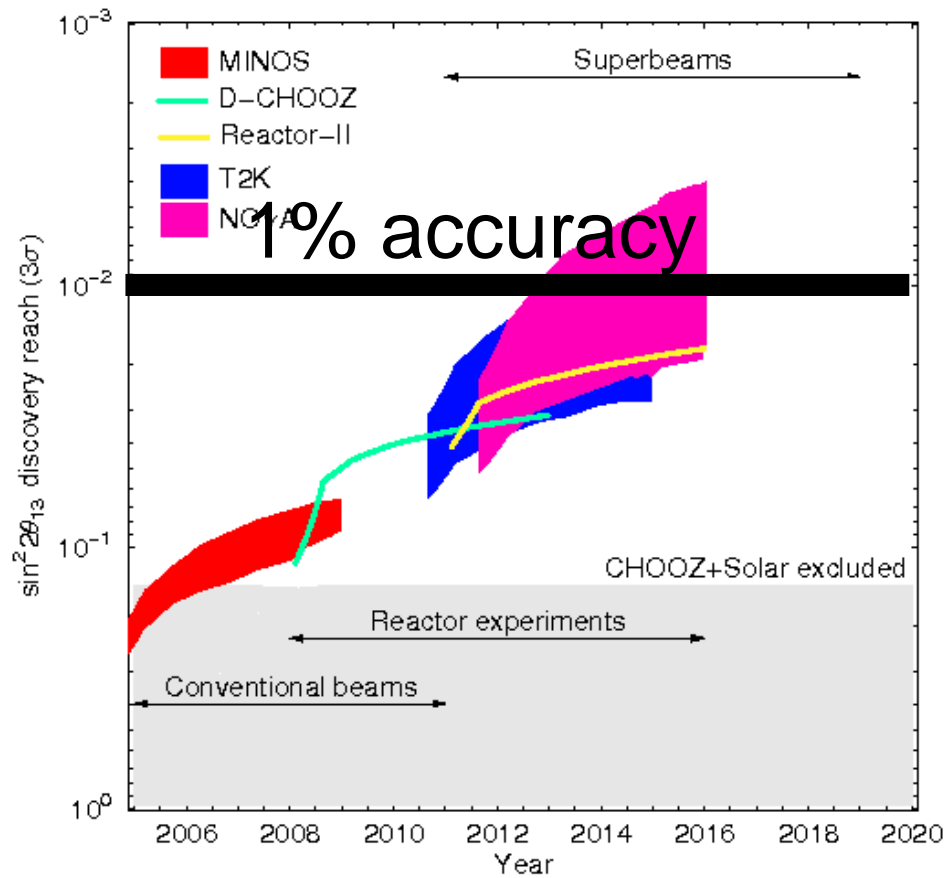


plot by W. Winter from
Albrow et al., hep-ex/0509019

$$\Delta m_{31}^2 = +2.5 \times 10^{-3} \text{ eV}^2$$
$$\sin^2 2\theta_{23} = 1$$

LBL exps.: neutrinos only

$\sin^2 2\theta_{13}$ discovery reach evolution



plot by W. Winter from
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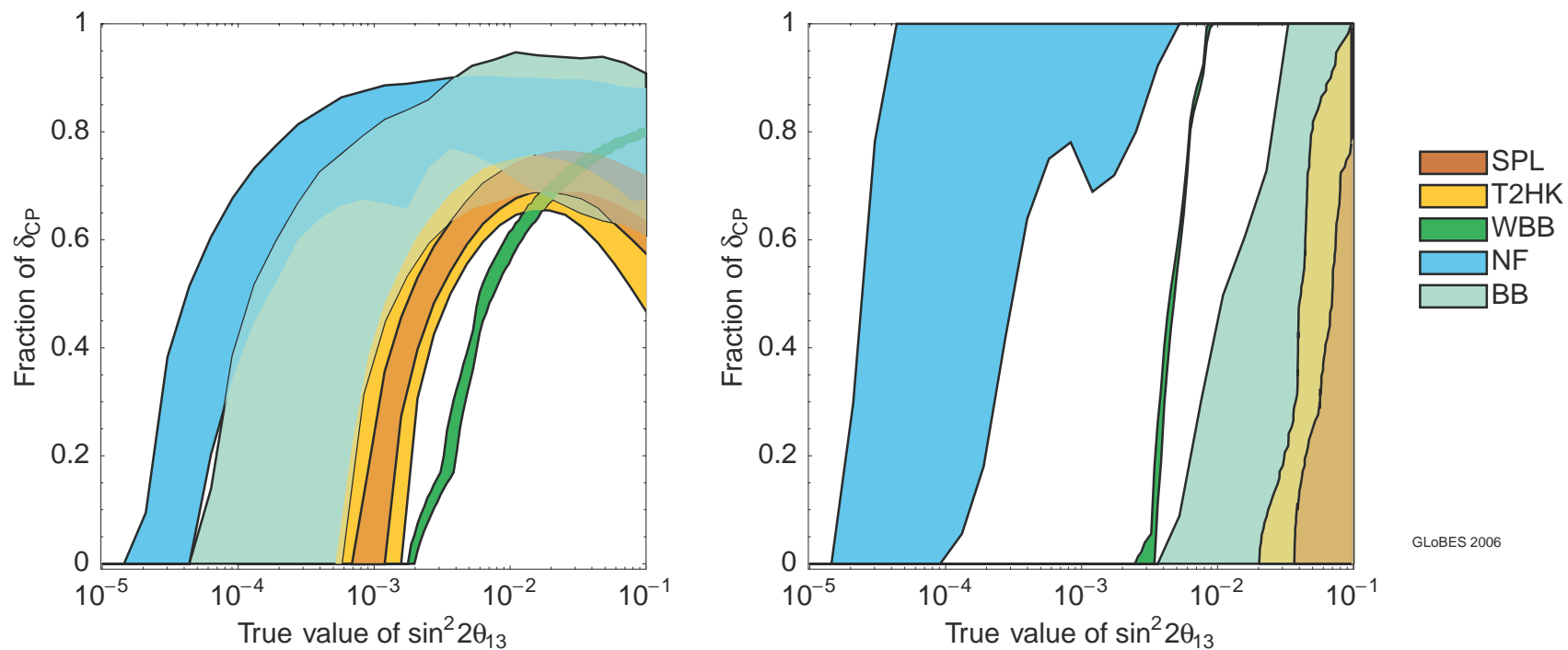
Going beyond the next generation of experiments

The ultimate goals:

- measure the value of δ_{CP}
establish CP violation
- determine the neutrino mass hierarchy
 $\rightarrow \text{sgn}(\Delta m_{31}^2)$

CPV, mass hierarchy sensitivities

The ISS Physics Working Group report [arxiv:0710.4947](https://arxiv.org/abs/0710.4947)



CP violation

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In theory: measure $P_{\nu_\alpha \rightarrow \nu_\beta}$ and $P_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta}$

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In practice:

- cross section and fluxes are different for ν and $\bar{\nu}$
- matter effect is CP violating

CP violation

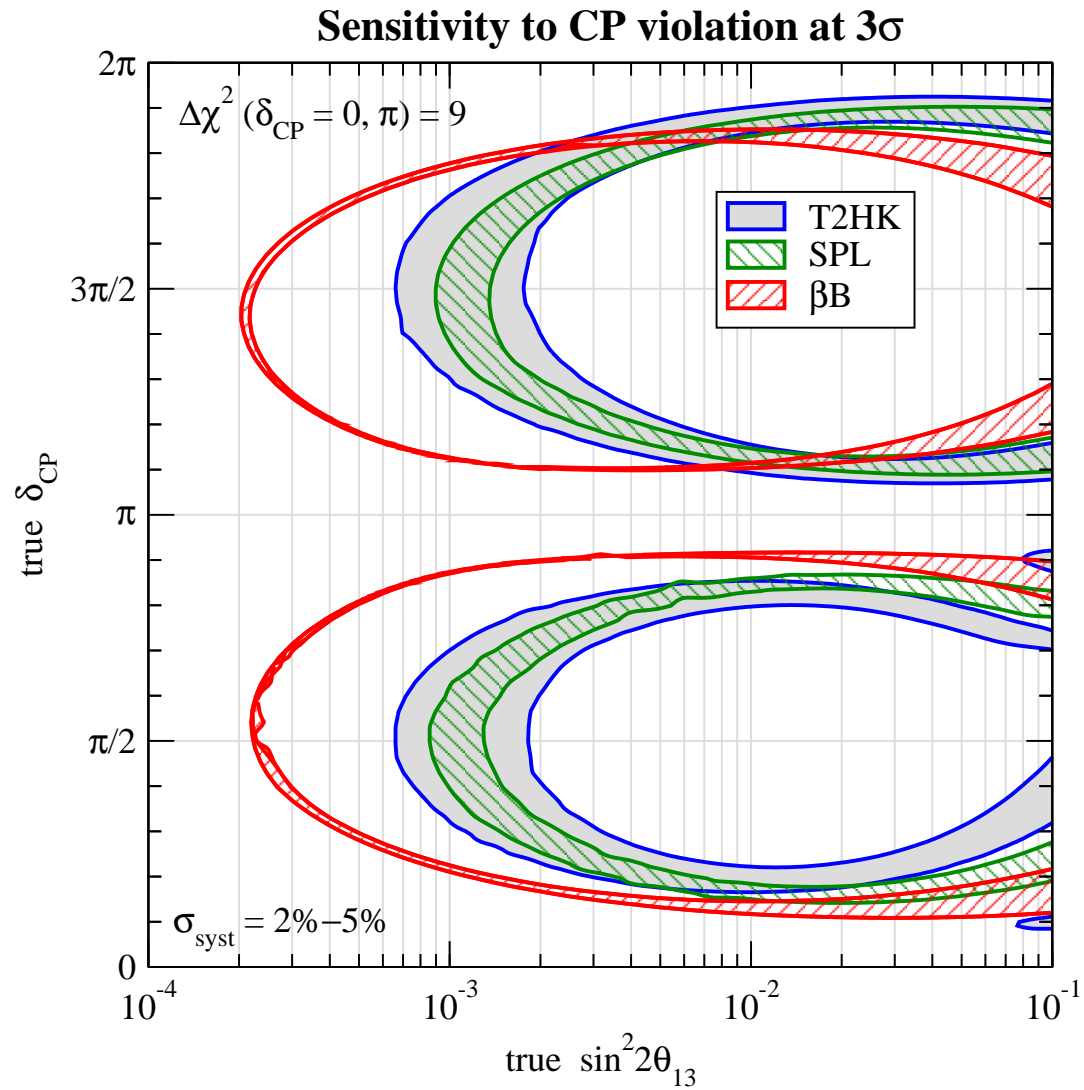
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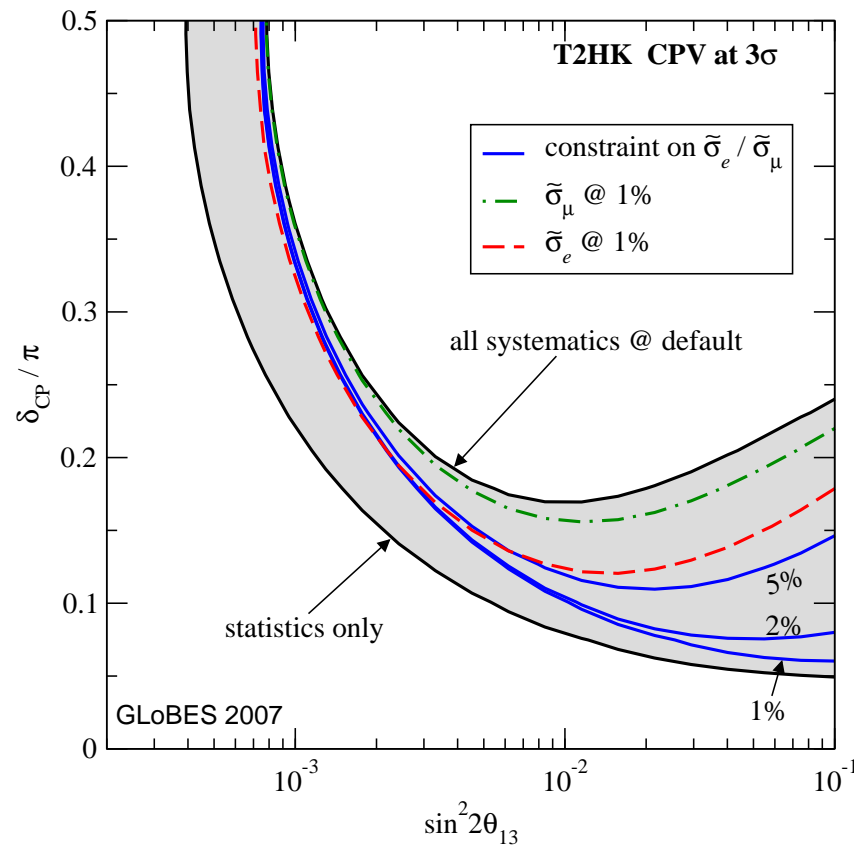
Assume standard 3-flavour oscillations
perform a parametric fit to δ

CP violation



Systematics in superbeam experiments

Uncertainties on fluxes and cross sections have a big impact on the sensitivity to CP violation:



Huber, Mezzetto, Schwetz, arXiv:0711.2950

Determination of the mass hierarchy

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the vacuum oscillation probability is invariant under

$$\Delta m_{31}^2 \rightarrow -\Delta m_{31}^2 \quad \delta_{\text{CP}} \rightarrow \pi - \delta_{\text{CP}}$$

→ the key to resolve the hierarchy degeneracy is the **matter effect**

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→ the key to resolve the hierarchy degeneracy is the **matter effect**

resonance condition for $\nu_\mu \rightarrow \nu_e$ oscillations:

$$\pm \frac{2EV}{\Delta m_{31}^2} = \cos 2\theta_{13} \approx 1$$

can be fulfilled for

neutrinos if $\Delta m_{31}^2 > 0$ (normal hierarchy)

anti-neutrinos if $\Delta m_{31}^2 < 0$ (inverted hierarchy)

Determination of the mass hierarchy

- LBL experiments need very long BL: $\gtrsim 1000$ km
wideband beam seems to be a very appealing option:
sensitivities somewhat below $\sin^2 2\theta_{13} = 10^{-2}$
(**WBB** FNL to DUSEL, 1290 km, or **T2KK**, 1050 km)

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 - Atmospheric neutrinos: Mt WC atm+LBL combination
Huber, Maltoni, Schwetz, 05, Campagne, Maltoni, Mezzetto, Schwetz, 06
magnetized detector (μ only) Petcov, Schwetz, hep-ph/0511277

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 - Combination of superbeam and beta beam works even at
relatively short baselines (130 km) Schwetz, hep-ph/0703279

Determination of the mass hierarchy

- LBL experiments need very long BL: $\gtrsim 1000$ km
wideband beam seems to be a very appealing option:
sensitivities somewhat below $\sin^2 2\theta_{13} = 10^{-2}$
(**WBB** FNL to DUSEL, 1290 km, or **T2KK**, 1050 km)
- If $\sin^2 2\theta_{13} \gtrsim 2 \times 10^{-2}$:
 - Atmospheric neutrinos: Mt WC atm+LBL combination
Huber, Maltoni, Schwetz, 05, Campagne, Maltoni, Mezzetto, Schwetz, 06
magnetized detector (μ only) Petcov, Schwetz, hep-ph/0511277
 - Combination of superbeam and beta beam works even at
relatively short baselines (130 km) Schwetz, hep-ph/0703279
- if $\sin^2 2\theta_{13} \ll 10^{-2}$ probably only a **NuFact** can determine the
hierarchy ($L >$ several 1000 km, e.g., 3000 & 7000)

Determination of θ_{13} , δ_{CP} , $\text{sgn}(\Delta m_{31}^2)$

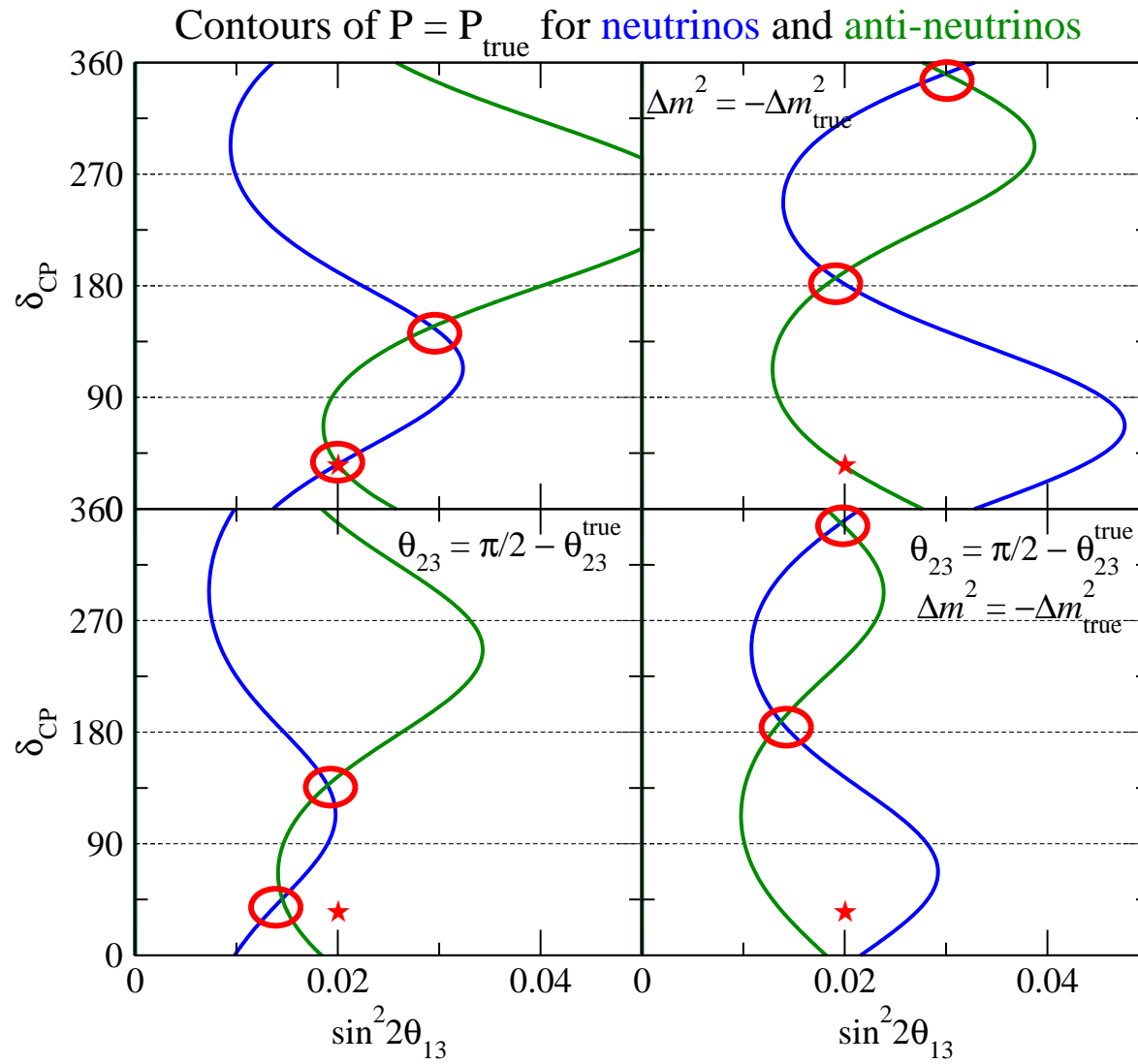
or the problem of

Degeneracies

G.L. Fogli, E. Lisi, Phys. Rev. D54 (1996) 3667; J. Burguet-Castell et al., Nucl. Phys. B608 (2001) 301; H. Minakata, H. Nunokawa, JHEP 10 (2001) 001; V.Barger, D.Marfatia, K.Whisnant, Phys. Rev. D65 (2002) 073023; D66 (2002) 053007; P.Huber, M.Lindner, W.Winter, Nucl. Phys. B645 (2002) 3; Nucl. Phys. B654 (2003) 3; J. Burguet-Castell et al., Nucl.Phys. B646 (2002) 301; O. Yasuda, New J. Phys. 6 (2004) 83; A.Donini, D.Meloni, S.Rigolin, JHEP 0406 (2004) 011

and many more

The eight-fold degeneracy



$$\Delta \hat{m}_{21}^2 = 7.9 \times 10^{-5} \text{eV}^2$$

$$\Delta \hat{m}_{31}^2 = 2.5 \times 10^{-3} \text{eV}^2$$

$$\sin^2 \hat{\theta}_{12} = 0.3$$

$$\sin^2 \hat{\theta}_{23} = 0.4$$

$$\sin^2 2\hat{\theta}_{13} = 0.02$$

$$\hat{\delta}_{\text{CP}} = 36^\circ$$

$$E_\nu = 2.2 \text{ GeV}$$

$$L = 812 \text{ km}$$

(NO ν A)

Resolving the degeneracies

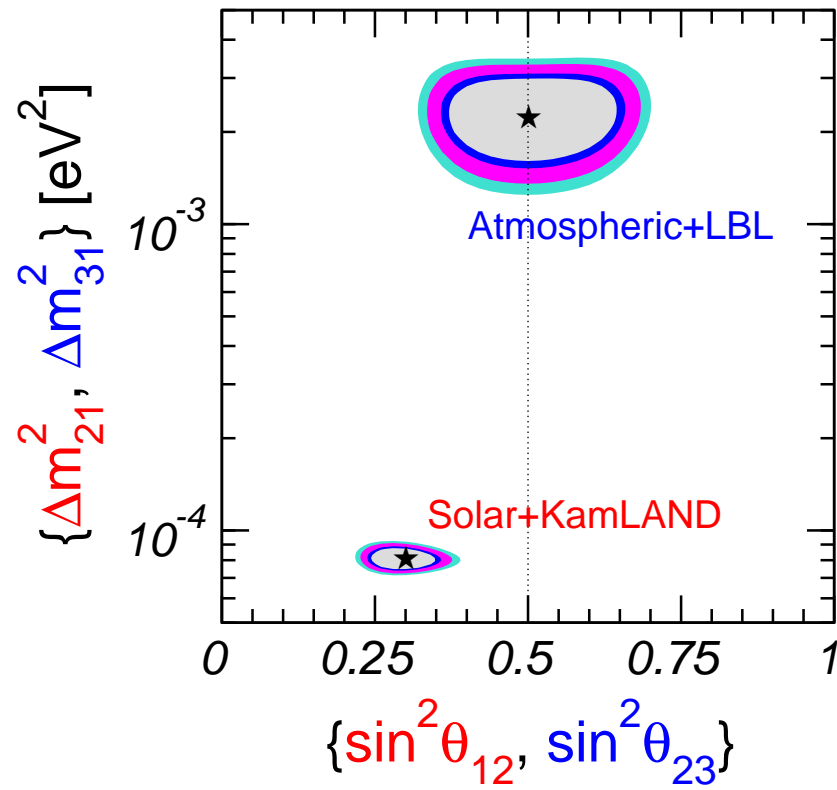
several possibilities to resolve the degeneracies are known:

- combining information from detectors at different baselines
- “Magic baseline” ~ 7000 km (NuFact)
- using additional oscillation channels ($\nu_e \rightarrow \nu_\tau$)
- spectral information (wide band beam)
- adding information on θ_{13} from a reactor experiment
- adding information from (Mt scale) atmospheric neutrino experiments
- ...

To conclude...

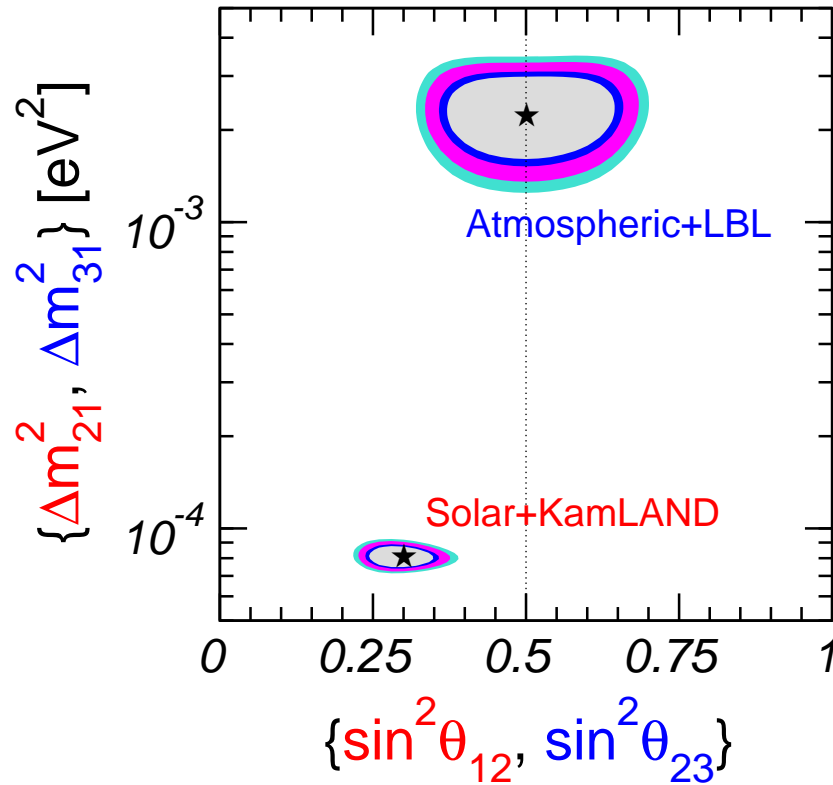
To conclude...

present status

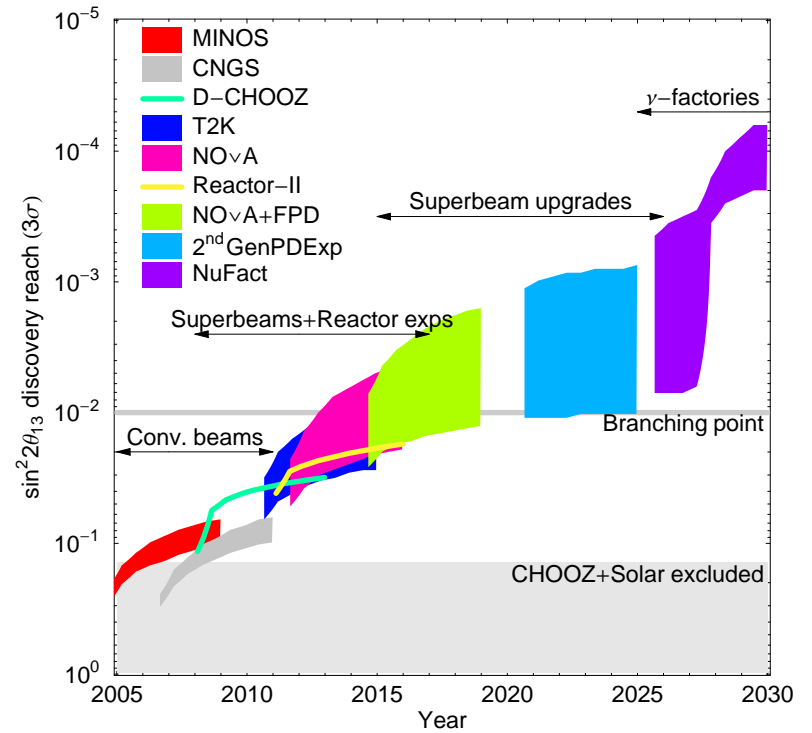


To conclude...

present status

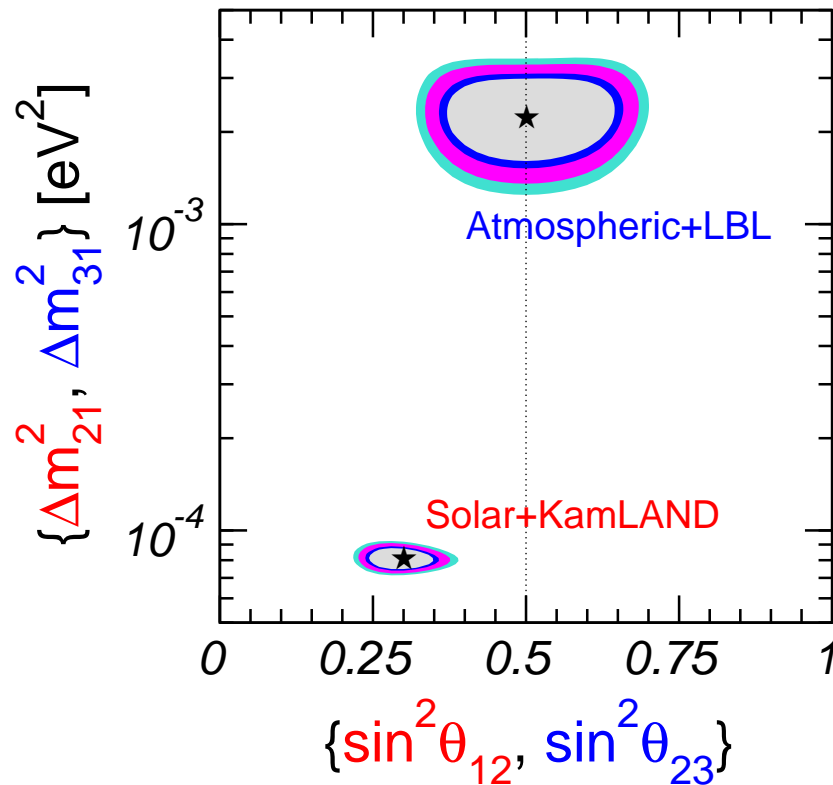


future

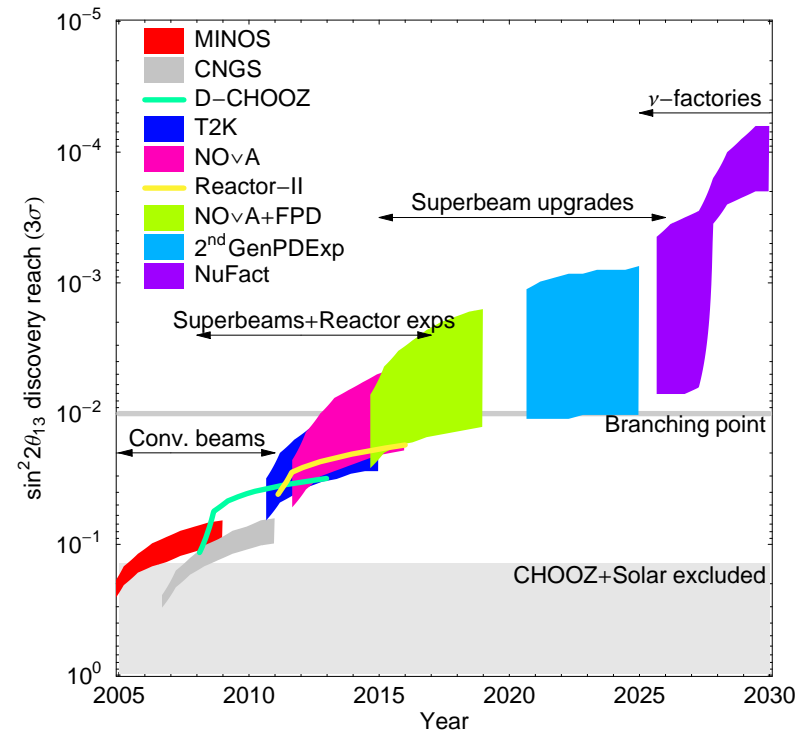


To conclude...

present status



future



Thanks for your attention!